

Surfaces Of Revolution (S.O.R.)

Part I

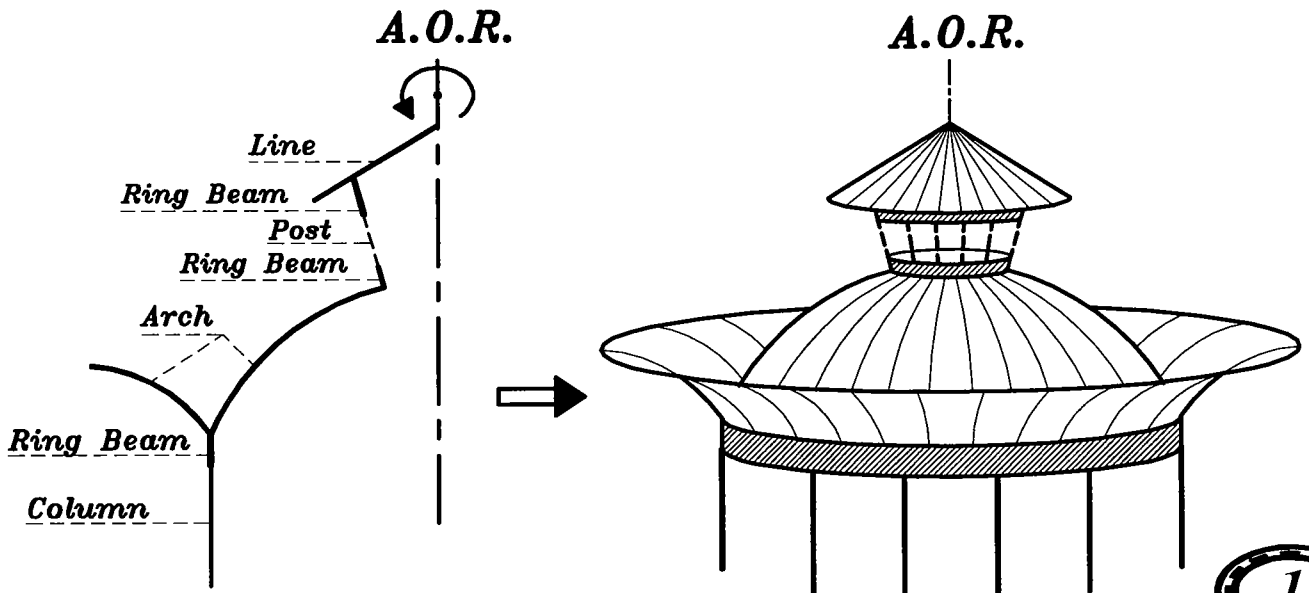
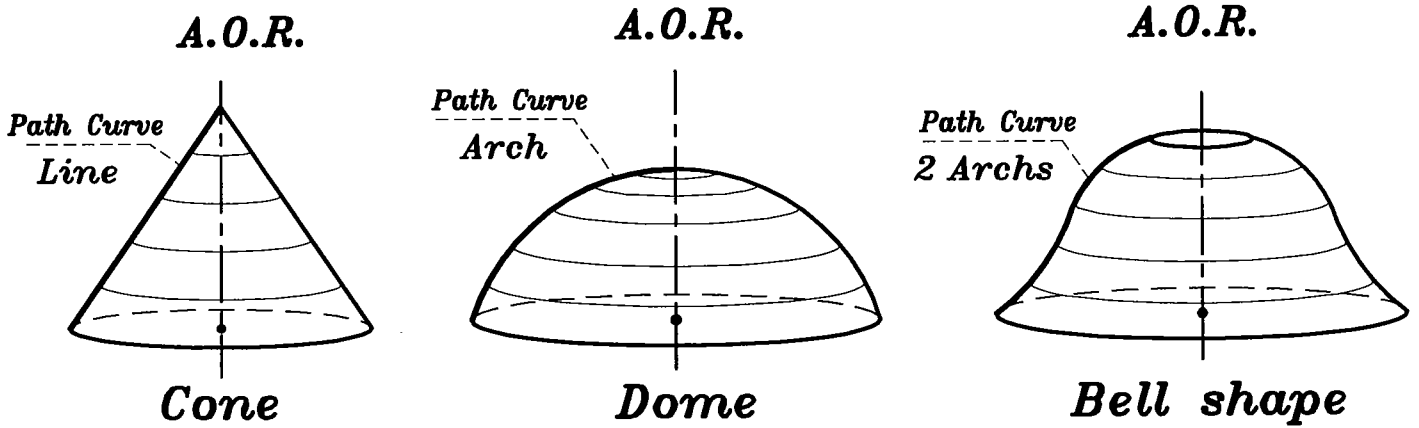
الأسطح الدورانية

هى عبارة عن أسطح رقيقة (غشاء) تنشأ من دوران منحنى (*Path Curve*) حول محور رأسى يسمى محور الدوران (*Axis Of Revolution (A.O.R.)*)

وال (*Path Curve*) عبارة عن المنحنى الذى يدور أفقياً دوره كامله و ممكن أن يكون خط مستقيم أو قطعه من دائره (*Arch*) أو قطع ناقص (*Parabola*) أو أى منحنى آخر .

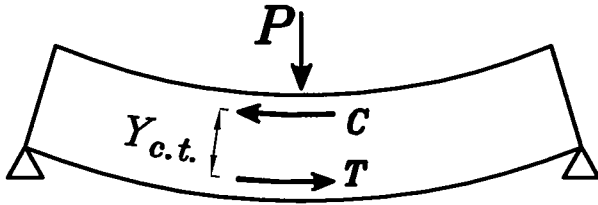
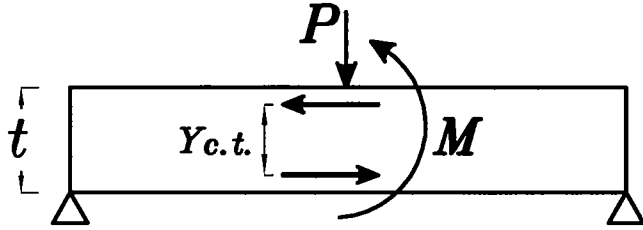
Definition.

Surfaces Of Revolution is a surfaces has a membrane behavior created by rotation of a curve called Path Curve around vertical axis called Axis Of Revolution (A.O.R.)



Membrane Theory.

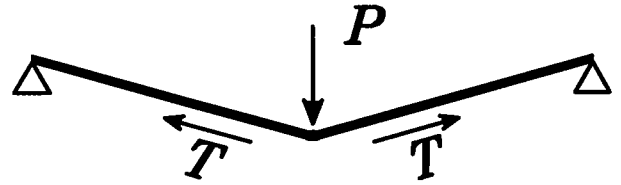
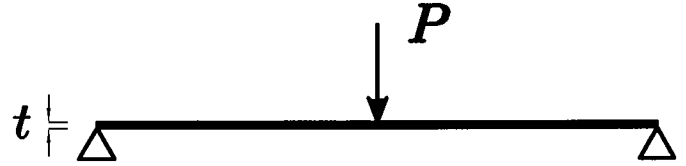
Beam or slab thickness (t)
has a big value.



Bending Moment
Compression & Tension

نظريه الغشاء (القشره)

Shell (membrane) thickness (t)
has a very small value.



Axial Force
Compression only
or
Tension only

نظرا لصغر سُمك الأشكال القشريه (*Shells*) و صغر سُمك الأسطح الدورانيه فعند تعرضها للاحمال لن تكون هناك تخانه (t) كافيه ليحدث لها **Bending** أى أن يحدث لجزء **Compression** و الآخر **Tension** لكن الاحمال المؤثره تسبب ان يكون كل القطاع معرض اما لـ **Compression** فقط او لـ **Tension** فقط.

أى أن ال **Inertia** للقطاع صغيره جدا فلا يكون هناك **Bending Rigidity**. فتقاوم هذه المنشآت الأحمال الواقعه عليها عن طريق (**Axial Forces**) فقط و لا توجد مقاومه للـ (**Bending Moments**)

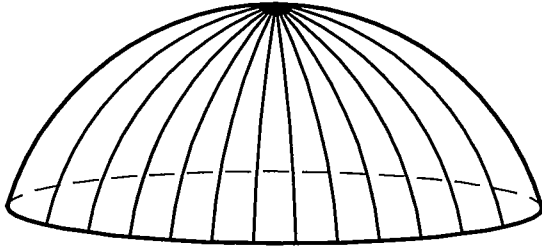
Because of the very small thickness of the shell, it works as a membrane, Which has No Bending Rigidity. Means NO Bending Moment acting on the shell. Only Axial Forces [Meridian Force (T_1) & Ring Force (T_2)] acting on the Shell.

Definitions & Signs.

هناك بعض التعريفات المعمه و الاشارات (الموجبه و السالبه) التى يجب ان نعرفها أولا .

* Meridian Direction & Ring Direction.

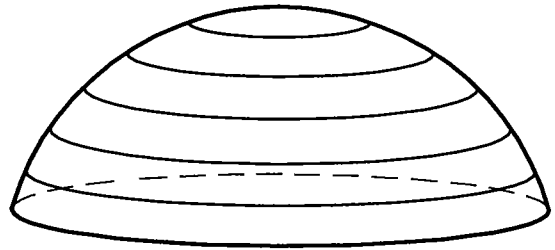
و هى عبارة عن اتجاهات القوى المؤثره على ال Surface



Meridian Direction.

هو الاتجاه الطولى (الرأسى)

و يأخذ نفس شكل ال Path Curve



Ring Direction.

هو الاتجاه الدائرى العرضى (الافقى)

و دائها مركزه هو محور الدوران

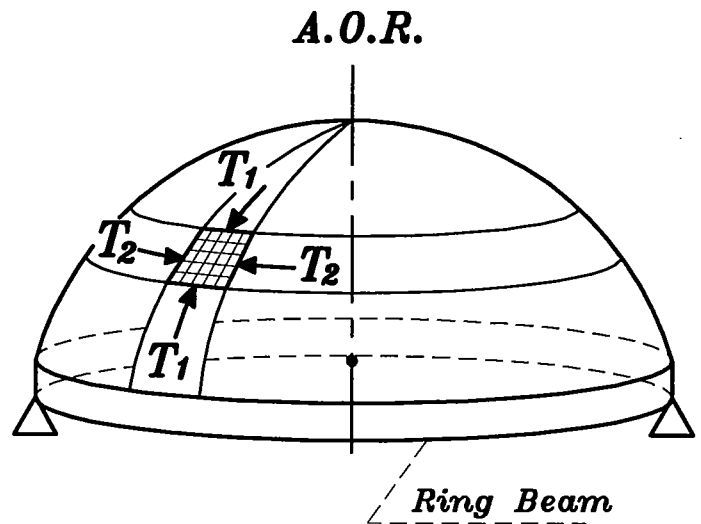
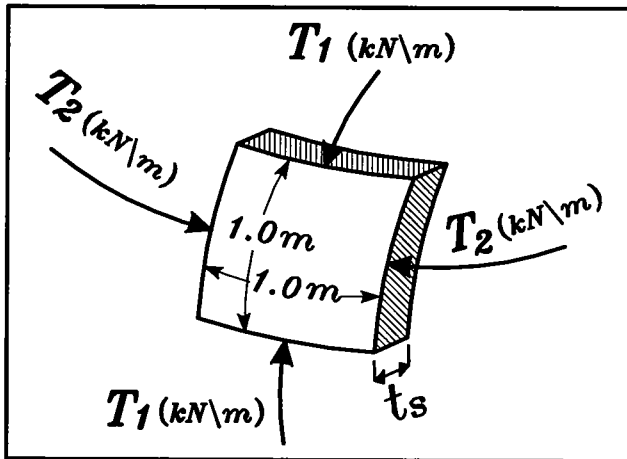
* Internal Forces (T_1) & (T_2).

هى قوى الضغط أو الشد المؤثره على 1.0 m طولى من السطح فى الاتجاهين

Meridian direction واتجاه *Ring direction*

T_1 is Meridian Force. (kN/m)

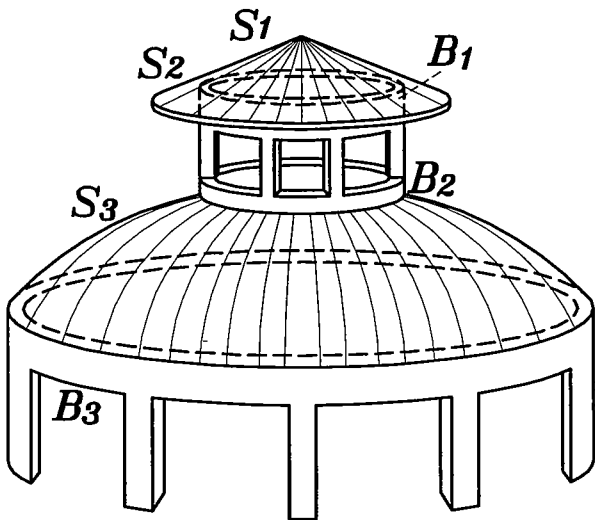
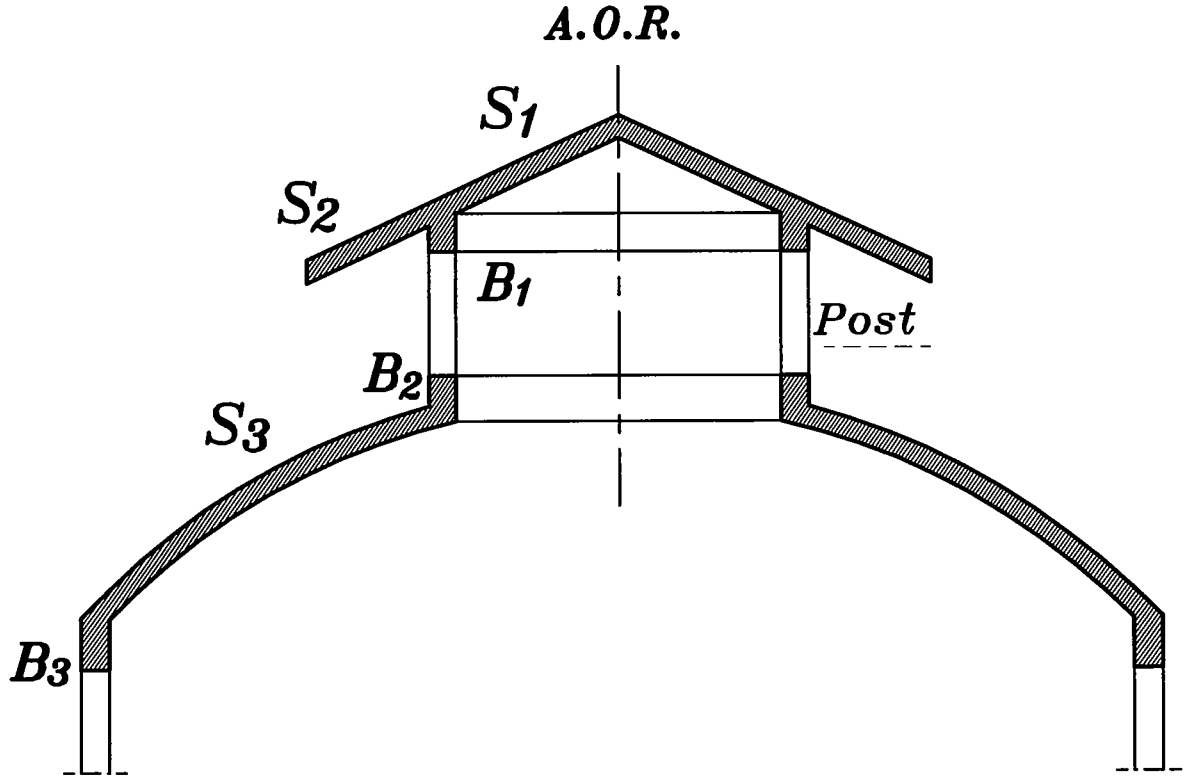
T_2 is Ring Force. (kN/m)



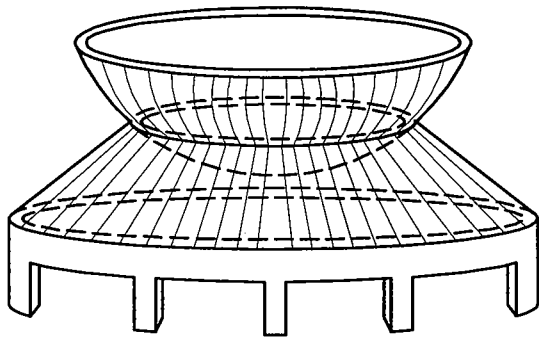
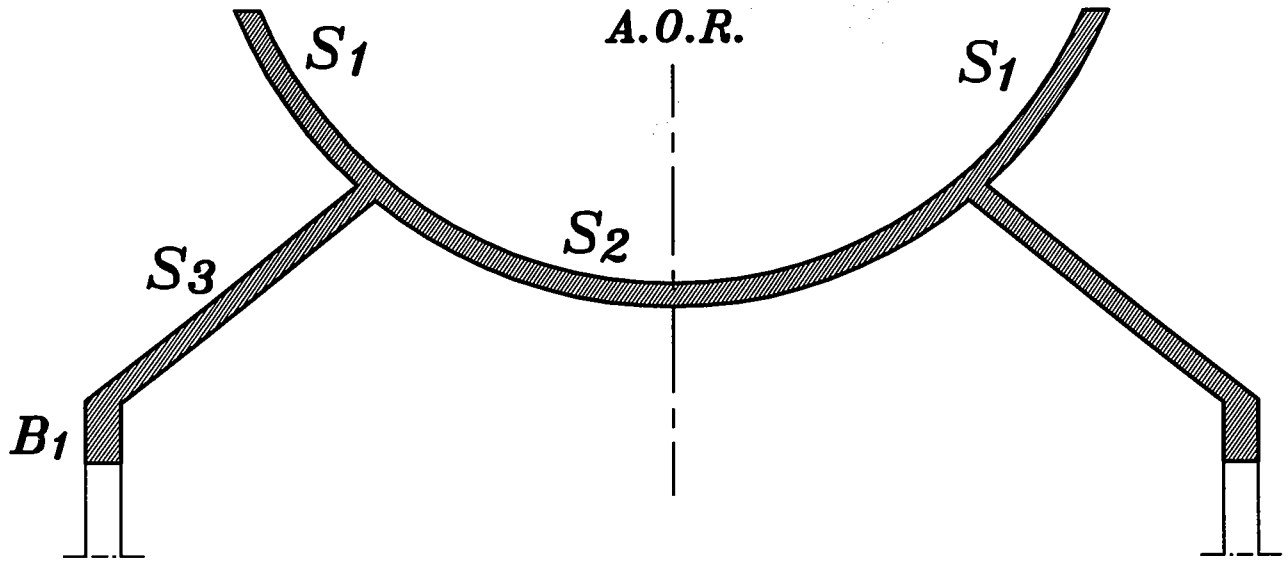
Signs of T_1 & T_2	+Ve \rightarrow Compression
	-Ve \rightarrow Tension

* Shell Surface.

و هى الاسطح الدورانيه التى يكونها ال *path curve* و تكون دائما محموله على *support* واحد فقط و هو اما كمره دائريه *Ring Beam* او محموله على سطح اخر .
و يتم تحليل القوى فى كل سطح على حده ما دام بينهم ركيزه *support*



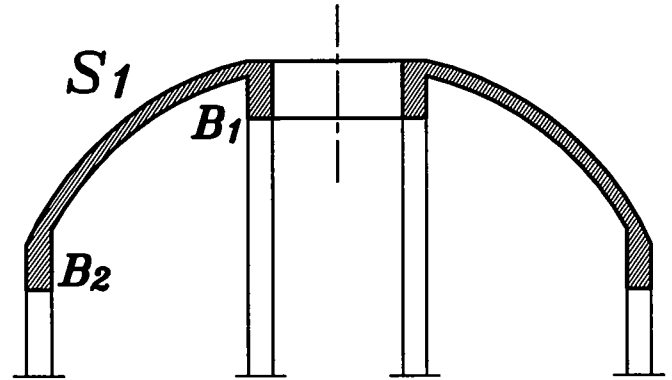
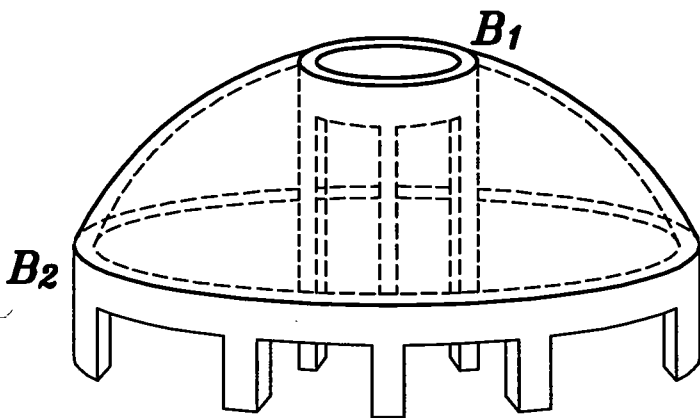
- السطح S_1 محمول على الكمره B_1
- السطح S_2 محمول على الكمره B_1
- الكمره B_1 محموله على ال *Posts*
- ال *Posts* محموله على الكمره B_2
- الكمره B_2 محموله على السطح S_3
- السطح S_3 محمول على الكمره B_3
- الكمره B_3 محموله على الاعمده



- السطح S_1 محمول على السطح S_3
- السطح S_2 محمول على السطح S_3
- السطح S_3 محمول على الكمره B_1
- الكمره B_1 محموله على الاعمده

ملحوظه هامه .

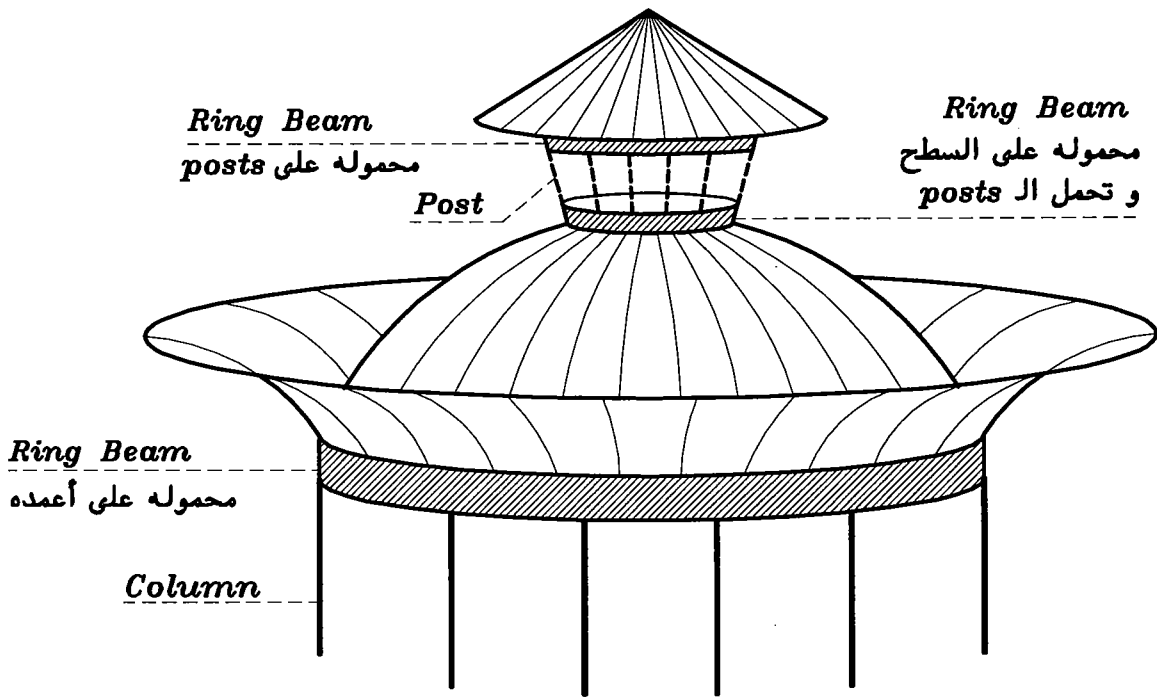
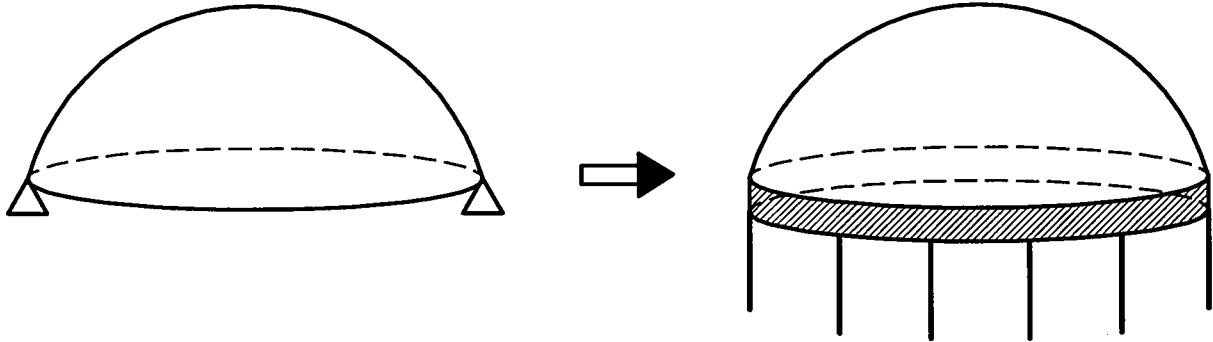
فى هذا الملف لن نتناول تحليل الاسطح المحموله على اكثر من *support* حيث يتم تحليلها بالكمبيوتر .



لن نستطيع تحليل السطح S_1 لانه محمول على $2 supports$ لذا يجب تحليله بالكمبيوتر

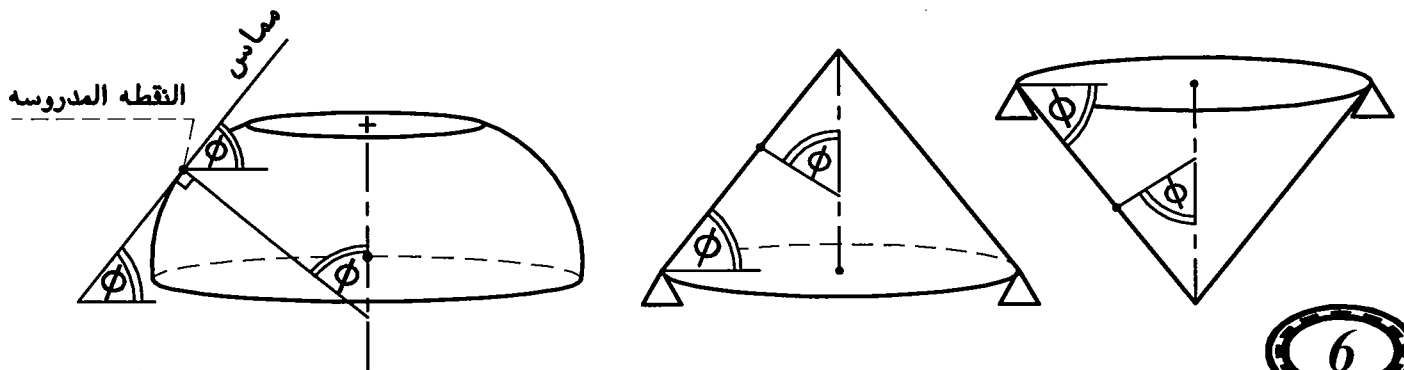
* Ring Beams.

الكمرات الدائرية تعتبر *support* للأسطح الدورانية .
و تكون محمولة على أعمده أو *posts* او تكون محمولة على السطح الدوراني و تحمل ال *posts*



* ϕ

ϕ هي زاوية ميل المماس للسطح عند النقطة المدروسة مع المستوى الافقى .
و في حاله اذا كان المنحنى عباره عن خط مستقيم تكون ال ϕ هي زاوية ميل هذا الخط مع الافقى .

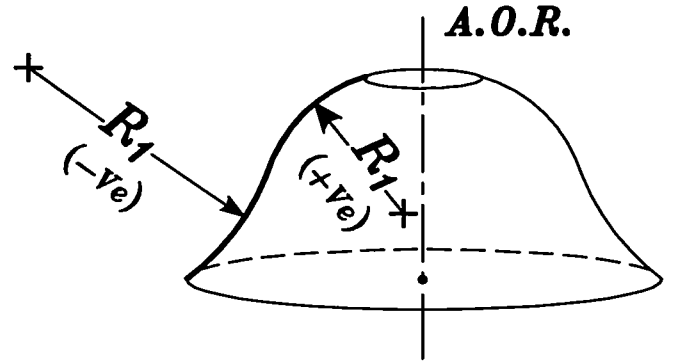


* R_1

R_1 هو نصف قطر المنحني (Path Curve)

R_1 (+Ve) Sign
عندما تكون خارجه بعيدا عن ال (A.O.R.)

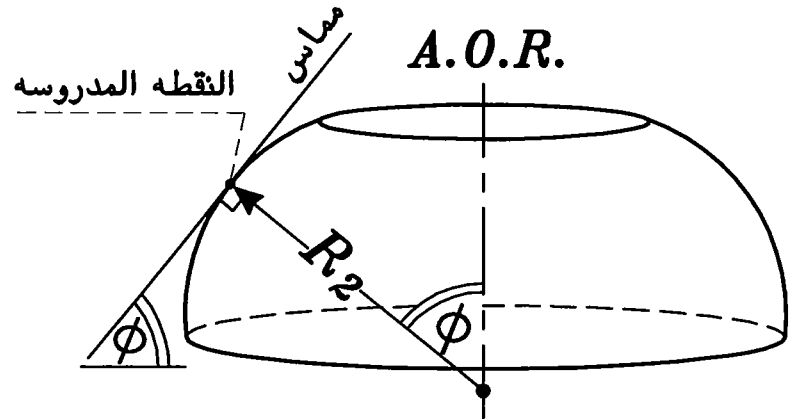
R_1 (-Ve) Sign
عندما تكون داخله فى اتجاه ال (A.O.R.)



* R_2

R_2 هو البعد العمودى على المماس من النقطة المدروسة حتى (A.O.R.)
و زاويه ميله مع الرأسى هى ϕ

R_2 دائما اشارتها (+Ve)

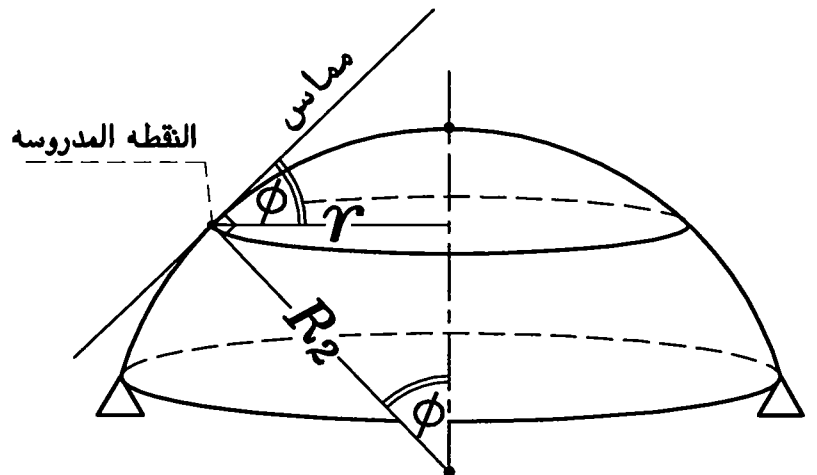


* r

r هو نصف قطر الدائره الافقيه عند النقطة المدروسة

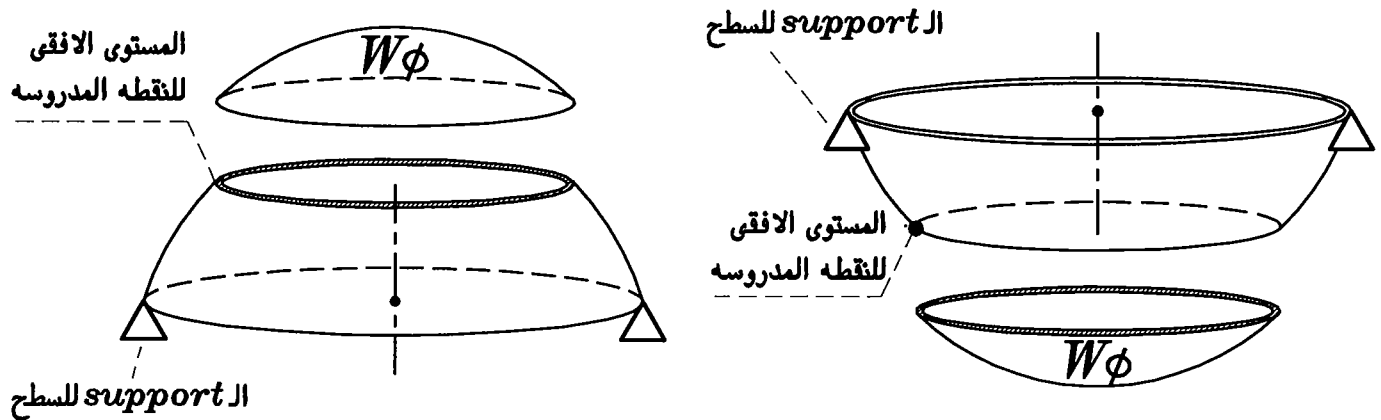
$$r = R_2 * \sin \phi$$

r دائما اشارتها (+Ve)



* W_ϕ

W_ϕ هي مجموع الازان الرأسية المحسوبة عند المستوى الأفقي عند النقطة المدروسة لسطح معين محسوبة من الجهة البعيدة للـ *support* الذي يحمل هذا السطح .



$$D.L. = g = t_s \delta_c + F.C. = \checkmark \text{ (kN/m}^2\text{)}$$

$$L.L. = P = \checkmark \text{ (kN/m}^2\text{) H.P. (Horizontal Projection)}$$

$$\text{Water Weight} = \delta_w * \text{Volume}$$

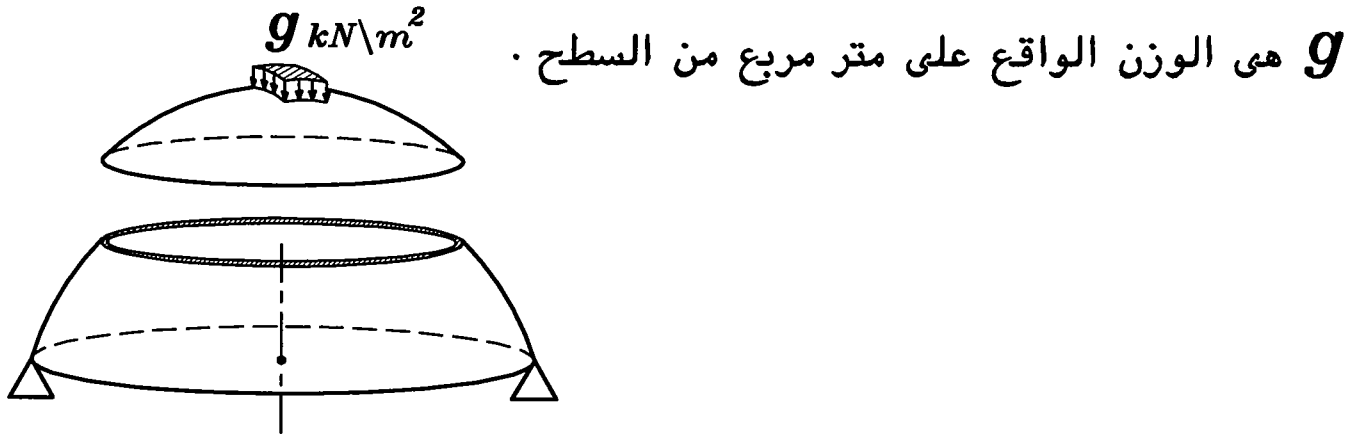
$$\delta_w = 10.0 \text{ (kN/m}^3\text{)}$$

$$\text{In Case of No Water} \longrightarrow W_\phi = W_{\phi D.L.} + W_{\phi L.L.}$$

$$\text{In Case of Water} \longrightarrow W_\phi = W_{\phi D.L.} + W_{\phi \text{Water}}$$

$$\underline{\underline{W\phi_{D.L.}}}$$

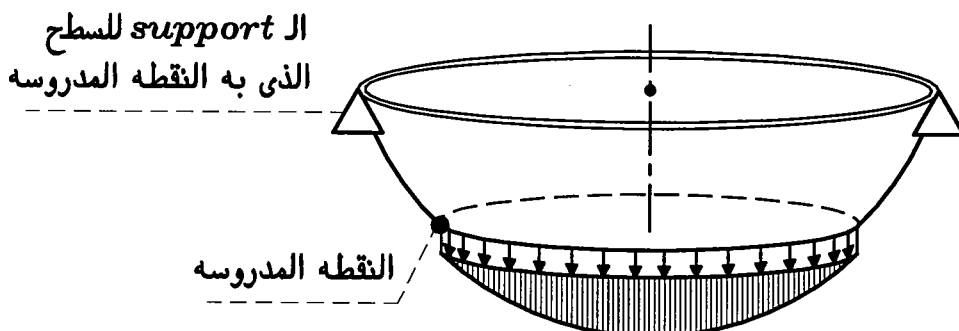
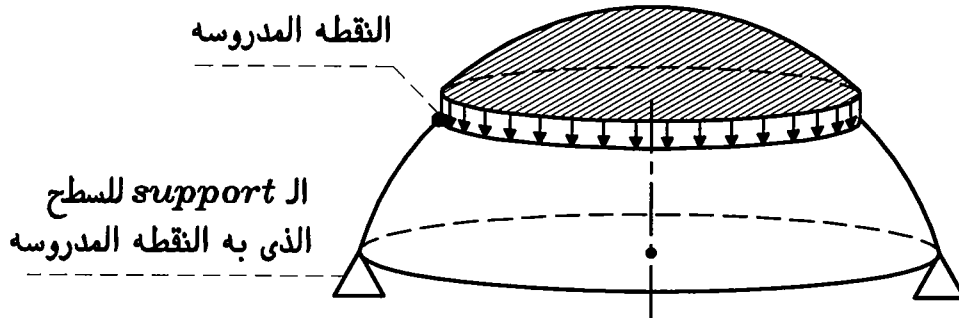
$$D.L. = g = t_s \delta_c + F.C. = \checkmark (kN/m^2)$$



$W\phi_{D.L.}$ هو محصلة الوزن من الجبهة البعيدة عن ال $support$

$$W\phi_{D.L.} = g * S.A. = \checkmark (kN) \quad \boxed{S.A. = Surface Area}$$

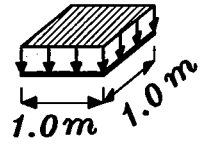
$$W\phi_{D.L.} = g * Surface Area$$



$$W\phi_{D.L.} = g * Surface Area$$

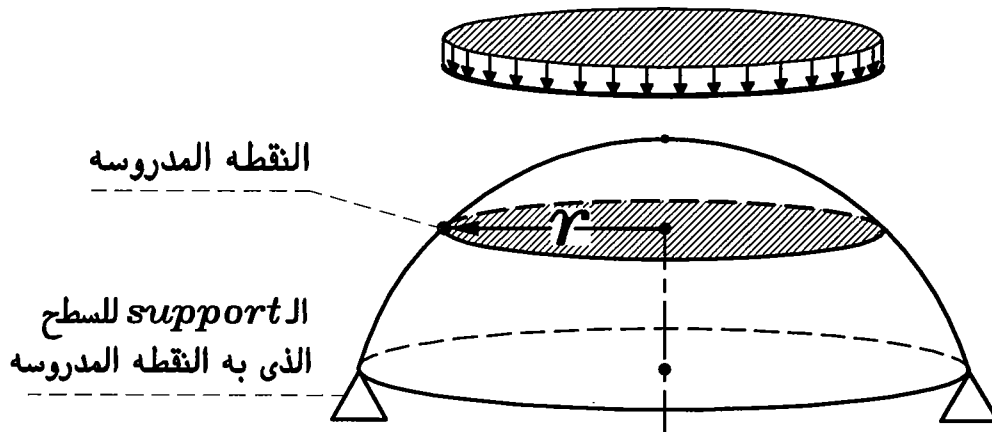
$$\underline{W_{\phi_{L.L.}}}$$

$$L.L. = P = \sqrt{(kN/m^2) H.P. (Horizontal Projection)}$$



$$W_{\phi_{L.L.}} = P * Projected Area = P * \pi r^2 = \sqrt{(kN)}$$

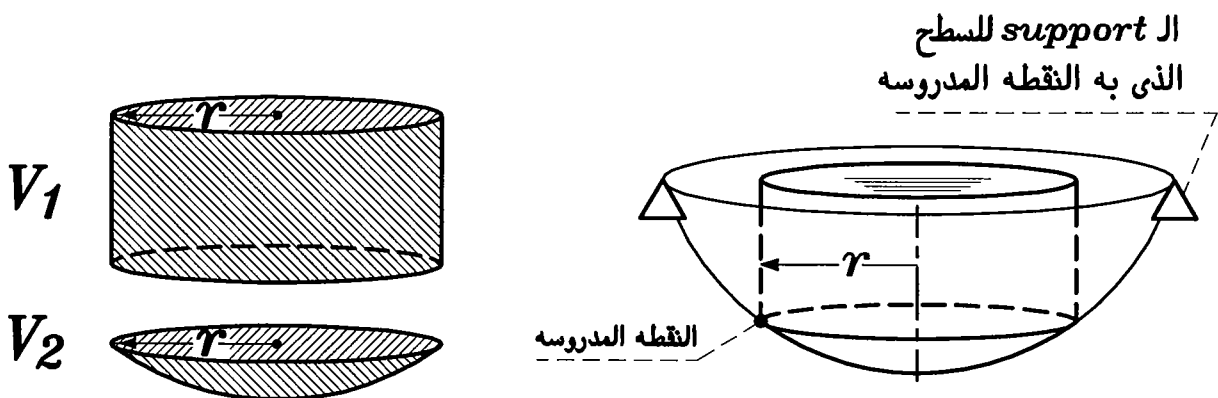
$$W_{\phi_{L.L.}} = P * Projected Area$$



$$\underline{W_{\phi_{Water}}}$$

$$W_{\phi_{Water}} = \delta_w * Volume \quad \delta_w = 10.0 (kN/m^3)$$

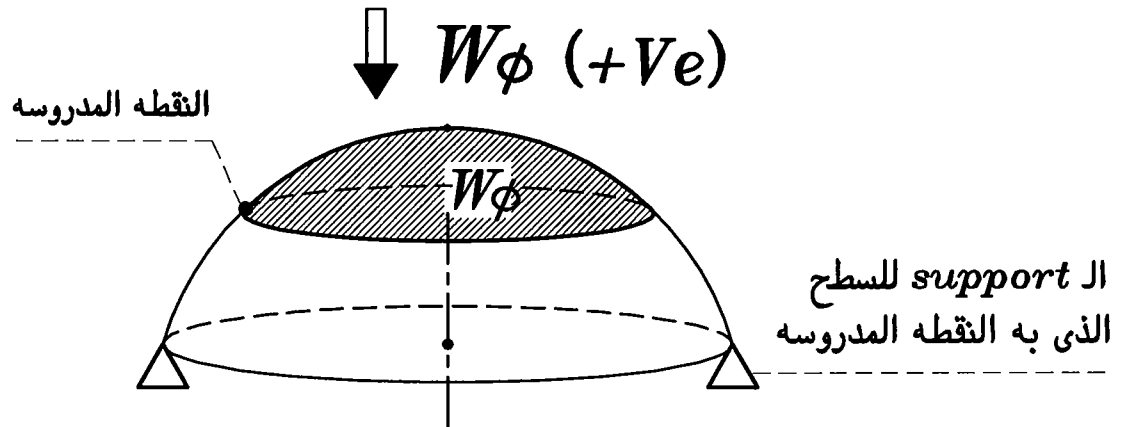
Volume هو مجموع حجم الماء فوق المستوى الافقى للنقطة المدروسة للسطح من الجبهه البعيده لا *support* الذي يحمل هذا السطح .



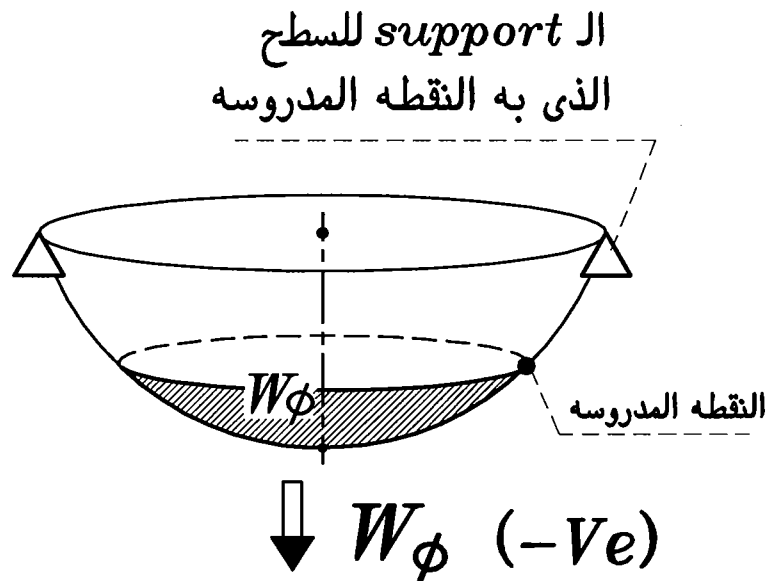
$$W_{\phi_{Water}} = \delta_w * (V_1 + V_2)$$

Signs of W_ϕ

$(+Ve)$ Sign عندما يكون اتجاه ال W_ϕ داخل الى ال $Support$

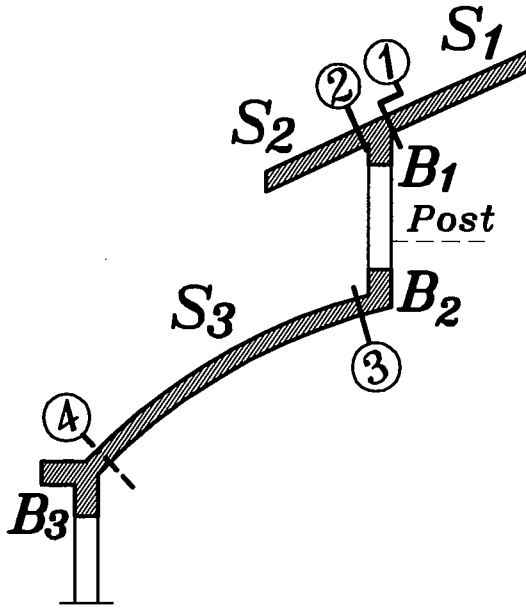


$(-Ve)$ Sign عندما يكون اتجاه ال W_ϕ خارج من ال $Support$



Special Cases of Calculating W_ϕ

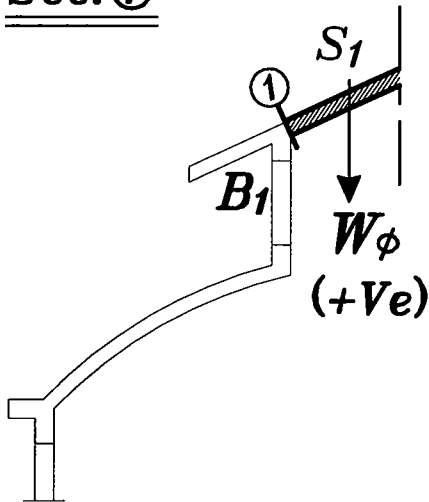
A.O.R.



الكمرة B_1 هي ال support للسطحين S_1 & S_2

الكمرة B_3 هي ال support للسطح S_3

Sec. ①

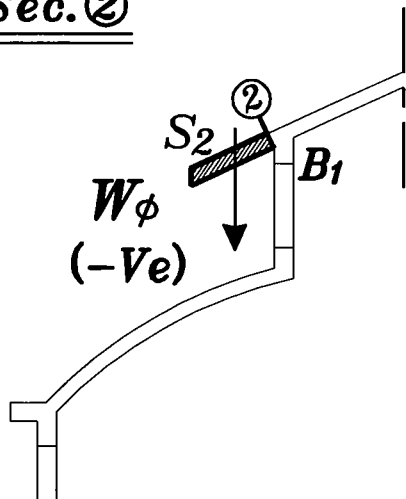


Sec. ① موجود في السطح S_1

الكمرة B_1 هي ال support للسطح S_1

W_ϕ (Sec. 1) = Total Loads on Slab S_1

Sec. ②



Sec. ② موجود في السطح S_2

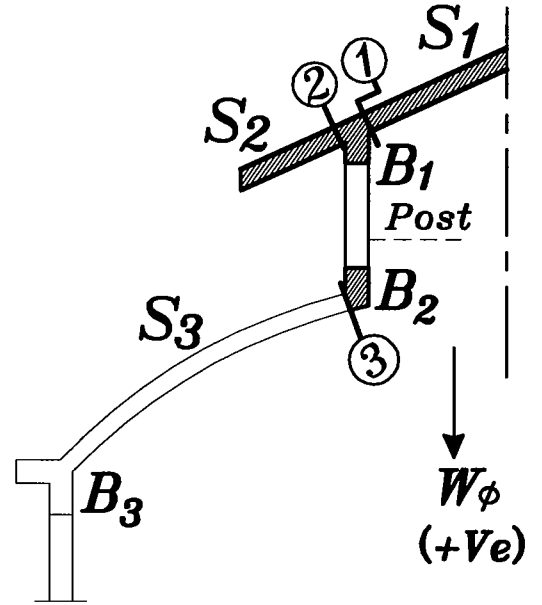
الكمرة B_1 هي ال support للسطح S_2

W_ϕ (Sec. 2) = Total Loads on Slab S_2

Sec. ③

Sec. ③ موجود فى السطح S_3

الكمره B_3 هى ال support للسطح S_3

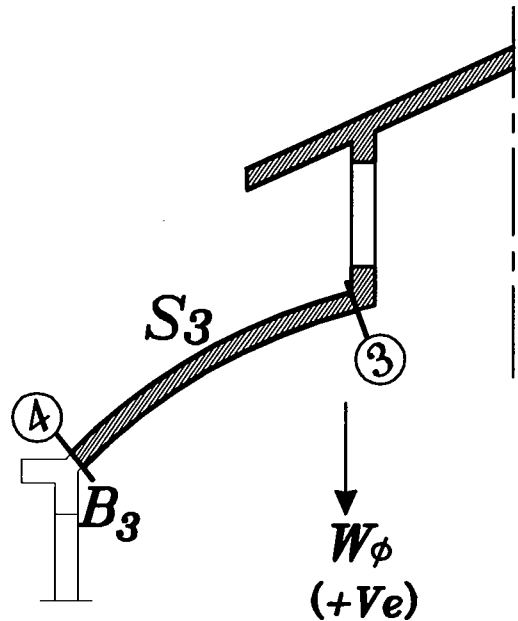


$$W_{\phi} (Sec. 3) = W_{\phi} (Sec. 1) + W_{\phi} (Sec. 2) \\ + \text{Total weight of Beam } (B_1) \\ + \text{Weight of all Posts} \\ + \text{Total weight of Beam } (B_2)$$

Sec. ④

Sec. ④ موجود فى السطح S_3

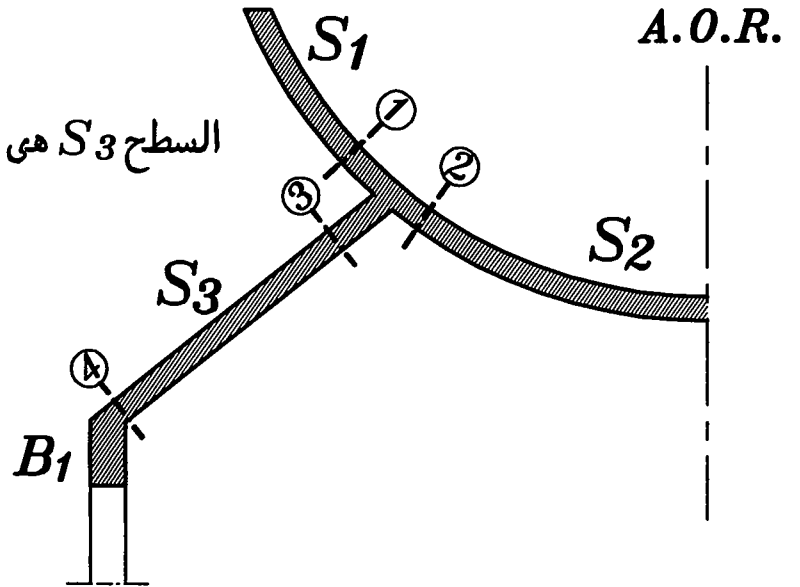
الكمره B_3 هى ال support للسطح S_3



$$W_{\phi} (Sec. 4) = W_{\phi} (Sec. 3) + \text{Total Loads on Slab } S_3$$

Special Case.

السطح S_3 هي ال support للسطحين S_1 & S_2

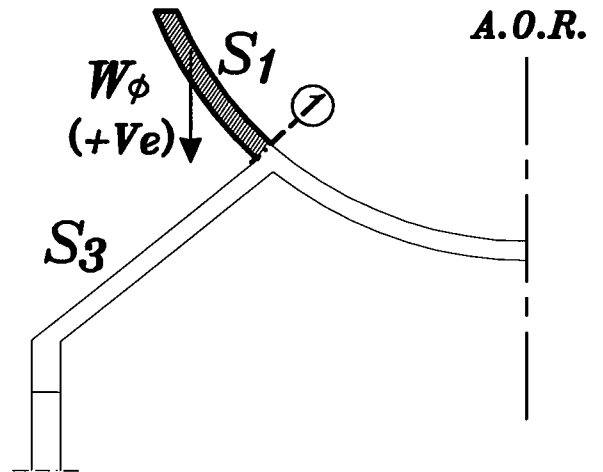


Sec. ①

Sec. ① موجود في السطح S_1

السطح S_3 هو ال support للسطح S_1

W_ϕ (Sec. 1) = Total Loads on Slab S_1

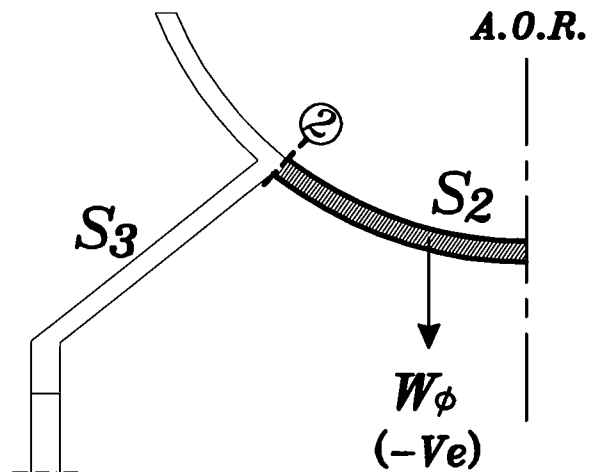


Sec. ②

Sec. ② موجود في السطح S_2

السطح S_3 هو ال support للسطح S_2

W_ϕ (Sec. 2) = Total Loads on Slab S_2

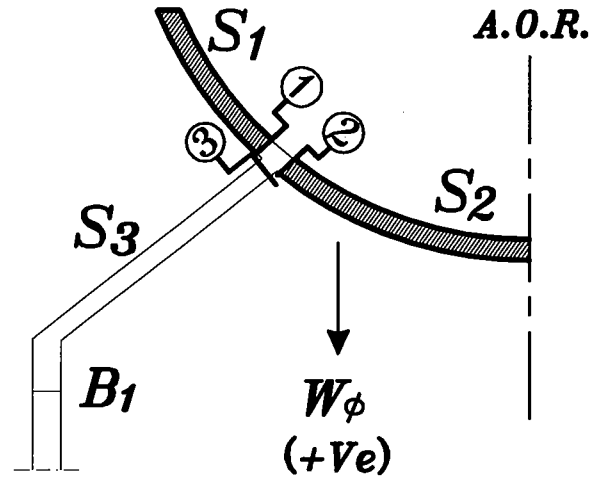


Sec. ③

Sec. ③ موجود في السطح S_3

الكمرة B_1 هي ال support للسطح S_3

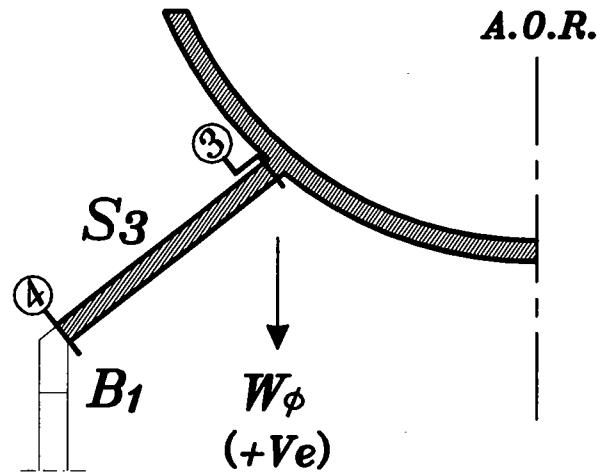
$$W_{\phi} (Sec. 3) = W_{\phi} (Sec. 1) + W_{\phi} (Sec. 2)$$



Sec. ④

Sec. ④ موجود في السطح S_3

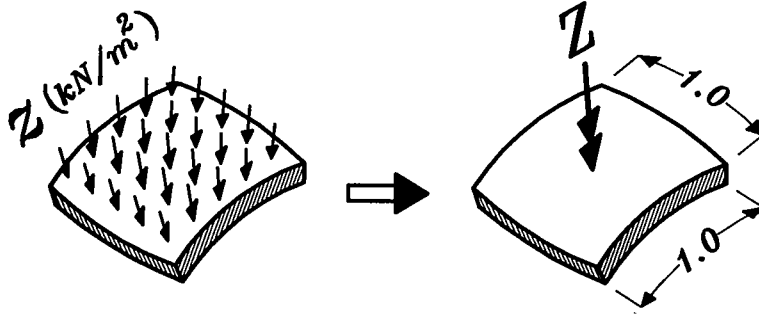
الكمرة B_1 هي ال support للسطح S_3



$$W_{\phi} (Sec. 4) = W_{\phi} (Sec. 3) + \text{Total Loads on Slab } S_3$$

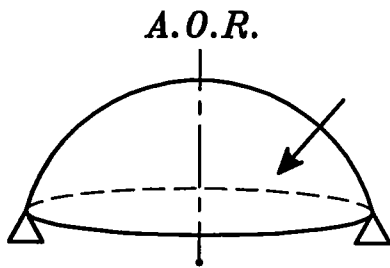
* Z

(Z) هي محصلة القوى الخارجيه العموديه على وحده المساحات من السطح .
و وحداتها (kN/m^2)



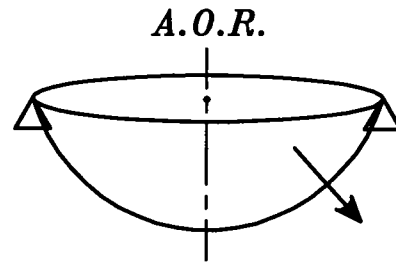
Dead Load	Live Load	Water Load
<p>$g (kN/m^2)$</p> <p>$Z = g * \cos \phi$</p>	<p>$P (kN/m^2)$</p> <p>$P * \cos \phi$</p> <p>$Z = P * \cos^2 \phi$</p>	<p>h</p> <p>ϕ</p> <p>$Z = \delta w * h$</p>
$Z = g * \cos \phi$	$Z = P * \cos^2 \phi$	$Z = \delta w * h$

Sign of Z



$Z (+Ve) \text{ Sign}$

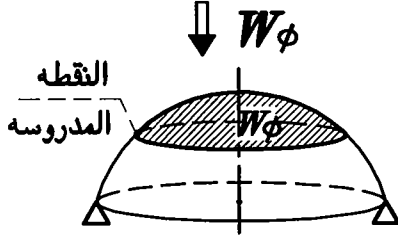
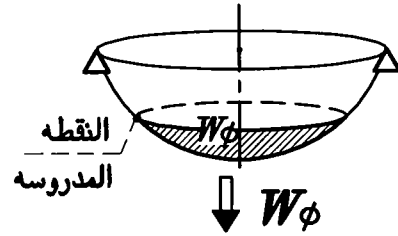
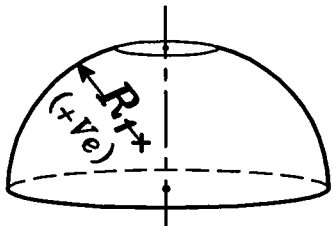
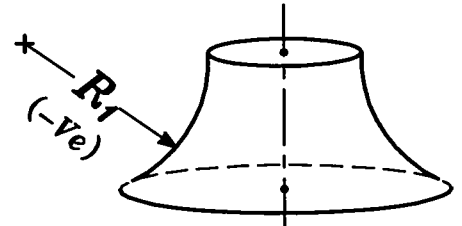
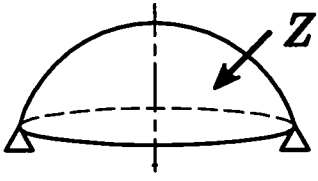
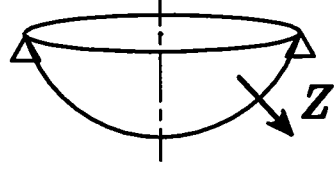
عندما تكون Z داخله
في اتجاه ال (A.O.R.)



$Z (-Ve) \text{ Sign}$

عندما تكون Z خارجه
بعيدا عن ال (A.O.R.)

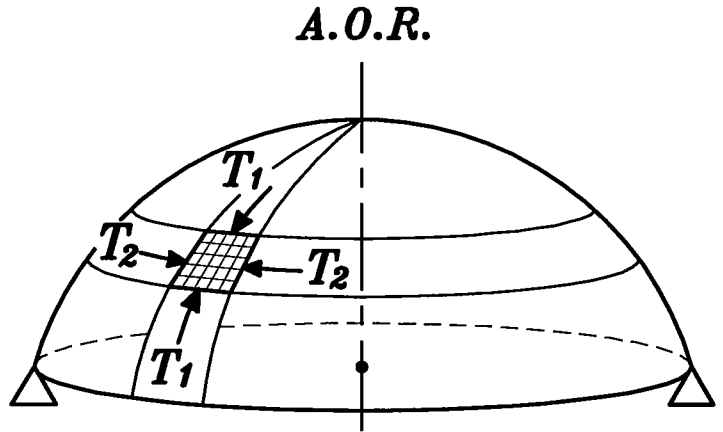
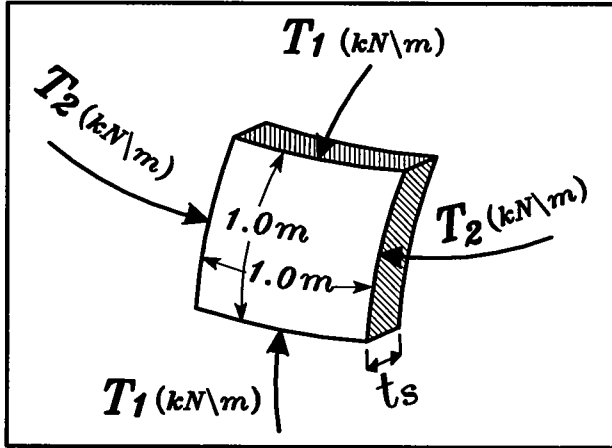
Parameter Signs.

Parameter	(+Ve) Sign	(-Ve) Sign
T_1	Compression Force	Tension Force
T_2	Compression Force	Tension Force
W_ϕ	 <p>W_ϕ داخله الى ال Support</p>	 <p>W_ϕ خارجه من ال Support</p>
r	دائماً (+Ve)	
ϕ	دائماً (+Ve)	
R_1	 <p>عندما تكون خارجه بعيدا عن ال (A.O.R.)</p>	 <p>عندما تكون داخله في اتجاه ال (A.O.R.)</p>
R_2	دائماً (+Ve)	
Z	 <p>عندما تكون Z داخله في اتجاه ال (A.O.R.)</p>	 <p>عندما تكون Z خارجه بعيدا عن ال (A.O.R.)</p>

Calculation of Internal Forces (T_1) & (T_2).

T_1 is Meridian Force. (kN/m)

T_2 is Ring Force. (kN/m)



$$T_1 = \frac{W_\phi}{2\pi r \sin\phi}$$

حفظ

اثبات القانون في صفحه 113

$$\frac{T_1}{R_1} + \frac{T_2}{R_2} = Z$$

حفظ

اثبات القانون في صفحه 114

ملحوظه هامه .

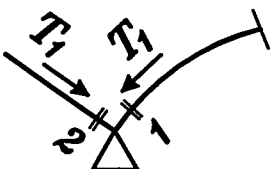
* تحديد اشاره (T_1) يعتمد على اشاره (W_ϕ) فقط

* تحديد اشاره (T_2) يعتمد على اشاره (T_1) و اشاره (R_1) و اشاره (Z)

$$\frac{\pm T_1}{\pm R_1} + \frac{T_2}{R_2} = \pm Z$$

في حاله وجود ركيزه تفصل بين سطحين يتم التعامل مع كل سطح على حده

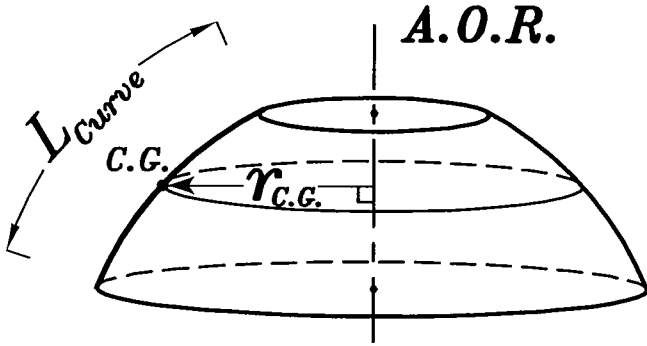
و لا يوجد بينهما أى أثر .



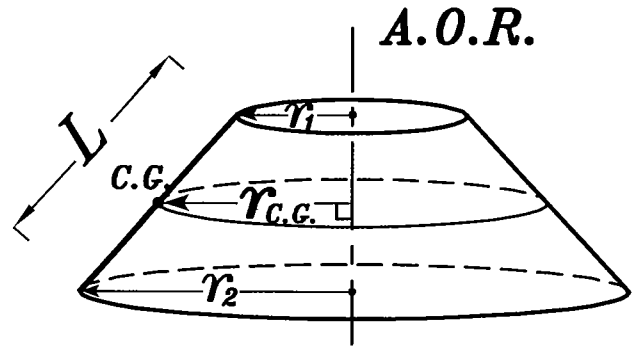
Sec. ① ل T_1, T_2 لا علاقه لها ب T_1, T_2 ل Sec. ②

Theory of Surface Areas of S.O.R.

مساحة السطح الناتجة من دوران خط أو منحنى حول محور
تساوى طول الخط أو المنحنى مضروباً في محيط الدائرة الناتجة عن
دوران نقطه مركز ثقل (C.G.) هذا الخط أو المنحنى حول نفس المحور.



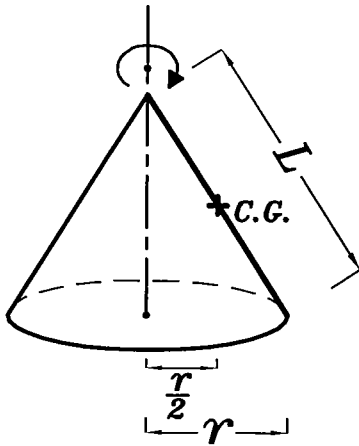
$$S.A. = L_{Curve} * 2\pi * r_{C.G.}$$



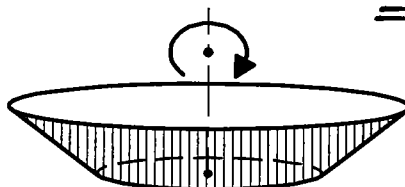
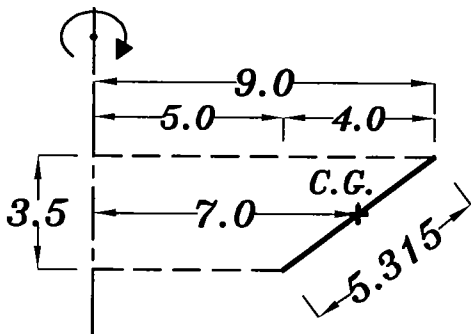
$$r_{C.G.} = \frac{r_1 + r_2}{2}$$

$$S.A. = L * 2\pi * r_{C.G.}$$

Example.



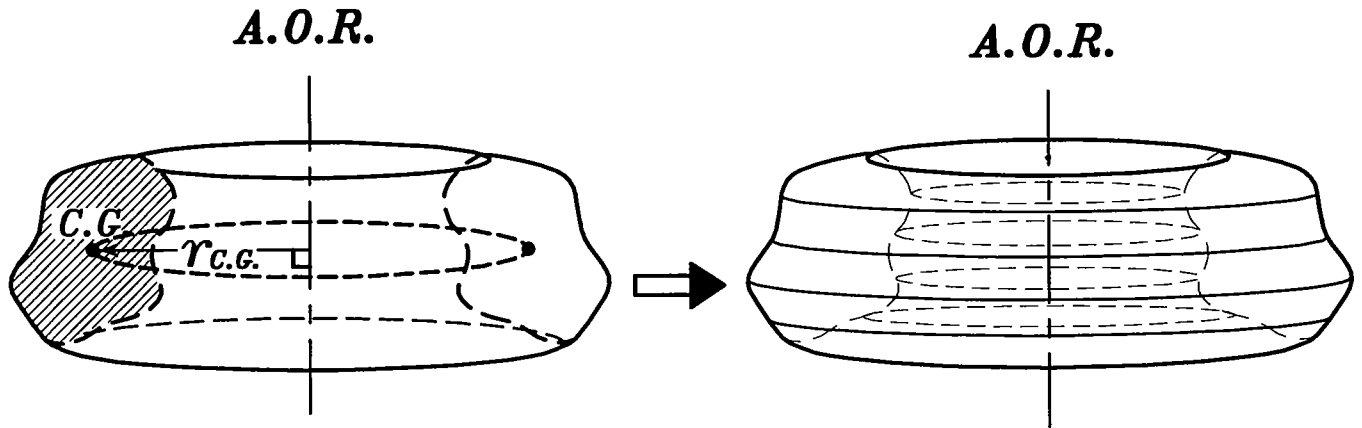
$$\begin{aligned} S.A. &= L * 2\pi * r_{C.G.} \\ &= L * 2\pi * \frac{r}{2} = \pi * r * L \end{aligned}$$



$$\begin{aligned} S.A. &= L * 2\pi * r_{C.G.} \\ &= 5.315 * 2\pi * 7.0 \\ &= 233.76 \text{ m}^2 \end{aligned}$$

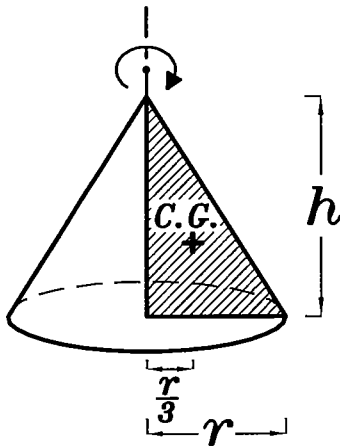
Theory of Volumes of S.O.R.

الحجم الناتج من دوران مساحة حول محور تساوى قيمه هذه المساحة مضروبا فى محيط الدائره الناتجه عن دوران نقطه مركز ثقل (C.G.) هذه المساحة حول نفس المحور .



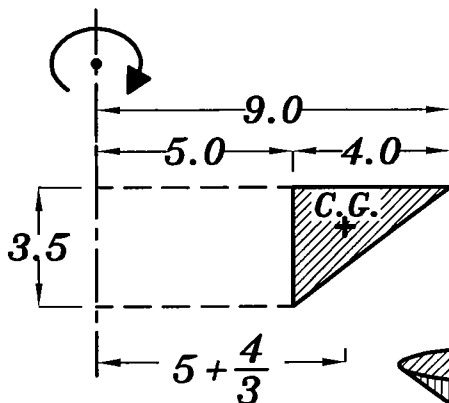
$$\text{Volume} = \text{Area} * 2\pi * r_{c.g.}$$

Example.



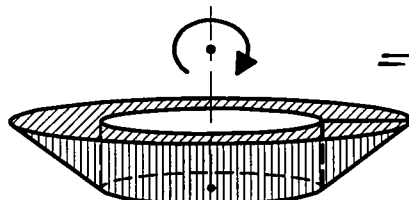
$$\text{Volume} = \text{Area} * 2\pi * r_{c.g.}$$

$$\begin{aligned} &= \left(\frac{1}{2} * r * h\right) * 2\pi * \frac{r}{3} \\ &= \frac{\pi * r^2 * h}{3} \end{aligned}$$



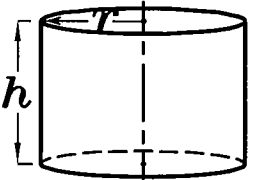
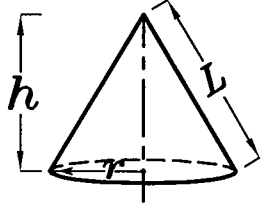
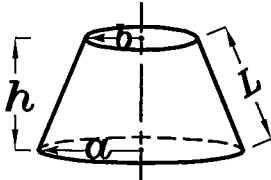
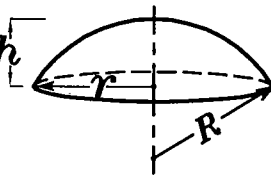
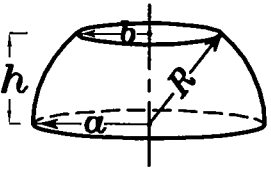
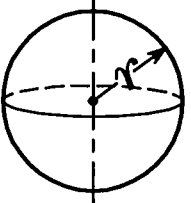
$$\text{Volume} = \text{Area} * 2\pi * r_{c.g.}$$

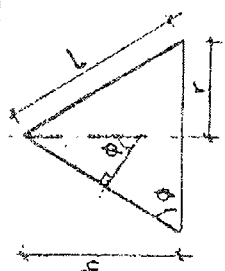
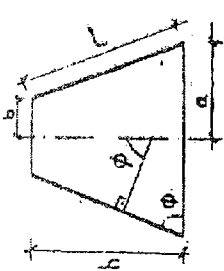
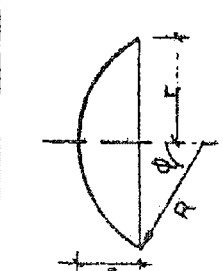
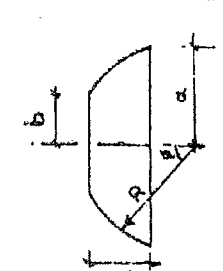
$$\begin{aligned} &= \left(\frac{1}{2} * 3.5 * 4\right) * 2\pi * \left(5 + \frac{4}{3}\right) \\ &= 278.55 \text{ m}^3 \end{aligned}$$

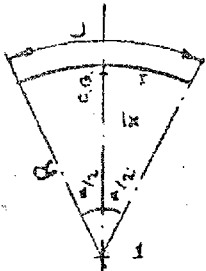
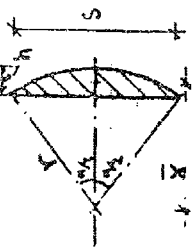
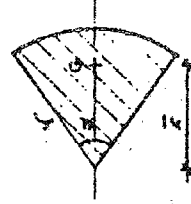


Volume and Surface Areas For some shapes.
Old tables Page 121

حفظ للأسف

Name	Shape	Surface Area	Volume
Cylinder		$S.A. = 2 \pi r * h$	$V = \pi r^2 * h$
Cone		$S.A. = \pi * L * r$	$V = \frac{1}{3} * \pi * r^2 * h$
Part Of Cone		$S.A. = \pi * L (a+b)$	$V = \frac{\pi h}{3} (a^2 + b^2 + ab)$
Dome		$S.A. = 2 \pi * R * h$	$V = \pi * h^2 (R - \frac{h}{3})$
Part Of Dome		$S.A. = 2 \pi * R * h$	$V = \frac{\pi h}{6} (3a^2 + 3b^2 + h^2)$
Sphere		$S.A. = 4 * \pi * r^2$	$V = \frac{4}{3} * \pi * r^3$

Solid Bodies		
Shape	Volume	Surface Area
	<p>CONE</p> $\pi r^2 h / 3$	$\pi r l$
	<p>PART OF CONE</p> $\frac{\pi h (a^2 + b^2 + ab)}{3}$	$\pi l (a + b)$
	<p>DOME</p> $\frac{\pi h^2 (R - h/3)}{\pi h (3R^2 + h^2)/6}$	$2 \pi R h = \pi (r^2 + h^2)$
	<p>PART OF DOME</p> $\frac{\pi h (3a^2 + 3b^2 + h^2)}{6}$	$2 \pi R h$

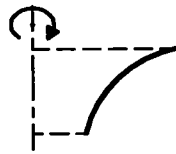
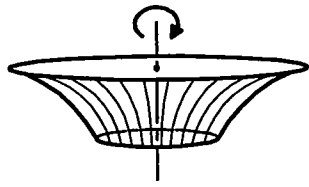
Arc of a Circle		
	$\bar{x} = R \sin(a/2) / (a/2)$ $L = r \cdot a$	
Segment and Sector of a Circle		
Shape	Area	C.G. (\bar{x})
	$r^2 a/2$ $- s(r-h)/2$	$s^3 / (12 A)$
	$r^2 a / 2$	$\frac{2 r \sin (a/2)}{(3a/2)}$

For Surfaces of Revolution :

* Meridian Force = T_1
 $T_1 = W \phi / 2 \pi r \sin(\phi)$

* Ring Force = T_2
 $T_1/R_1 + T_2/R_2 = Z$

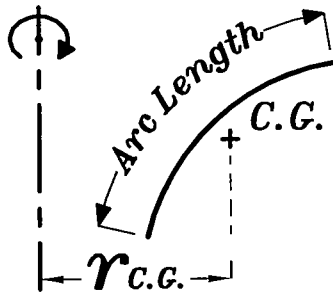
Special Cases.



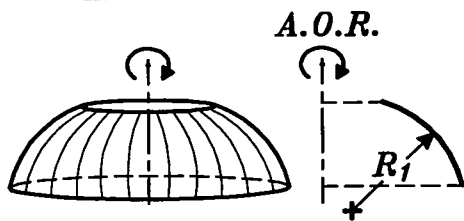
إذا كان المنحنى للخارج (كما بالشكل)

فانه يجب لحساب ال Surface Area استخدام القانون :

A.O.R.



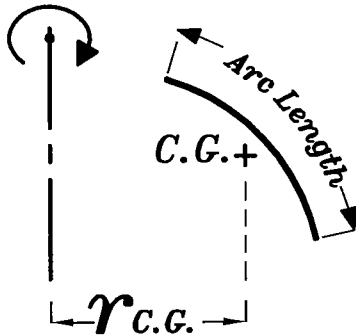
$$S.A. = \text{Arc Length} * 2\pi * r_{C.G.}$$



A.O.R.

إذا كان المنحنى للداخل لكن مركزه ليس على ال A.O.R.

فانه يجب لحساب ال Surface Area استخدام القانون :



$$S.A. = \text{Arc Length} * 2\pi * r_{C.G.}$$

Radian

$$\text{Arc Length} = 2 * R * \theta$$

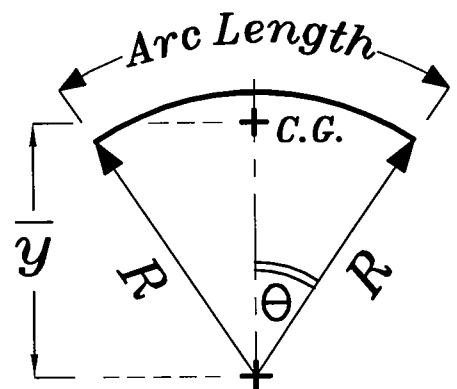
$$\bar{y} = \frac{R * \sin \theta}{\theta}$$

Radian

where: θ is the Central Angle.

R is the Radius of the Arc.

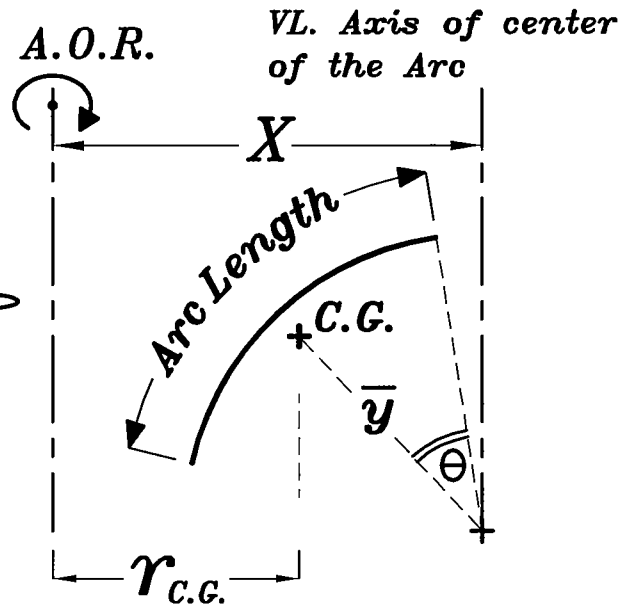
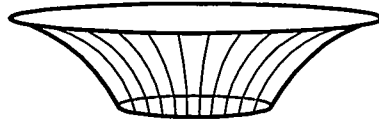
لاى قوس فى دائره .



$$S.A. = \text{Arc Length} * 2\pi * r_{c.g.}$$

$$\text{Arc Length} = 2 * R * \theta$$

$$\bar{y} = \frac{R * \sin \theta}{\theta}$$



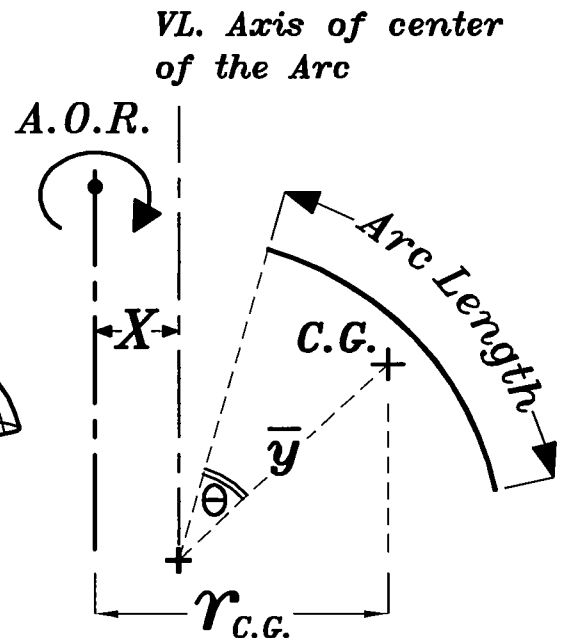
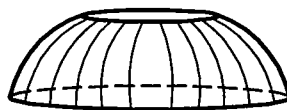
X is the H.L. distance between the Axis of Revolution and the V.L. Axis of center of the Arc.

المنحنى للداخل لكن مركزه ليس على ال A.O.R.

$$S.A. = \text{Arc Length} * 2\pi * r_{c.g.}$$

$$\text{Arc Length} = 2 * R * \theta$$

$$\bar{y} = \frac{R * \sin \theta}{\theta}$$



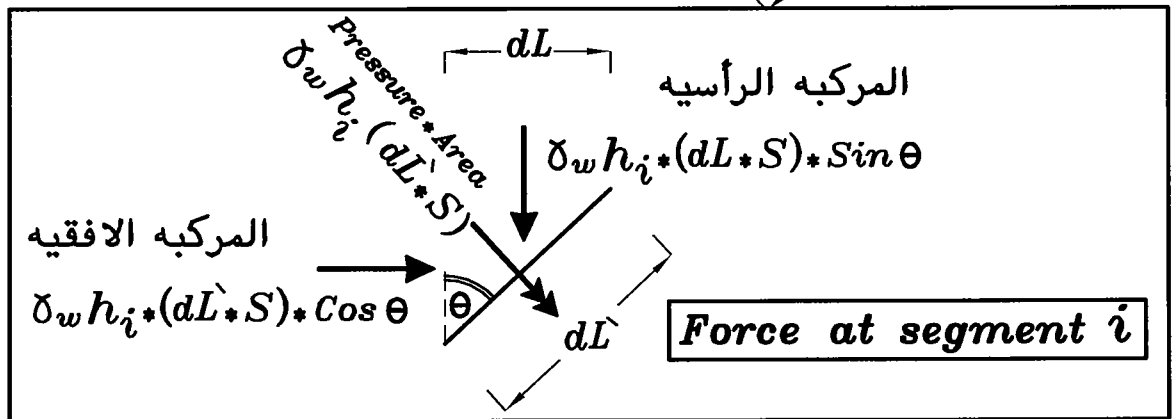
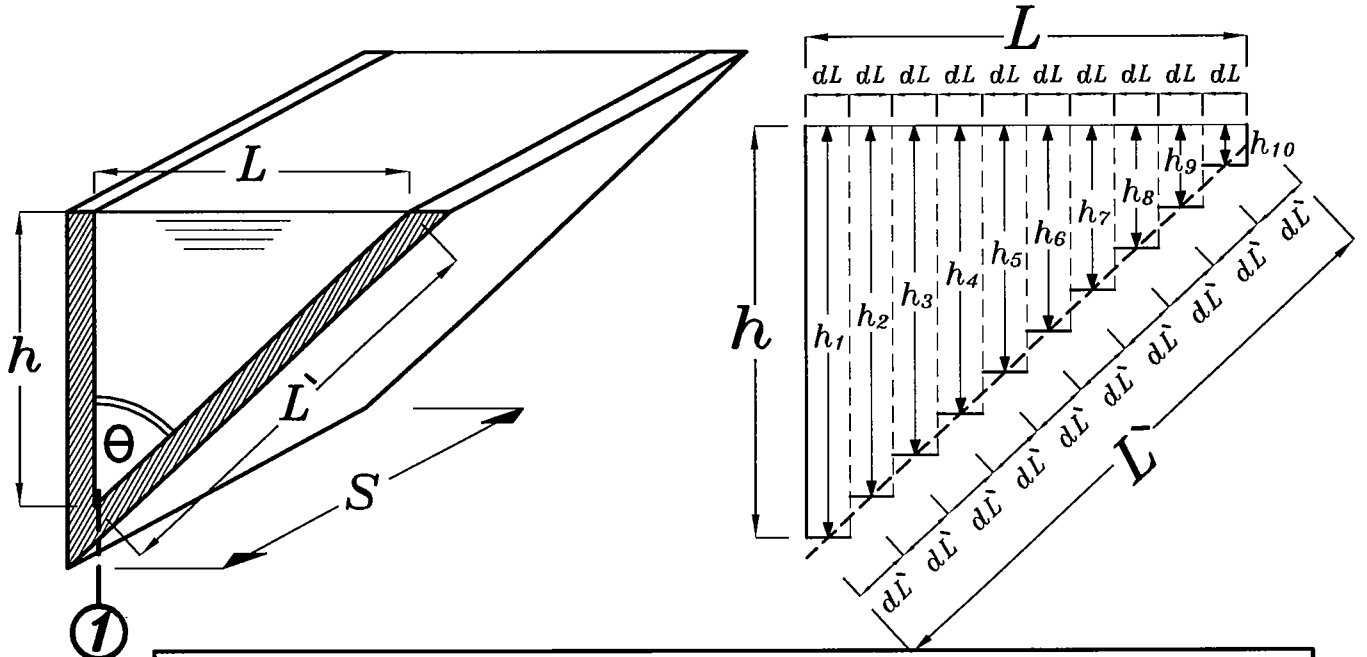
X is the H.L. distance between the Axis of Revolution and the V.L. Axis of center of the Arc.

سيتم شرح هذا الجزء بالتفصيل و الامثلة لاحقاً

Water pressure effect.

إذا كان السطح مائل للخارج أى ان الماء تضغط على السطح العلوى .

Calculate W_ϕ For section ① due to water pressure only.



محصله قوى الضغط العموديه على السطح فى طول dL

$$Pressure * Area = \delta_w h_i * (dL * S) \quad \downarrow \text{اتجاهها لاسفل}$$

المركبة الرأسية لقوى الضغط فى طول dL للجزء i \downarrow اتجاهها لاسفل

$$= \delta_w h_i * (dL * S) * \sin \theta = \delta_w h_i * (dL * S) * \frac{dL}{dL} = \delta_w h_i * (dL * S)$$

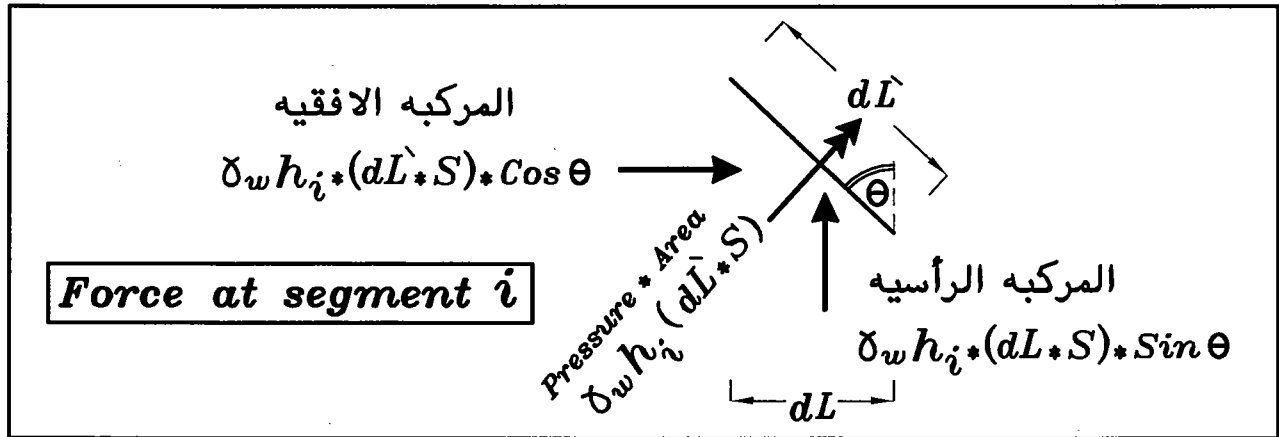
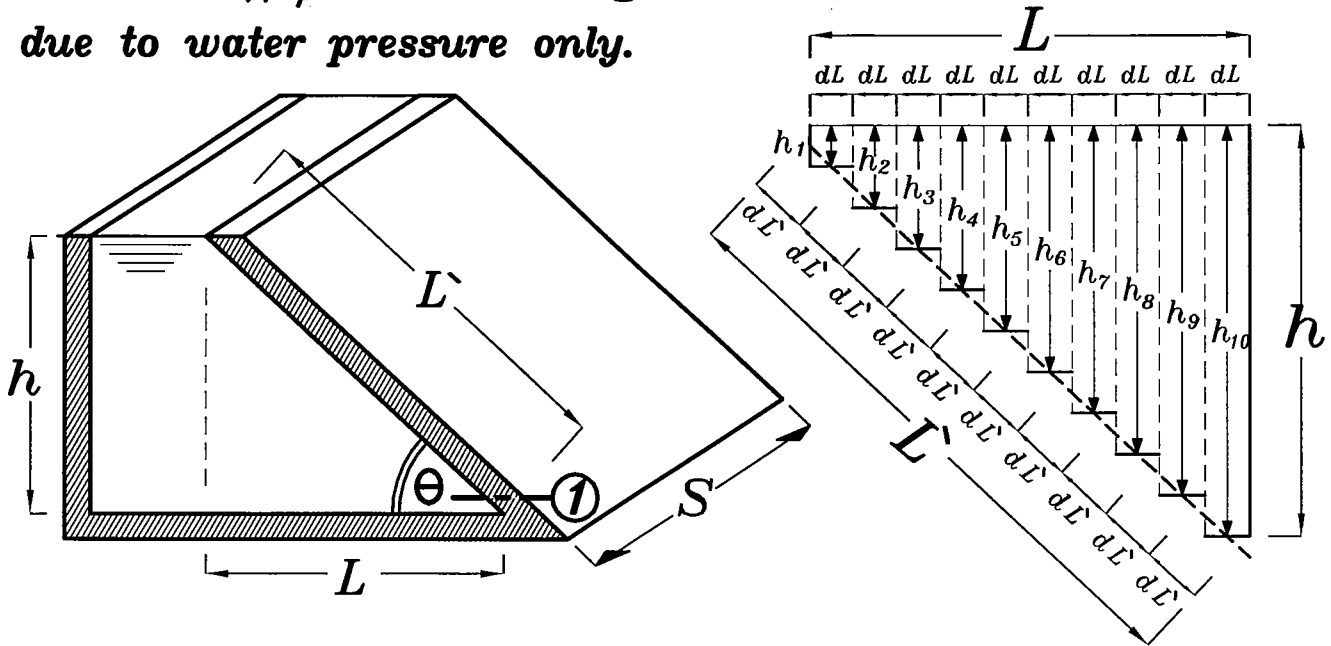
محصله المركبة الرأسية لقوى الضغط فى طول L \downarrow اتجاهها لاسفل $W_\phi =$

$$W_\phi = \delta_w * (\sum h_i * dL) * S = \delta_w * \sum Area * S = \delta_w * Water Volume$$

$$W_\phi = \delta_w * Volume of water above the surface. \downarrow$$

إذا كان السطح مائل للداخل أى ان الماء تضغط على السطح السفلى .

Calculate W_ϕ For section ①
due to water pressure only.



محصله قوى الضغط العموديه على السطح فى طول dL

$$\text{Pressure} * \text{Area} = \delta_w h_i * (dL * S) \quad \boxed{\text{اتجاهه لافى}}$$

المركبة الرأسية لقوى الضغط فى طول dL للجزء i = $\boxed{\text{اتجاهه لافى}}$

$$= \delta_w h_i * (dL * S) * \sin \theta = \delta_w h_i * (dL * S) * \frac{dL}{dL} = \delta_w h_i * (dL * S)$$

محصله المركبة الرأسية لقوى الضغط فى طول L = $\boxed{\text{اتجاهه لافى}}$ W_ϕ

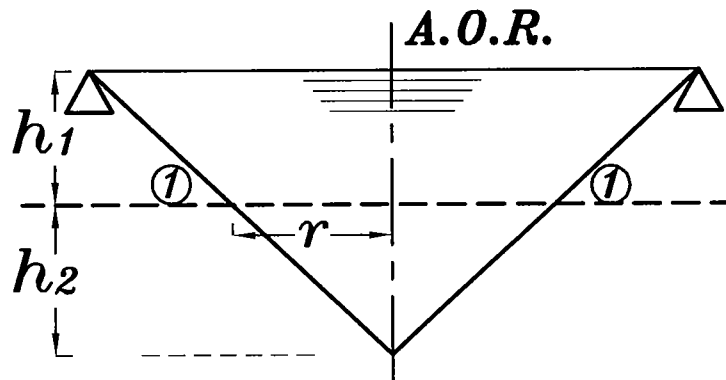
$$W_\phi = \delta_w * (\sum h_i * dL) * S = \delta_w * \sum \text{Area} * S = \delta_w * \text{Water Volume}$$

$$\boxed{W_\phi = \delta_w * \text{Virtual Volume of water above the surface.} \uparrow}$$

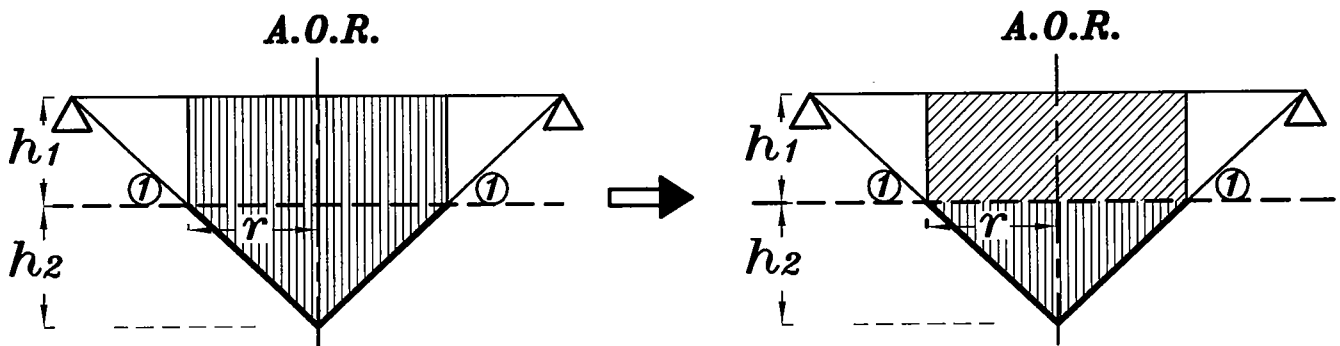
يساوى الحجم الوهمى للماء فوق السطح مباشره حتى منسوب سطح الماء .

Example.

Calculate (W_ϕ & Z) For section ① due to water pressure only.



W_ϕ عند Sec. ① سيكون ضغط الماء بعيدا عن ال support كله لاسفل .



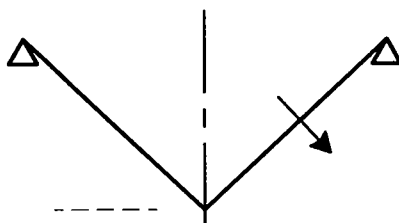
$$W_\phi = \gamma_w * \left[\text{Volume of } \begin{array}{c} \text{cylinder of height } h_1 \\ \text{and cone of height } h_2 \end{array} \right]$$

$$\therefore W_\phi = \gamma_w * \left[\text{Volume of } \begin{array}{c} \text{cylinder of height } h_1 \\ \text{and cone of height } h_2 \end{array} \right]$$

$$\gamma_w = 10 \text{ kN/m}^3$$

اشاره W_ϕ (-ve) لان اتجاها خارج من ال support

Z

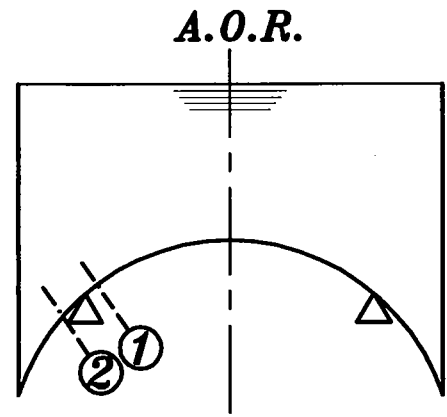


$$Z = \gamma_w * h_1 \text{ عند Sec. ①}$$

اشاره Z (-ve) لان اتجاها خارج من المحور

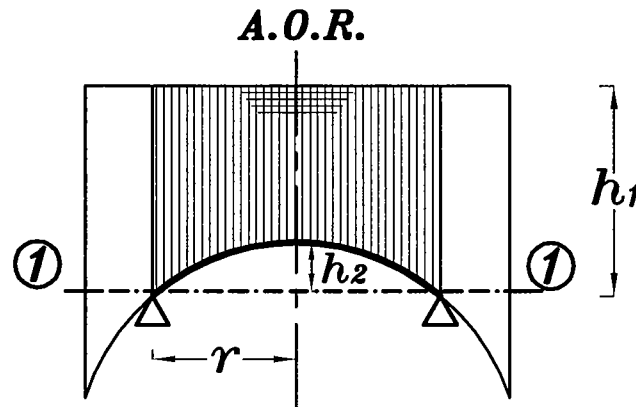
Example.

Calculate (W_ϕ & Z) For sections ①, ② due to water pressure only.



Sec. ①

عند Sec. ① أعلى ال support سيكون ضغط الماء بعيدا عن ال support كله لاسفل .



$$W_\phi = \gamma_w * \left[\text{Volume of } \downarrow \right]$$

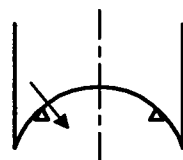
$$W_\phi = \gamma_w * \left[\text{Volume of } h_1 - h_2 \right]$$

$$\gamma_w = 10 \text{ kN/m}^3$$

اشاره W_ϕ (+Ve) لان اتجاهها داخل الى ال support

اشاره Z (+Ve)

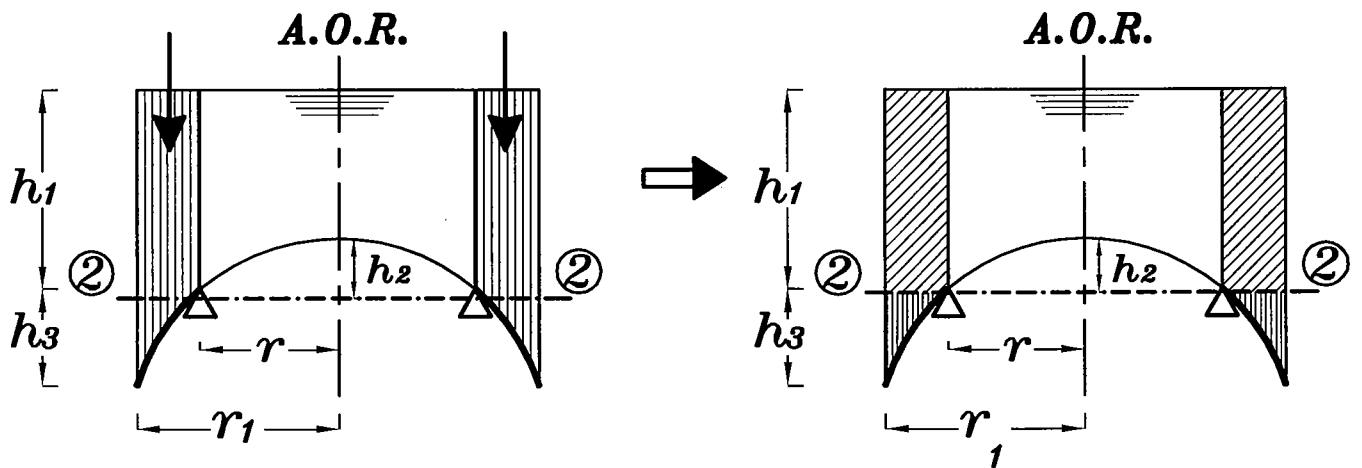
لان اتجاهها داخل الى المحور



$$Z = \gamma_w * h_1 \text{ عند Sec. ①}$$

Sec. ②

عند ② أسفل ال support
سيكون ضغط الماء بعيدا عن ال support كله لأسفل .



$$W_{\phi} = \delta_w * \left[\text{Volume of } \begin{array}{c} h_1 \\ h_3 \end{array} \right]$$

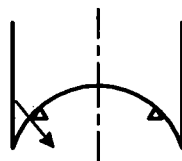
$$W_{\phi} = \delta_w * \left[\text{Volume of } \begin{array}{c} h_1 \\ h_3 \end{array} \right] + \begin{array}{c} h_1 \\ h_3 \end{array}$$

$$\delta_w = 10 \text{ kN/m}^3$$

اشاره W_{ϕ} (-Ve) لان اتجاها خارج من ال Support

اشاره Z (+Ve)

لان اتجاها داخل الى المحور



$$Z = \delta_w * h_1 \quad \text{عند ② Sec. ②}$$

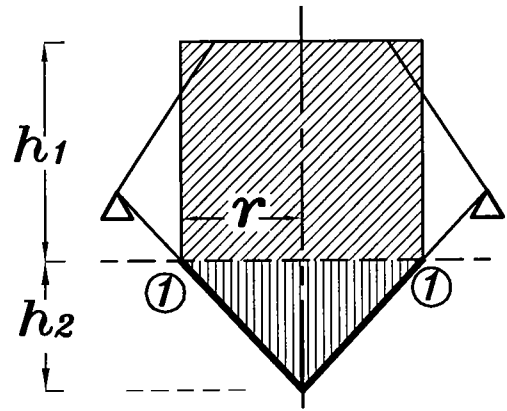
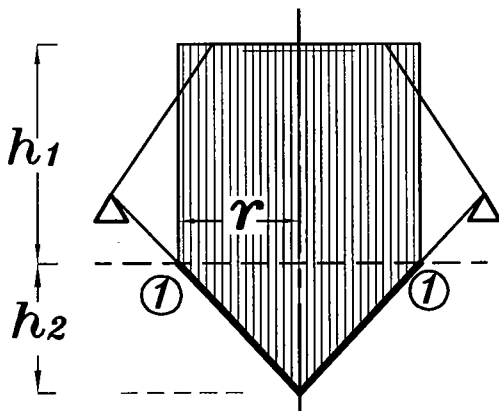
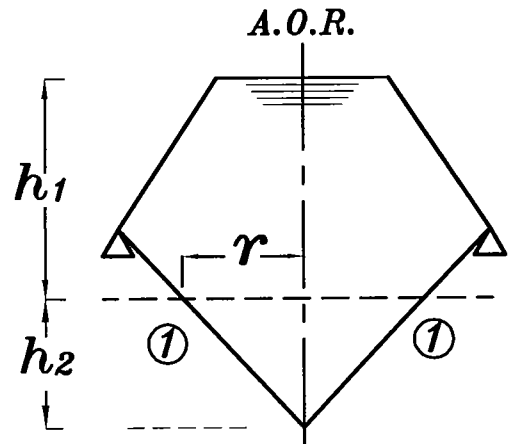
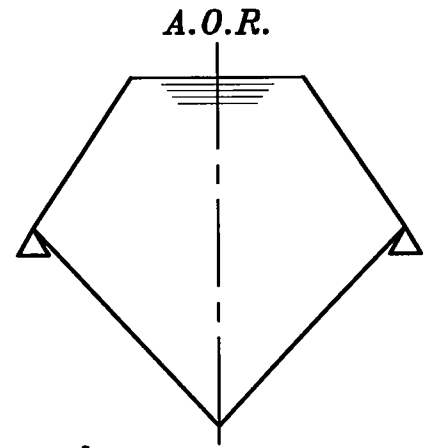
Example.

Calculate (W_ϕ & Z) For sections above & under the supports due to water pressure only.

1—For section under the support.

W_ϕ

عند ① سيكون ضغط الماء بعيدا عن ال support كله لاسفل .



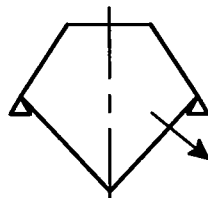
$$\therefore W_\phi = \gamma_w * \left[\text{Volume of } h_1 \text{ cylinder} + h_2 \text{ cone} \right]$$

$$\gamma_w = 10 \text{ kN/m}^3$$

اشاره W_ϕ (-Ve) لان اتجاها خارج من ال support

اشاره Z (-Ve)

لان اتجاها خارج من المحور



$$Z = \gamma_w * h_1 \text{ عند ①}$$

2- For section above the support.

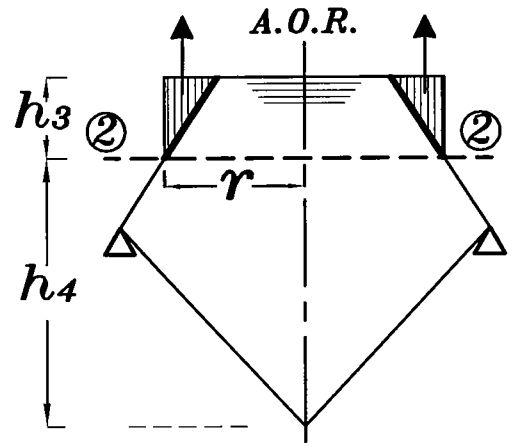
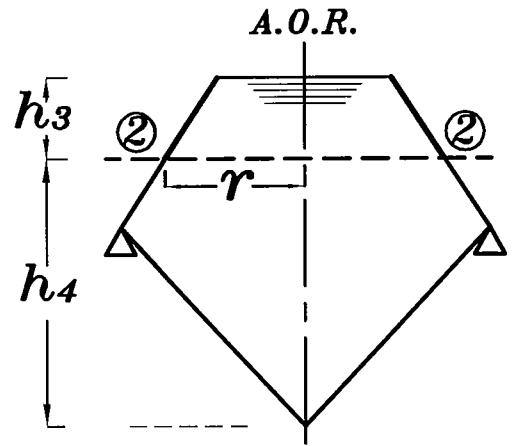
W_ϕ

عند ② سيكون ضغط الماء بعيدا عن ال support كله لاعلى .

الحجم الوهمي للماء فوق السطح مباشرة حتى منسوب سطح الماء .

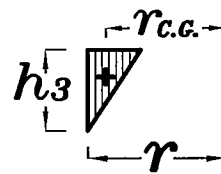
$$W_\phi = \delta_w * \text{Volume of } \begin{array}{c} \text{cylinder} \\ \text{radius } r \\ \text{height } h_3 \end{array}$$

اشاره W_ϕ (-ve) لان اتجاها خارج من ال support



لحساب حجم h_3 توجد طريقتين :

$$\text{Volume} = \text{Area} * 2\pi * r_{c.g.}$$



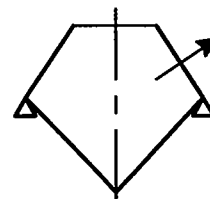
اما بطريقه

$$\left[\text{Volume of } h_3 \left[\begin{array}{c} \text{cylinder} \\ \text{radius } r \end{array} \right] - h_3 \left[\begin{array}{c} \text{trapezoid} \\ \text{radius } r \end{array} \right] \right] \text{ او بطرح حجم اسطوانه - مخروط ناقص}$$

Z

$$Z = \delta_w * h_1 \text{ عند ②}$$

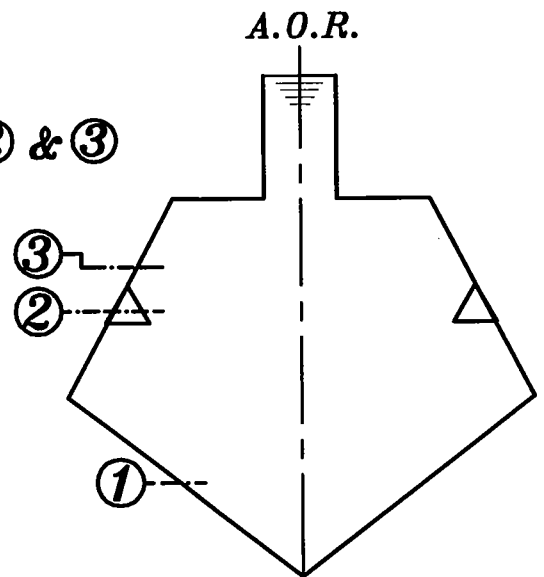
اشاره Z (-ve) لان اتجاها خارج من المحور



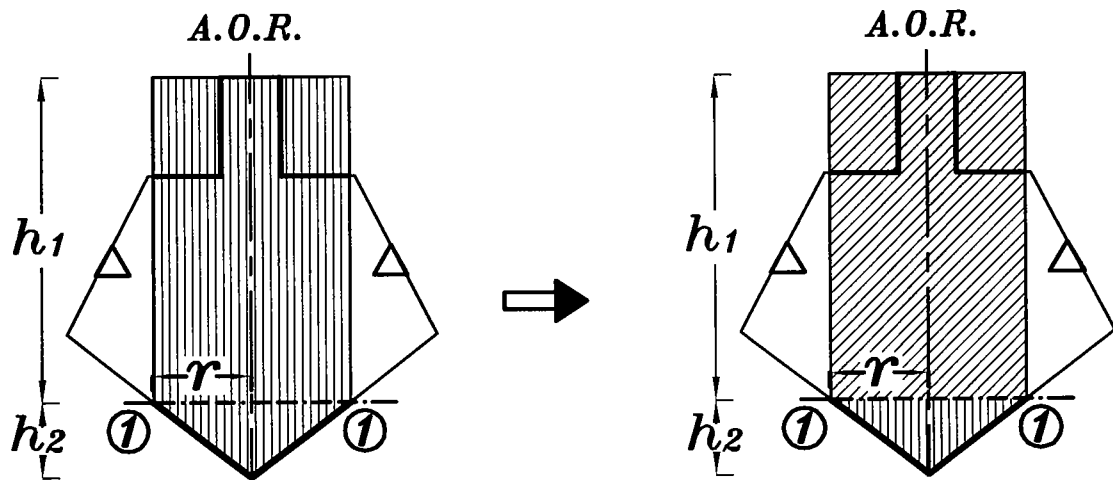
Example.

Calculate (W_ϕ & Z) For sections ①, ② & ③ due to water pressure only.

Sec. ①



عند Sec. ① سيكون ضغط الماء بعيدا عن ال support كله لأسفل .



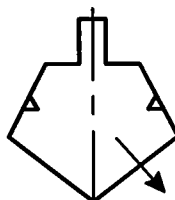
$$\therefore W_\phi = \gamma_w * \left[\text{Volume of } h_1 \text{ cylinder} \downarrow + h_2 \text{ cone} \downarrow \right]$$

$$\gamma_w = 10 \text{ kN/m}^3$$

اشاره W_ϕ (-ve) لان اتجاها خارج من ال Support

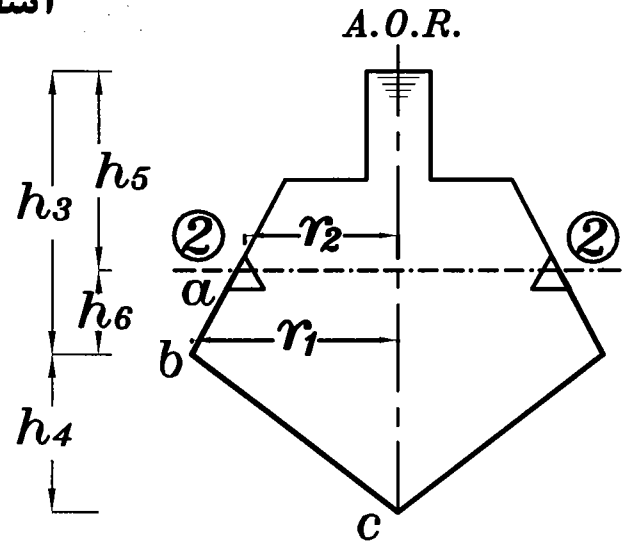
اشاره Z (-ve)

لان اتجاها خارج من المحور

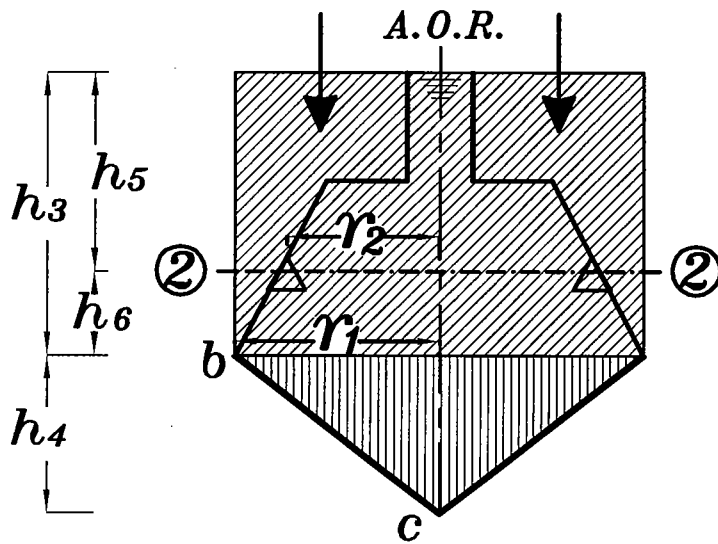


$$Z = \gamma_w * h_1 \quad \text{عند Sec. ①}$$

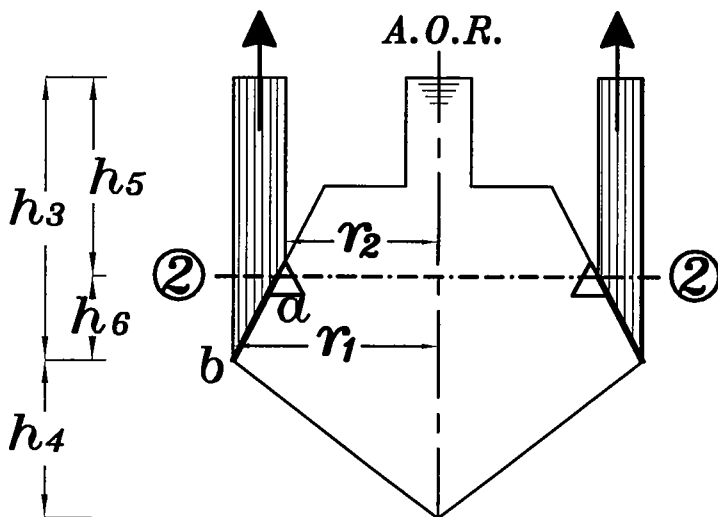
أسفل ال support ② Sec. ②



عند ② Sec. ② سيكون ضغط الماء بعيدا عن ال support لأسفل عند السطح $b\ c$
و سيكون لأعلى عند السطح $b\ a$

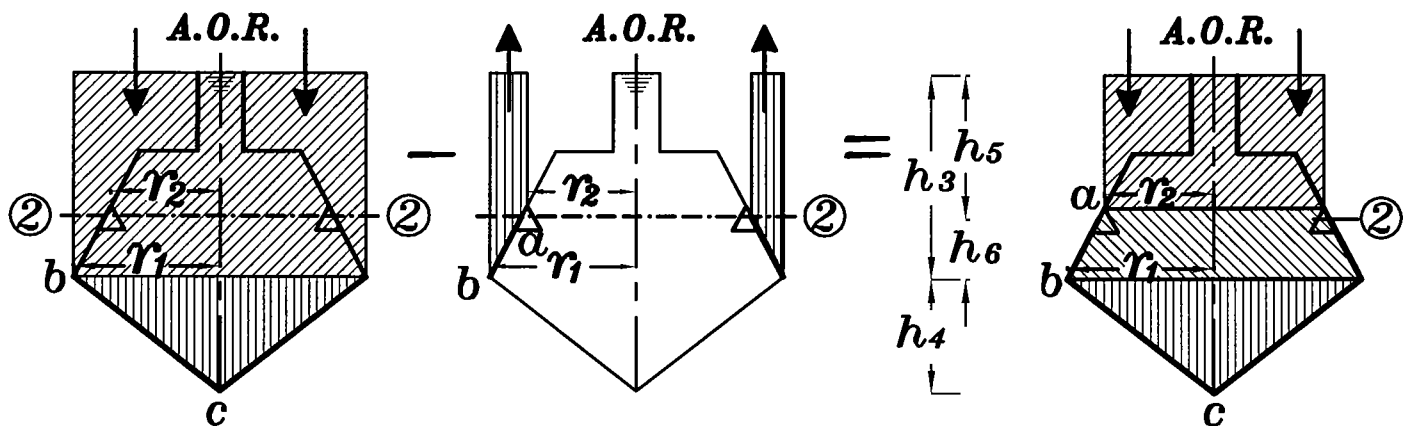


سيكون ضغط الماء لأسفل
عند السطح $b\ c$



سيكون ضغط الماء لأعلى
عند السطح $b\ a$

محصله ضغط المياه عند ② بعيدا عن ال support ستكون لأسفل
ستكون ضغط المياه على السطح $b c$ لأسفل مطروحا منه ضغط المياه على السطح $a b$ لا على



$$W_{\phi} = \gamma_w * \left[\text{Volume of } \begin{array}{c} \text{Cylinder of height } h_5 \text{ and radius } r_2 \\ \text{Frustum of height } h_6 \text{ with radii } r_2 \text{ and } r_1 \\ \text{Cone of height } h_4 \text{ and radius } r_1 \end{array} \right]$$

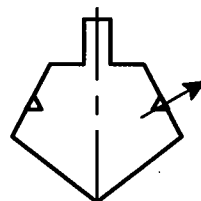
$$W_{\phi} = \gamma_w * \left[\text{Volume of } \begin{array}{c} \text{Cylinder of height } h_5 \text{ and radius } r_2 \\ \text{Frustum of height } h_6 \text{ with radii } r_2 \text{ and } r_1 \\ \text{Cone of height } h_4 \text{ and radius } r_1 \end{array} \right]$$

$$\gamma_w = 10 \text{ kN/m}^3$$

اشاره W_{ϕ} $(-Ve)$ لان اتجاها خارج من ال Support

اشاره Z $(-Ve)$

لان اتجاها خارج من المحور

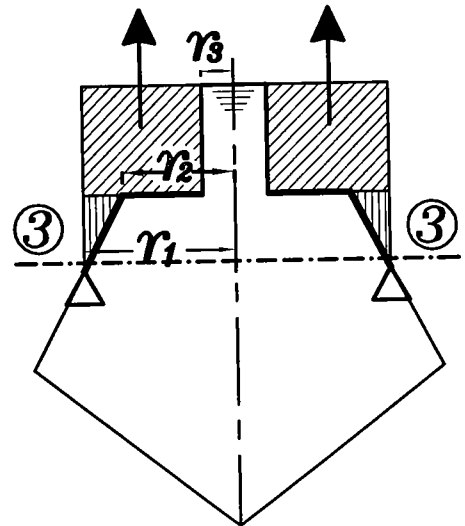
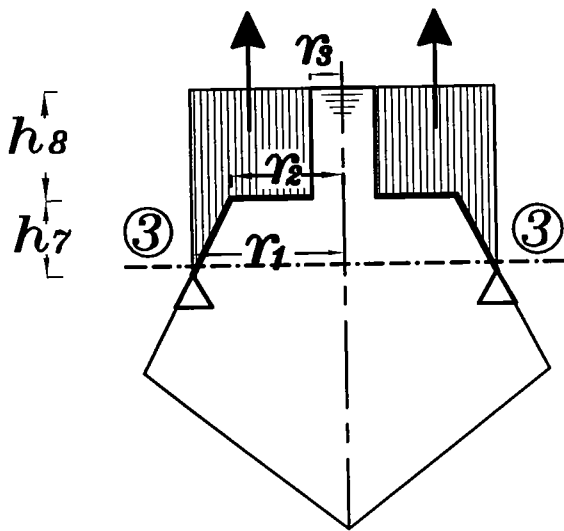
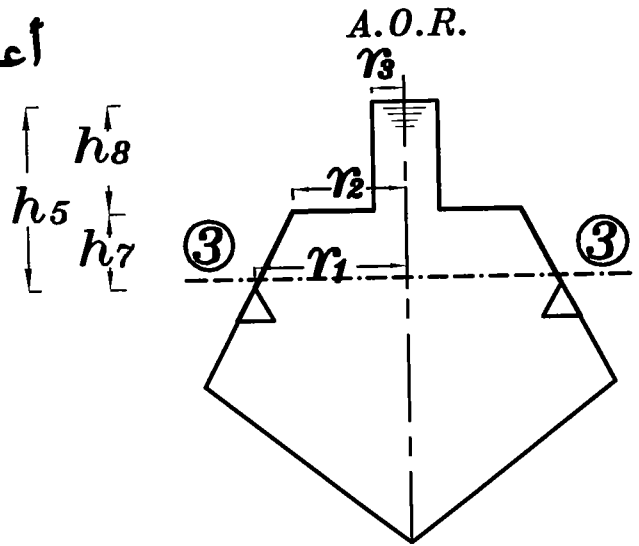


$$Z = \gamma_w * h_5$$

عند ② Sec.

أعلى ال support ③ Sec. ③

عند ③ Sec. سيكون ضغط الماء بعيدا عن ال support كله لاعلى .



$$W_{\phi} = \delta_w * \left[\text{Volume of } \begin{array}{c} h_8 \\ h_7 \end{array} \begin{array}{c} r_3 \\ r_2 \\ r_1 \end{array} \uparrow \right]$$

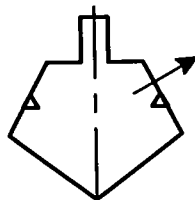
$$W_{\phi} = \delta_w * \left[\text{Volume of } \begin{array}{c} h_8 \\ h_7 \end{array} \begin{array}{c} r_3 \\ r_2 \\ r_1 \end{array} \uparrow + \begin{array}{c} h_8 \\ h_7 \end{array} \begin{array}{c} r_2 \\ r_1 \end{array} \uparrow \right]$$

$$\delta_w = 10 \text{ kN/m}^3$$

اشاره $W_{\phi} (-ve)$ لان اتجاها خارج من ال Support

اشاره $Z (-ve)$

لان اتجاها خارج من المحور

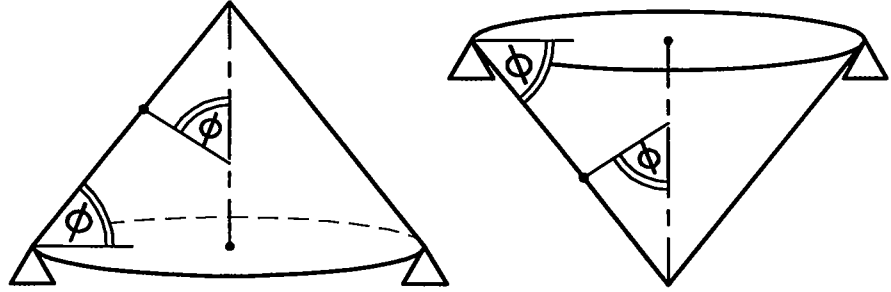


$$Z = \delta_w * h_5 \text{ عند } ③ \text{ Sec.}$$

Properties of Important Surfaces.

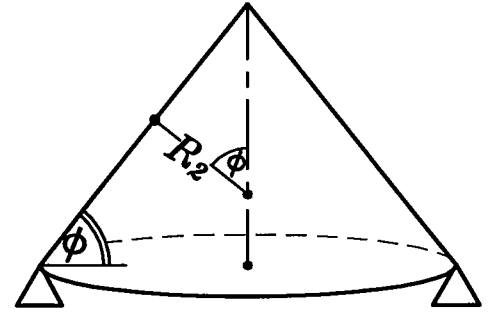
Cone.

ϕ هي زاويه ميل السطح مباشره مع الافقى .



$$\boxed{R_1 = \infty} \quad \therefore \frac{T_1}{R_1} + \frac{T_2}{R_2} = Z$$

$$\therefore \text{Zero} + \frac{T_2}{R_2} = Z$$

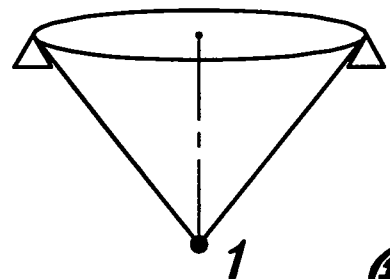
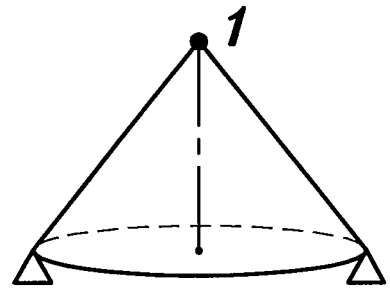


$$\boxed{T_2 = R_2 Z} \quad \text{حفظ}$$

At Cone Vertex Point ①

$$\boxed{T_1 = T_2 = \text{Zero}} \quad \text{حفظ}$$

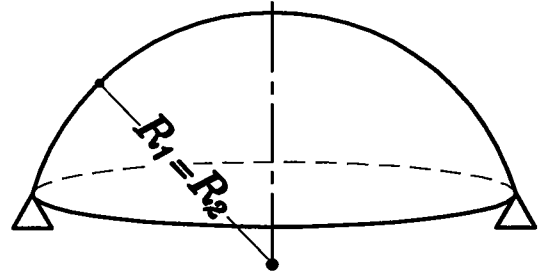
اثباته في صفحه 110



Dome.

$$R_1 = R_2 = R$$

$$\therefore \frac{T_1}{R_1} + \frac{T_2}{R_2} = Z \quad \therefore \frac{T_1 + T_2}{R} = Z$$

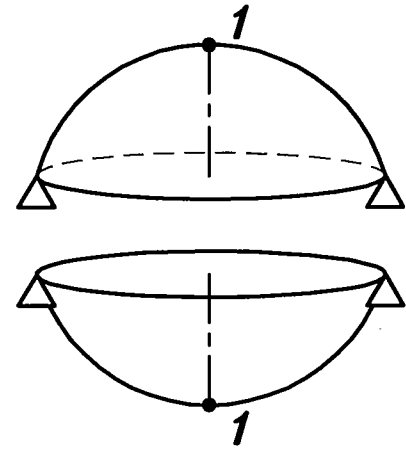


$$T_1 + T_2 = RZ \quad \text{حفظ}$$

At Dome Vertex Point ①

$$T_1 = T_2 = \frac{RZ}{2} \quad \text{حفظ}$$

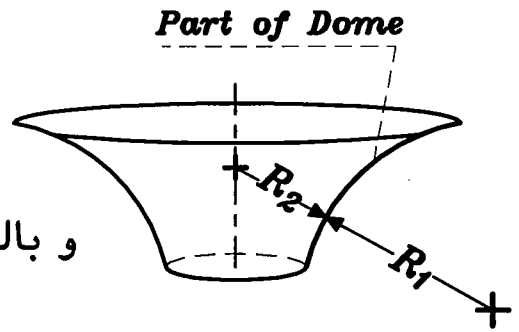
اثباته في صفحه 111



Special Case.

إذا كان المنحنى للخارج ستكون $R_1 \neq R_2$

و بالتالي معادله $T_1 + T_2 = RZ$ لن تكون صحيحة

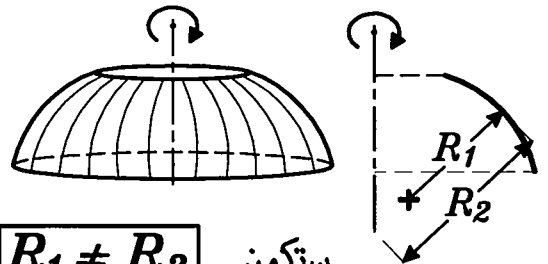


و سنضطر لاستخدام المعادله الاصليه $\frac{T_1}{R_1} + \frac{T_2}{R_2} = Z$

Special Case.

إذا كان المنحنى للداخل لكن مركزه ليس على ال A.O.R.

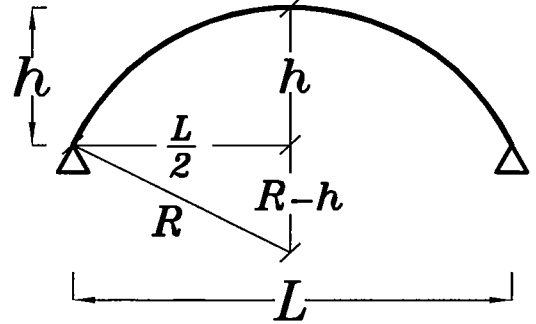
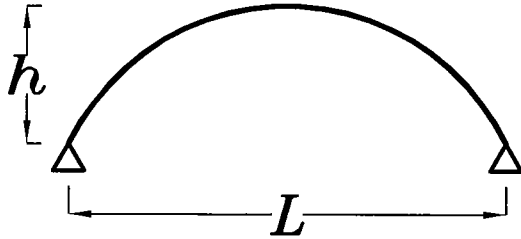
ستكون $R_1 \neq R_2$ و بالتالي معادله $T_1 + T_2 = RZ$ لن تكون صحيحة .



و سنضطر لاستخدام المعادله الاصليه $\frac{T_1}{R_1} + \frac{T_2}{R_2} = Z$

Calculations of Dome Radius.

من الممكن ان يكون معطى لا *Dome* عرض قاعدتها و ارتفاعها .
و بالطبع سنحتاج ان نحدد نصف قطرها لتكملة حسابات المسألة .



$$R^2 = \left(\frac{L}{2}\right)^2 + (R-h)^2$$

$$R^2 = \frac{L^2}{4} + R^2 - 2Rh + h^2$$

$$R = \frac{L^2/4 + h^2}{2h}$$

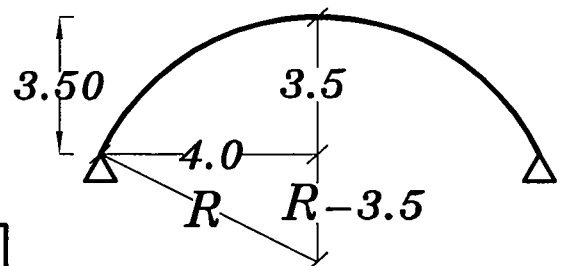
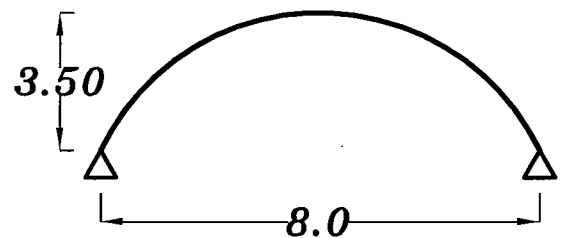
Example.

*Fined the radius
For the given Dome.*

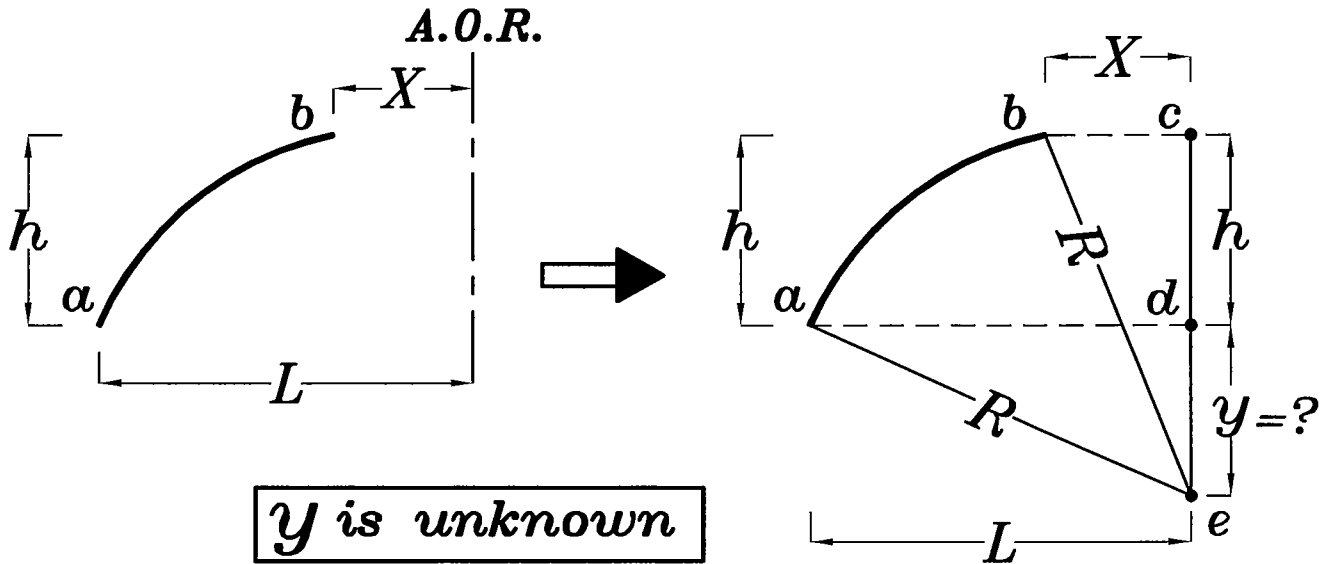
$$R^2 = 4.0^2 + (R-3.5)^2$$

$$R^2 = 16 + R^2 - 7.0R + 12.25$$

$$7.0R = 28.25 \longrightarrow \boxed{R = 4.03\text{ m}}$$



إذا كان معطى جزء من ال *Dome* و لا توجد *Vertex*
و معطى فقط ارتفاع هذا الجزء و عرضه و بعده الافقى عن المحور .
و بالطبع سنحتاج ان نحدد نصف قطرها لتكملة حسابات المسألة .



For Triangle a d e

$$R^2 = L^2 + y^2 \quad \text{---} R, y \text{---} \textcircled{1}$$

For Triangle e c b

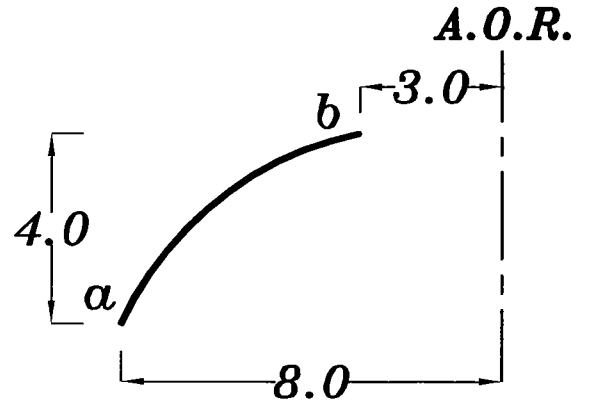
$$R^2 = X^2 + (y+h)^2 = X^2 + y^2 + 2yh + h^2$$

$$R^2 = X^2 + y^2 + 2yh + h^2 \quad \text{---} R, y \text{---} \textcircled{2}$$

Solve the Two equations and Get y, R

Example.

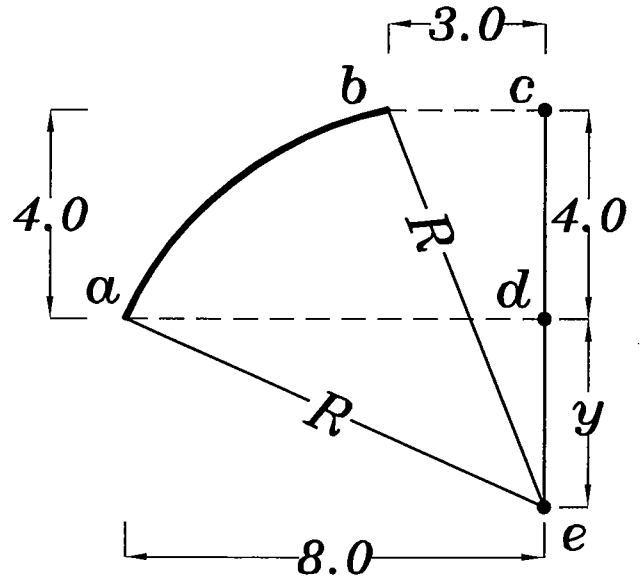
Fined the radius For the
Dome Contains the Arch *a b*



For Triangle *a d e*

$$R^2 = 8.0^2 + y^2$$

$$\therefore R^2 = 64 + y^2 \quad \text{--- } R, y \text{ --- } \textcircled{1}$$



For Triangle *e c b*

$$R^2 = 3.0^2 + (y + 4.0)^2$$

$$R^2 = 9.0 + y^2 + 8.0 y + 16.0$$

$$R^2 = 25.0 + y^2 + 8.0 y \quad \text{--- } R, y \text{ --- } \textcircled{2}$$

بتعويض R^2 من المعادله الاولى فى المعادله الثانيه

$$\therefore 64 + y^2 = 25.0 + y^2 + 8.0 y \longrightarrow y = 4.875 \text{ m}$$

$$\therefore R^2 = 64 + 4.875^2 = 87.76 \text{ m}^2 \longrightarrow \boxed{R = 9.37 \text{ m}}$$

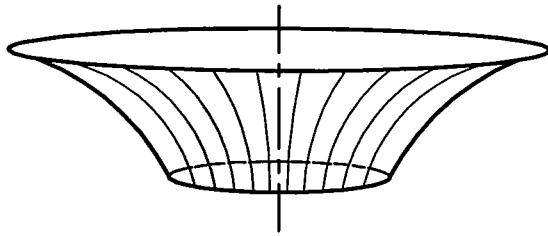
Special Case.

يمكن تأجيل قراءه هذه الحاله حتى الانتهاء من الدرس و بدء حل الامثله

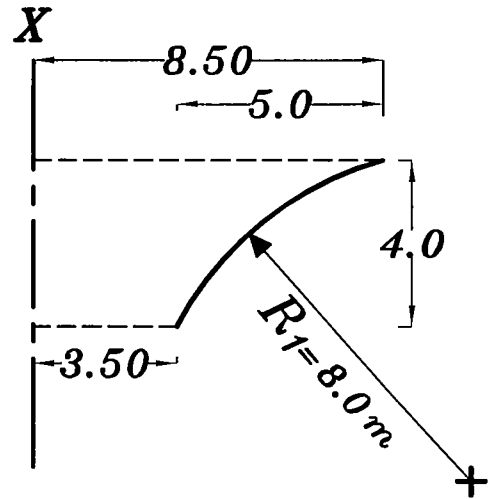
اذا كان المنحنى للخارج (كما بالشكل فى الاسفل) ستكون $R_1 \neq R_2$ و يجب ان يكون نصف قطر المنحنى (R_1) معطى لكى نستطيع تكمله حسابات المسأله. سنحتاج لتحديد مكان المحور (Y) الذى يوجد عنده مركز الدائره المكونه لهذا المنحنى. ثم نحدد المسافه الافقيه بين المحور (Y) و محور الدوران (X).

Example.

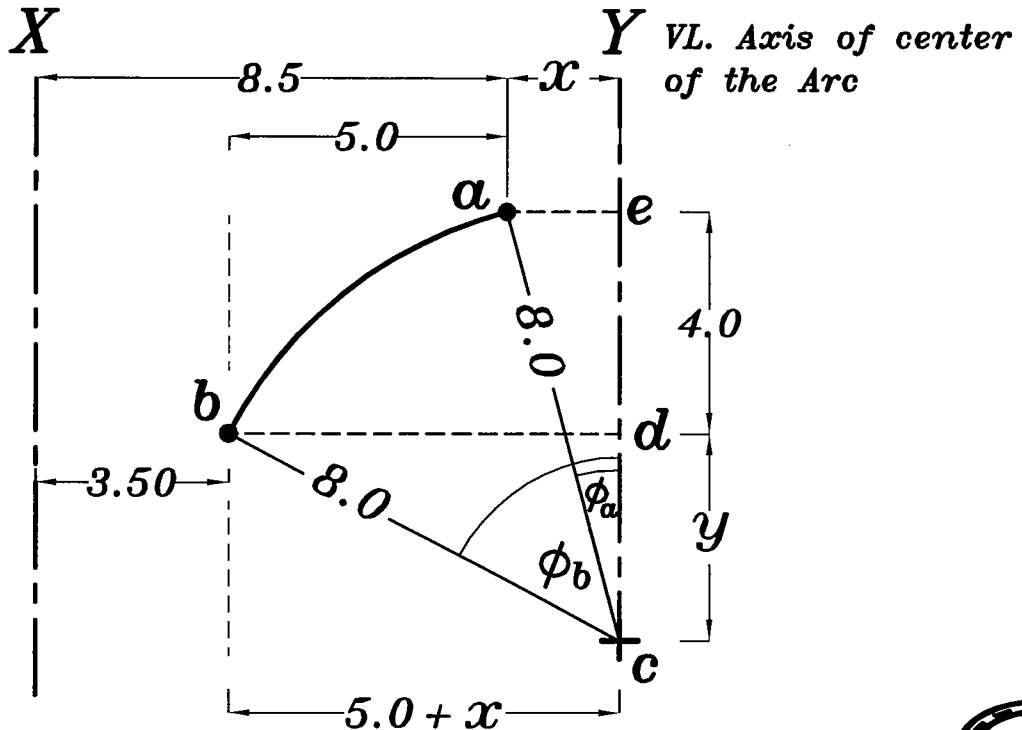
*Fined The surface Area
For the Given Dome.*



A.O.R.

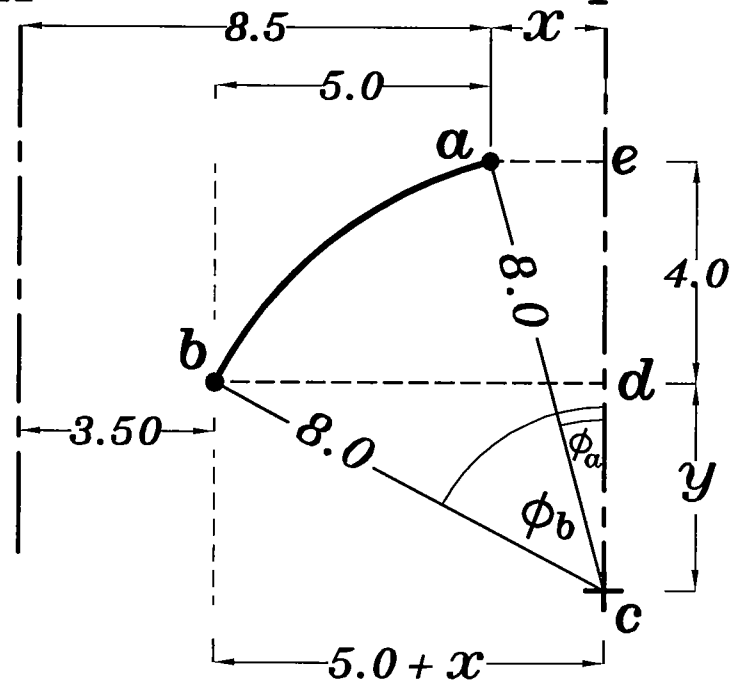


A.O.R.



A.O.R.
X

VL. Axis of center
of the Arc
Y



For Triangle b c d

$$8.0^2 = y^2 + (x+5.0)^2$$

$$64 = y^2 + (x+5.0)^2$$

$$\therefore y^2 = 64 - (x+5.0)^2 \quad \text{--- } x, y \text{ --- } \textcircled{1}$$

For Triangle a c e

$$8.0^2 = x^2 + (y+4)^2$$

$$\therefore 64 = x^2 + (y+4)^2 \quad \text{--- } x, y \text{ --- } \textcircled{2}$$

Substitution From $\textcircled{1}$ in $\textcircled{2}$

$$\therefore 64 = x^2 + (y+4)^2 = x^2 + y^2 + 8y + 16$$

$$\therefore \cancel{64} = x^2 + \cancel{64} - (x+5)^2 + 8 * \sqrt{64 - (x+5)^2} + 16$$

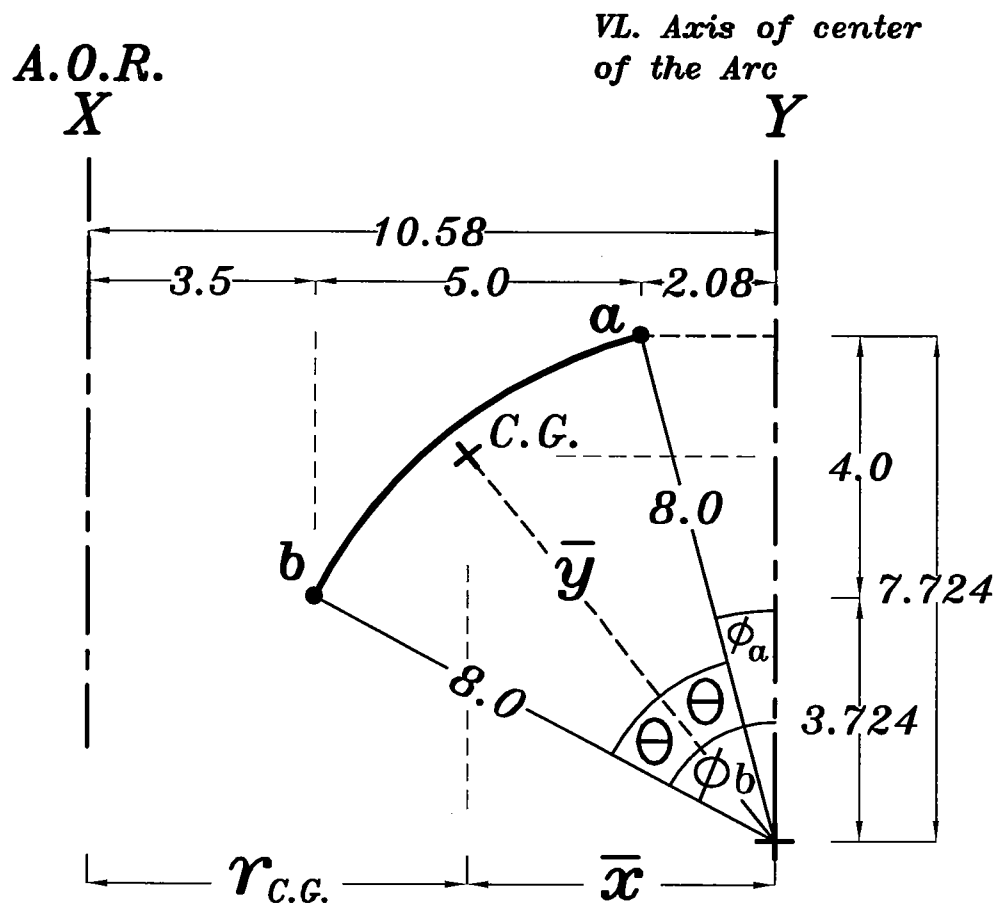
$$0.0 = x^2 - (x^2 + 10x + 25) + 8 * \sqrt{64 - (x+5)^2} + 16$$

$$0.0 = \cancel{x^2} - \cancel{x^2} - 10x - 25 + 8 * \sqrt{64 - (x+5)^2} + 16$$

$$0.0 = -10x - 9.0 + 8 * \sqrt{64 - (x+5)^2} \longrightarrow \boxed{x = 2.08 \text{ m}}$$

$$\therefore y^2 = 64 - (x+5)^2 = 64 - (2.08+5)^2$$

$$\therefore y^2 = 13.873 \longrightarrow \boxed{y = 3.724 \text{ m}}$$



$$\sin \phi_a = \frac{2.08}{8.0} \rightarrow \boxed{\phi_a = 15.07^\circ}$$

$$\cos \phi_b = \frac{3.724}{8.0} \rightarrow \boxed{\phi_b = 62.257^\circ}$$

$$\text{Central Angle } \Theta = \frac{\phi_b - \phi_a}{2} = \frac{62.257 - 15.07}{2} = 23.59^\circ$$

$$\bar{y} = \frac{R * \sin \Theta}{\Theta} = \frac{8.0 * \sin 23.59^\circ}{23.59 * \pi / 180} = 7.775 \text{ m}$$

$$\therefore \sin(\phi_a + \Theta) = \frac{\bar{x}}{\bar{y}} \therefore \sin(15.07 + 23.59) = \frac{\bar{x}}{7.775} \rightarrow \bar{x} = 4.857 \text{ m}$$

$$r_{C.G.} = \text{Distance between the Two axes} - \bar{x}$$

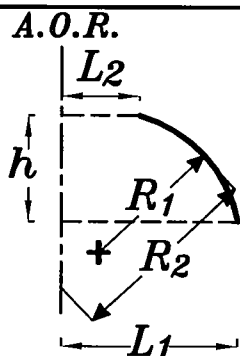
$$r_{C.G.} = 10.58 - 4.857 = 5.723 \text{ m}$$

$$\text{Arc Length} = 2 * R * \Theta = 2 * 8.0 * 23.59 * \frac{\pi}{180} = 6.587 \text{ m}$$

$$S.A. = \text{Arc Length} * 2 \pi * r_{C.G.} = 6.587 * 2 \pi * 5.723 = 236.86 \text{ m}^2$$

Special Case.

يمكن تأجيل قراءه هذه الحاله حتى الانتهاء من الدرس و بدء حل الامثله



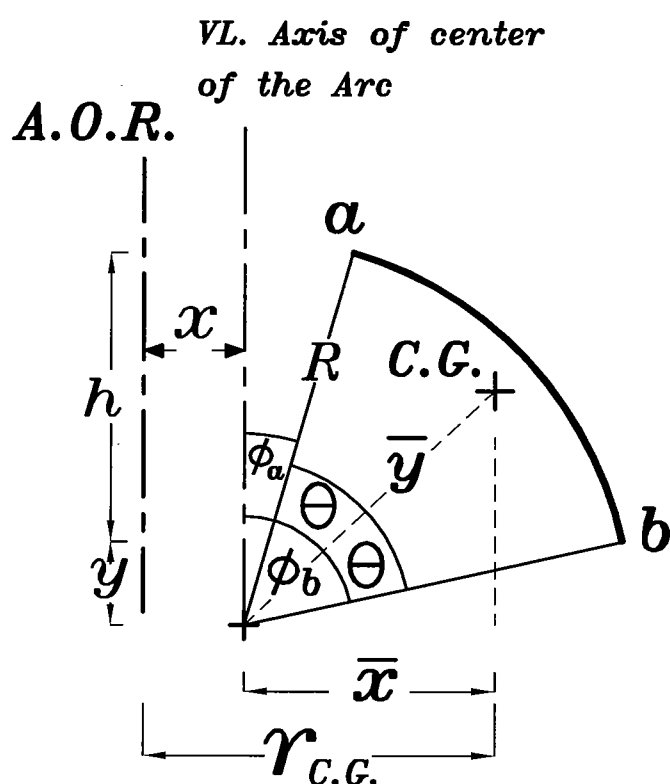
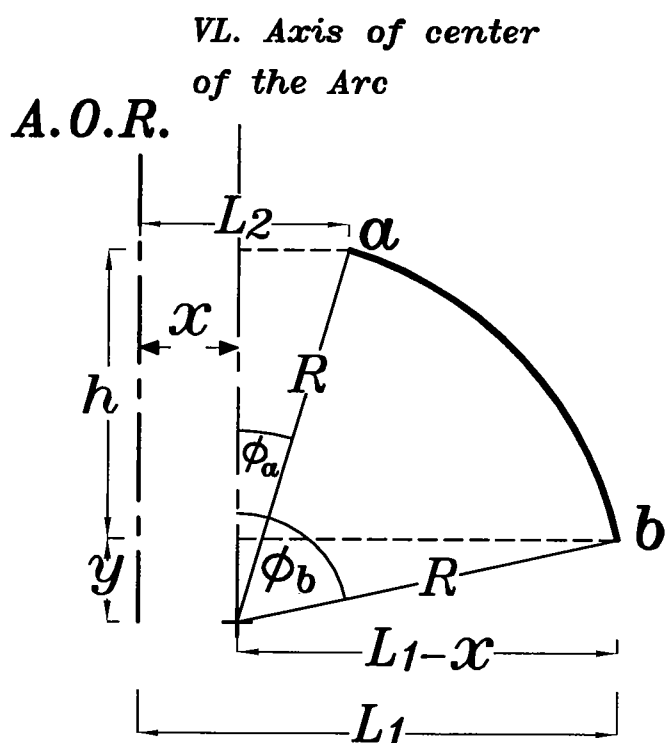
اذا كان المنحنى للداخل لكن مركزه ليس على ال A.O.R.

ستكون $R_1 \neq R_2$

و يجب ان يكون نصف قطر المنحنى (R_1) معطى لكى نستطيع تكمله حسابات المسأله.

سنحتاج لتحديد مكان المحور (Y) الذى يوجد عنده مركز الدائره المكونه لهذا المنحنى .

ثم نحدد المسافه الافقيه بين المحور (Y) و محور الدوران (X) .



$$S.A. = \text{Arc Length} * 2 \pi * r_{c.g.}$$

$$\text{Arc Length} = 2 * R * \theta$$

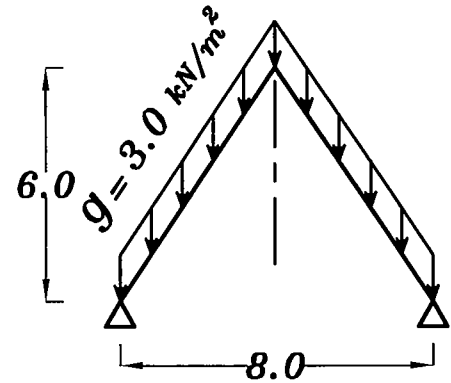
$$\bar{y} = \frac{R * \sin \theta}{\theta}$$

Training To Calculate T_1 & T_2

Example.

Draw T_1 & T_2 distribution
on the vertical projection of
the Cone due to dead load only.

$$g = 3.0 \text{ kN/m}^2$$



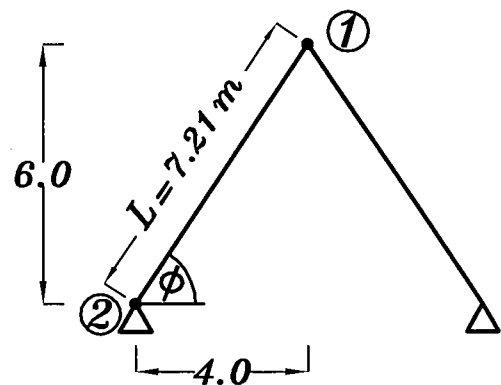
$$\tan \phi = \frac{6.0}{4.0} \rightarrow \boxed{\phi = 56.31^\circ}$$


$$L^2 = 6.0^2 + 4.0^2 \rightarrow \boxed{L = 7.21 \text{ m}}$$

$$R_1 = \infty$$

Sec. ① $T_1 = T_2 = \text{Zero}$

Sec. ② $r = 4.0 \text{ m}$



$$S.A. = \pi * r * L = \pi * 4.0 * 7.21 = 90.60 \text{ m}^2$$


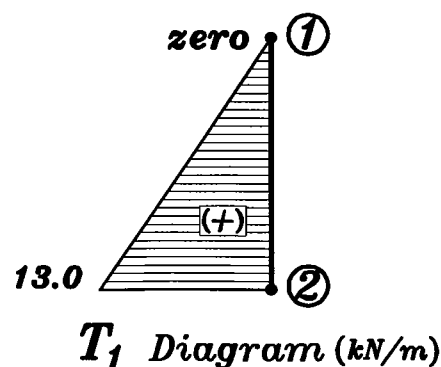
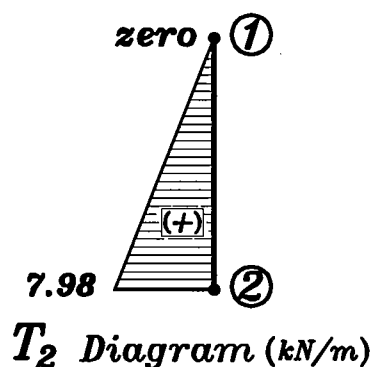
$$W_\phi = g * S.A. = 3.0 * 90.60 = + 271.8 \text{ kN}$$

$$T_1 = \frac{W_\phi}{2\pi r \sin \phi} = \frac{+ 271.8}{2\pi * 4.0 * \sin 56.31^\circ} = + 13.0 \text{ kN/m Comp.}$$

$$Z = g \cos \phi = 3.0 * \cos 56.31^\circ = + 1.664 \text{ kN/m}^2$$

$$R_2 = \frac{r}{\sin \phi} = \frac{4.0}{\sin 56.31^\circ} = 4.80 \text{ m}$$

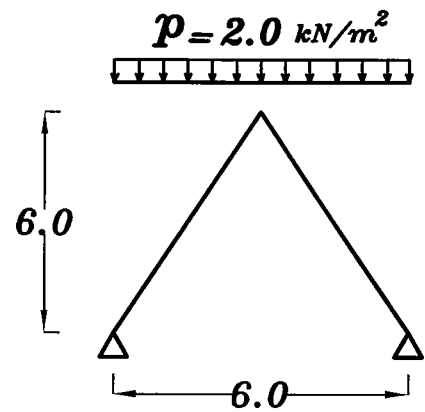
$$\therefore T_2 = Z * R_2 = 1.664 * 4.80 = + 7.98 \text{ kN/m Comp.}$$



Example.

Draw T_1 & T_2 distribution on the vertical projection of the Cone due to live load only.

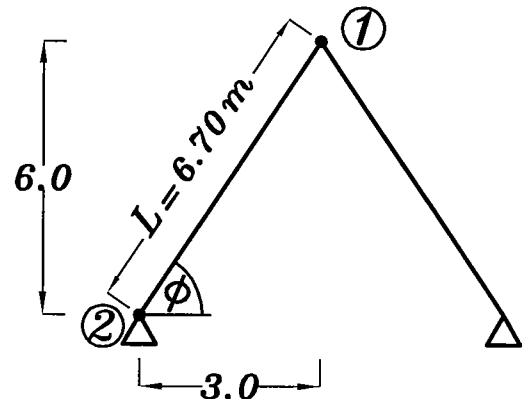
$$p = 2.0 \text{ kN/m}^2$$



$$\tan \phi = \frac{6.0}{3.0} \rightarrow \boxed{\phi = 63.43^\circ}$$

$$L^2 = 6.0^2 + 3.0^2 \rightarrow \boxed{L = 6.70 \text{ m}}$$

$$R_1 = \infty$$



Sec. ① $T_1 = T_2 = \text{Zero}$

Sec. ② $r = 3.0 \text{ m}$

$$\text{Projected area} = \pi * r^2 = \pi * 3.0^2 = 28.27 \text{ m}^2$$

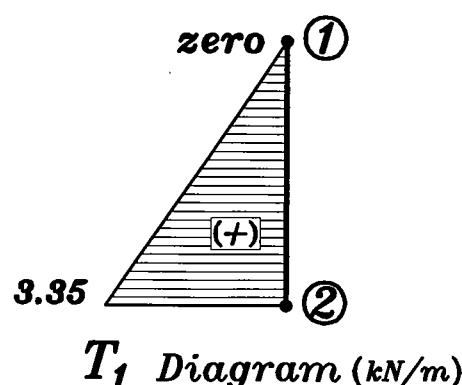
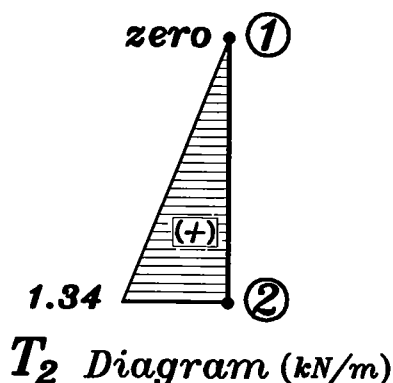
$$W_\phi = p * \text{Projected area} = 2.0 * 28.27 = +56.54 \text{ kN}$$

$$T_1 = \frac{W_\phi}{2\pi r \sin \phi} = \frac{+56.54}{2\pi * 3.0 * \sin 63.43^\circ} = +3.35 \text{ kN/m Comp.}$$

$$Z = p \cos^2 \phi = 2.0 * \cos^2 63.43^\circ = +0.40 \text{ kN/m}^2$$

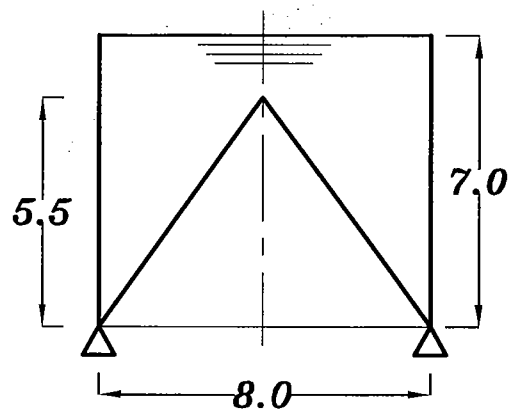
$$R_2 = \frac{r}{\sin \phi} = \frac{3.0}{\sin 63.43^\circ} = 3.35 \text{ m}$$

$$\therefore T_2 = Z * R_2 = 0.40 * 3.35 = +1.34 \text{ kN/m Comp.}$$



Example.

Draw T_1 & T_2 distribution
on the vertical projection of
The Cone due to water pressure.



$$\tan \phi = \frac{5.5}{4.0} \rightarrow \boxed{\phi = 53.97^\circ}$$

$$L^2 = 6.0^2 + 4.0^2 \rightarrow \boxed{L = 6.80 \text{ m}}$$

$$R_1 = \infty$$

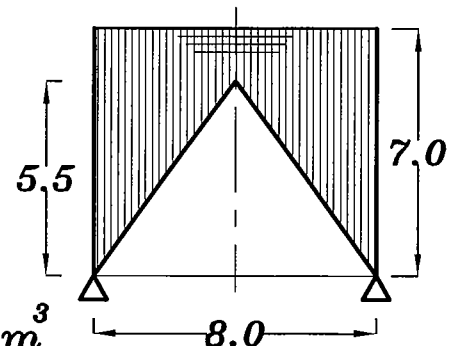
Sec. ① $T_1 = T_2 = \text{Zero}$

Sec. ② $r = 4.0 \text{ m}$

Volume of Cylinder = $\pi * r^2 * h$



$$= \pi * 4.0^2 * 7.0 = 351.85 \text{ m}^3$$

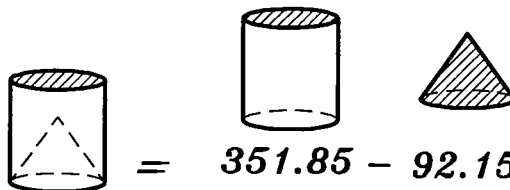


Volume of Cone = $\frac{1}{3} * \pi * r^2 * h$



$$= \frac{1}{3} * \pi * 4.0^2 * 5.5 = 92.15 \text{ m}^3$$

Volume of Water = $351.85 - 92.15 = 259.7 \text{ m}^3$

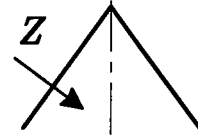


$$W_\phi = \gamma_w * \text{Volume} = 10.0 * 259.7 = +2597.0 \text{ kN} \downarrow$$

$$T_1 = \frac{W_\phi}{2\pi r \sin\phi} = \frac{+2597.0}{2\pi * 4.0 * \sin 53.97^\circ} = +127.77 \text{ kN/m Comp.}$$

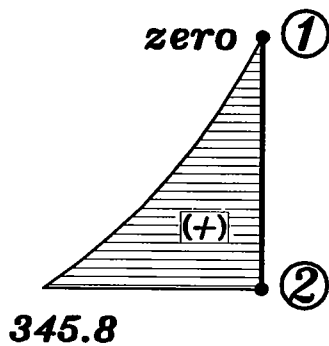
$$Z = \gamma_w * h = 10.0 * 7.0 = +70 \text{ kN/m}^2$$

اشاره Z (+Ve) لان اتجاها داخل الى المحور

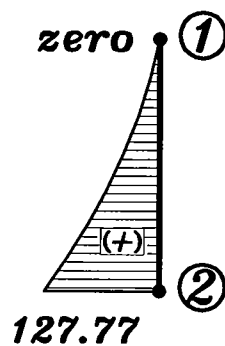


$$R_2 = \frac{r}{\sin\phi} = \frac{4.0}{\sin 53.97^\circ} = 4.94 \text{ m}$$

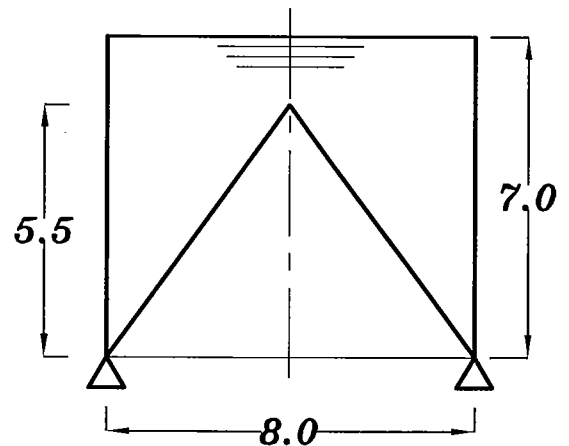
$$\therefore T_2 = Z * R_2 = 70.0 * 4.94 = +345.8 \text{ kN/m Comp.}$$



T_2 Diagram (kN/m)



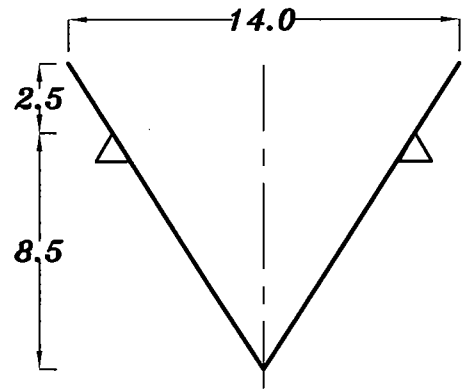
T_1 Diagram (kN/m)



Example.

Draw T_1 & T_2 distribution
on the vertical projection.
due to dead load only.

$$g = 3.0 \text{ kN/m}^2$$



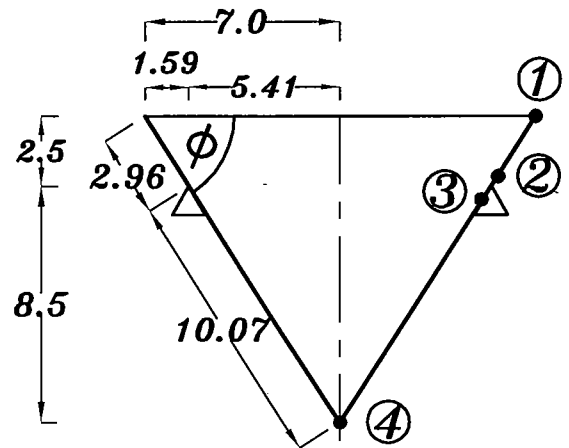
$$\tan \phi = \frac{11}{7.0} \rightarrow \boxed{\phi = 57.53^\circ}$$

$$R_1 = \infty$$

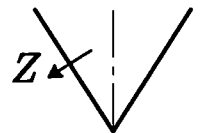
Sec. ① $r = 7.0 \text{ m}$

$$W_\phi = \text{Zero} \rightarrow T_1 = \text{Zero}$$

$$Z = g \cos \phi = 3.0 * \cos 57.53^\circ = -1.61 \text{ kN/m}^2$$



اشاره Z (-ve) لان اتجاهها خارج من المحور



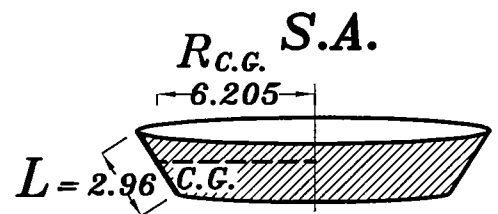
$$R_2 = \frac{r}{\sin \phi} = \frac{7.0}{\sin 57.53^\circ} = 8.297 \text{ m}$$

$$T_2 = Z * R_2 = -1.61 * 8.297 = -13.35 \text{ kN/m Ten.}$$

Sec. ② $r = 5.41 \text{ m}$

$$S.A. = L * 2 \pi * R_{c.g.}$$

$$= 2.96 * 2 \pi * 6.205 = 115.4 \text{ m}^2$$



$$W_\phi = g * S.A. = 3.0 * 115.4 = + 346.2 \text{ kN}$$

$$T_1 = \frac{W_\phi}{2 \pi r \sin \phi} = \frac{+ 346.2}{2 \pi * 5.41 * \sin 57.53^\circ} = + 12.07 \text{ kN/m Comp.}$$

$$Z = g \cos \phi = -1.61 \text{ kN/m}^2$$

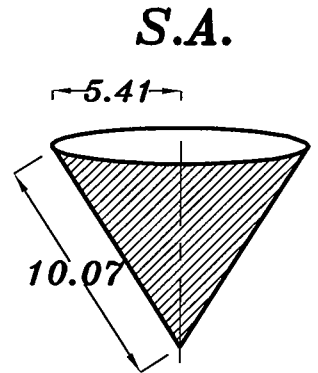
$$R_2 = \frac{r}{\sin \phi} = \frac{5.41}{\sin 57.53^\circ} = 6.41 \text{ m}$$

$$T_2 = Z * R_2 = -1.61 * 6.41 = -10.32 \text{ kN/m Ten.}$$

Sec. ③ $r = 5.41 \text{ m}$

$$S.A. = \pi * L * r = \pi * 10.07 * 5.41 = 171.15 \text{ m}^2$$

$$W_\phi = g * S.A. = 3.0 * 171.15 = -513.45 \text{ kN}$$



اشاره W_ϕ (-Ve) لان اتجاهها خارج من ال Support

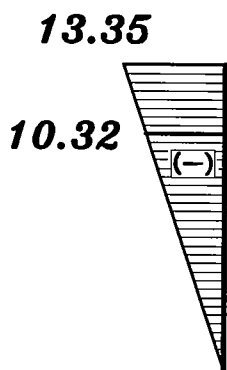
$$T_1 = \frac{W_\phi}{2\pi r \sin \phi} = \frac{-513.45}{2\pi * 5.41 * \sin 57.53^\circ} = -17.90 \text{ kN/m Ten.}$$

$$R_2 = \frac{r}{\sin \phi} = \frac{5.41}{\sin 57.53^\circ} = 6.41 \text{ m}$$

$$T_2 = Z * R_2 = -1.61 * 6.41 = -10.32 \text{ kN/m Ten.}$$

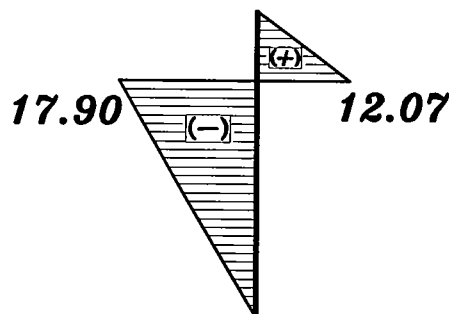
Sec. ④ Vertex of the Cone.

$$T_1 = T_2 = \text{Zero}$$



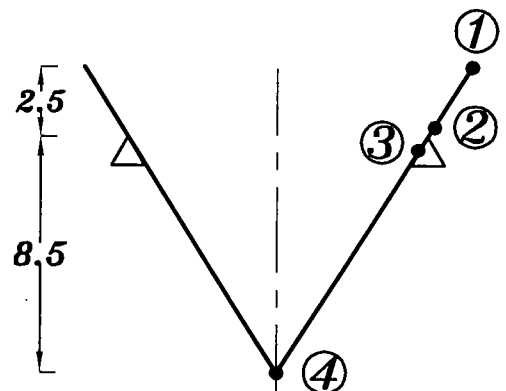
T_2

Diagram (kN/m)



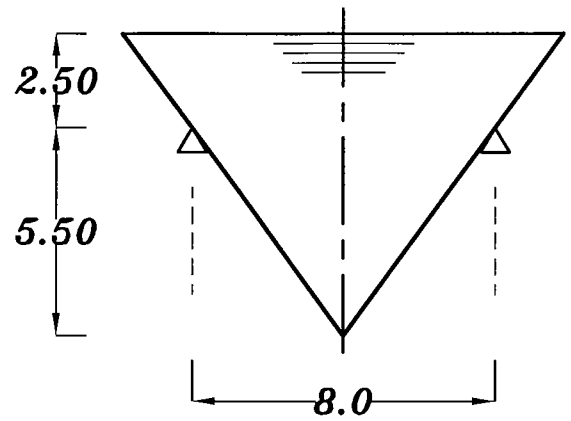
T_1

Diagram (kN/m)



Example.

Draw T_1 & T_2 distribution on the vertical projection due to water pressure.



$$\tan \phi = \frac{5.5}{4.0} \rightarrow \boxed{\phi = 53.97^\circ}$$

$$R_1 = \infty$$

Sec. ① $r = 5.1 \text{ m}$

$$W_\phi = \text{Zero} \rightarrow T_1 = \text{Zero}$$

$$Z = \delta_w * h = \delta_w * \text{Zero} = \text{Zero}$$

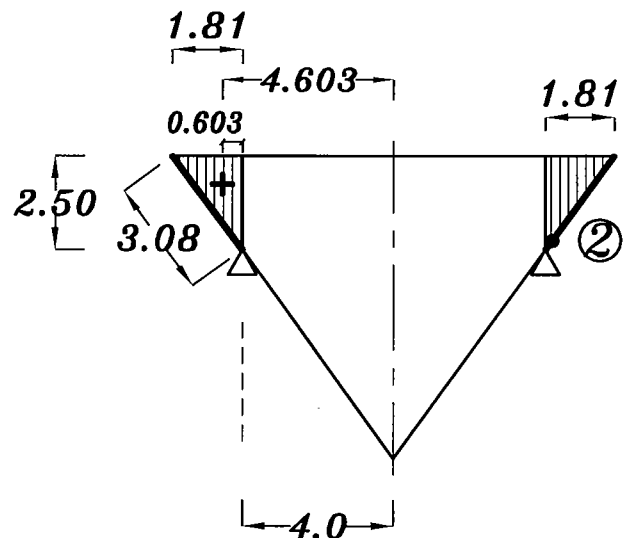
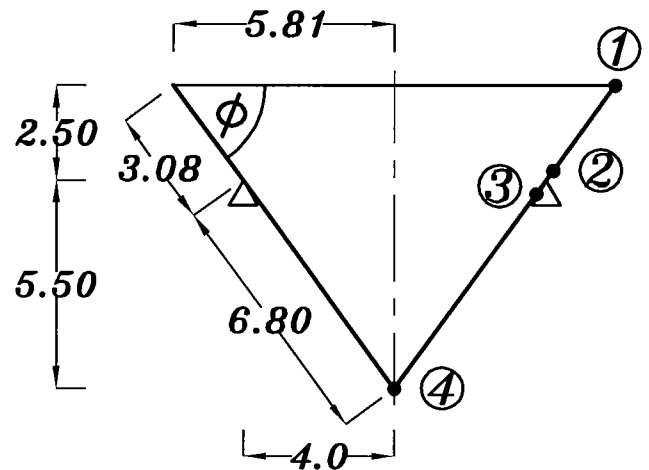
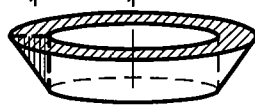
$$T_2 = Z * R_2 = \text{Zero}$$

Sec. ② $r = 4.0 \text{ m}$

Volume of water =



$$= \text{Area} * 2\pi * R_{c.g.}$$



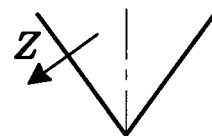
$$\text{Volume of water} = \left(\frac{1}{2} * 1.81 * 2.5 \right) * 2\pi * 4.603 = 65.43 \text{ m}^3$$

$$W_\phi = \delta_w * \text{Volume} = 10.0 * 65.43 = +654.3 \text{ kN}$$

$$T_1 = \frac{W_\phi}{2\pi r \sin \phi} = \frac{+654.3}{2\pi * 4.0 * \sin 53.97^\circ} = +32.19 \text{ kN/m Comp.}$$

$$Z = \delta_w * h = 10.0 * 2.5 = -25 \text{ kN/m}^2$$

اشاره Z (-ve) لان اتجاها خارج من المحور

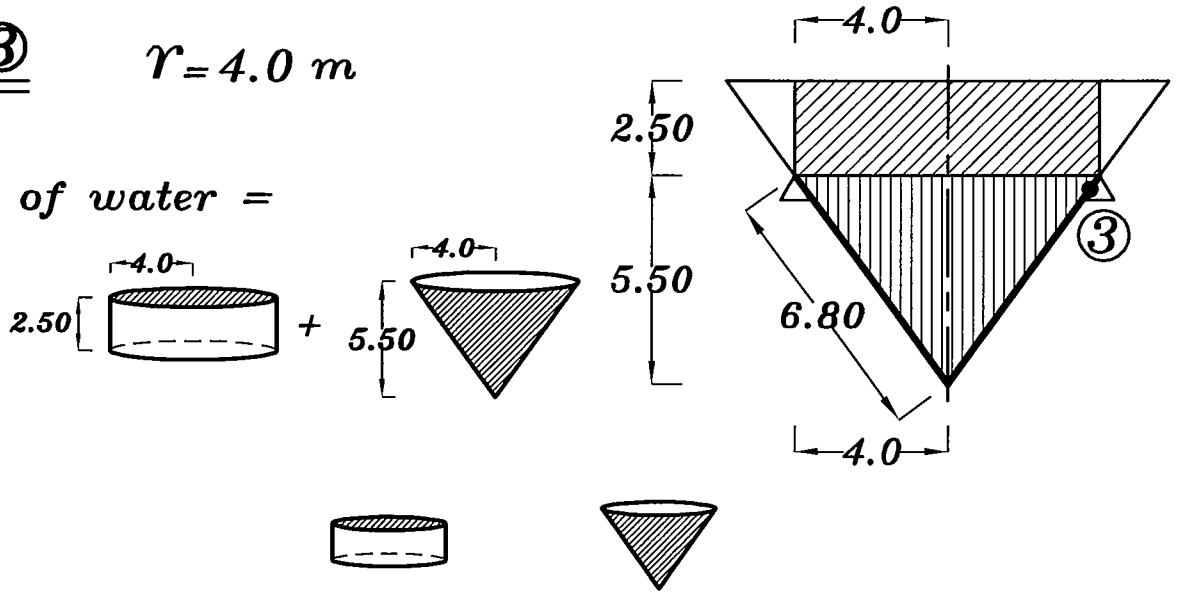


$$R_2 = \frac{r}{\sin \phi} = \frac{4.0}{\sin 53.97^\circ} = 4.94 \text{ m}$$

$$\therefore T_2 = Z * R_2 = -25 * 4.94 = -123.5 \text{ kN/m Ten.}$$

Sec. ③ $r = 4.0 \text{ m}$

Volume of water =



$$\begin{aligned} \text{Volume of water} &= \pi r^2 * h + \frac{1}{3} * \pi * r^2 * h \\ &= \pi * 4.0^2 * 2.5 + \frac{1}{3} * \pi * 4.0^2 * 5.5 = 217.82 \text{ m}^3 \end{aligned}$$

$$W_\phi = \gamma_w * \text{Volume} = 10.0 * 217.8 = -2178.2 \text{ kN}$$

اشاره W_ϕ (-Ve) لان اتجاهها خارج من ال Support

$$T_1 = \frac{W_\phi}{2\pi r \sin \phi} = \frac{-2178.2}{2\pi * 4.0 * \sin 53.97^\circ} = -107.17 \text{ kN/m Comp.}$$

$$Z = \gamma_w * h = 10.0 * 2.5 = -25 \text{ kN/m}^2$$

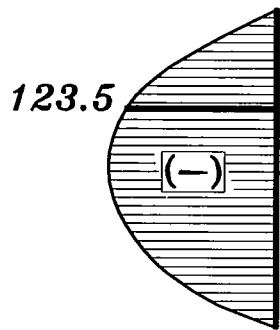
اشاره Z (-Ve) لان اتجاهها خارج من المحور

$$R_2 = \frac{r}{\sin \phi} = \frac{4.0}{\sin 53.97^\circ} = 4.94 \text{ m}$$

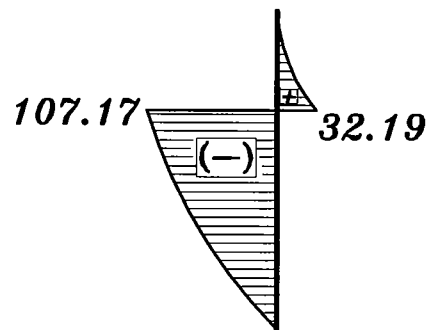
$$\therefore T_2 = Z * R_2 = -25 * 4.94 = -123.5 \text{ kN/m Ten.}$$

Sec. ④ *Vertex of the Cone.*

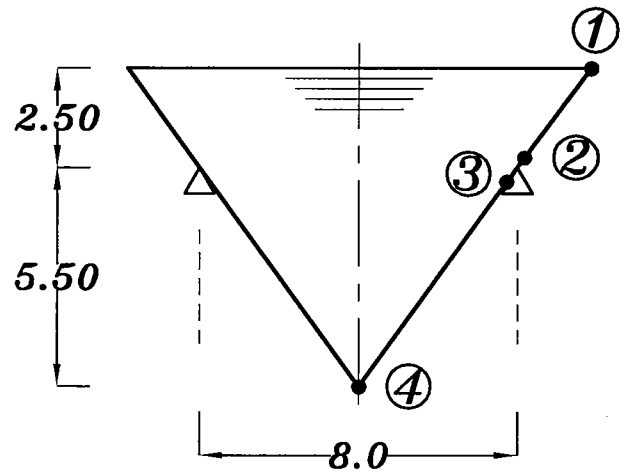
$$T_1 = T_2 = \text{Zero}$$



T_2
Diagram (kN/m)

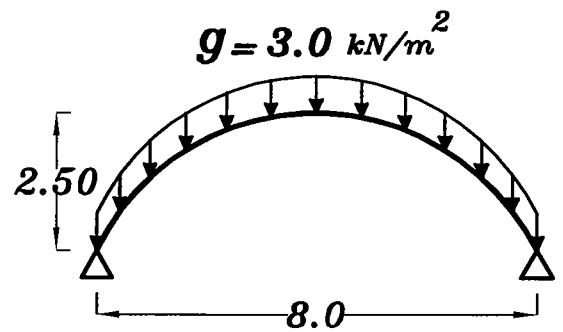


T_1
Diagram (kN/m)



Example.

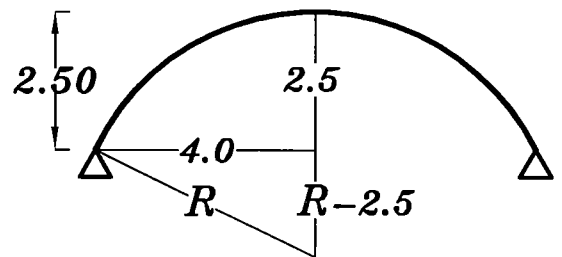
Draw T_1 & T_2 distribution
(at least 3 points) on the vertical
projection of the Dome due to
Dead load only. $g = 3.0 \text{ kN/m}^2$



$$R^2 = 4.0^2 + (R - 2.5)^2$$

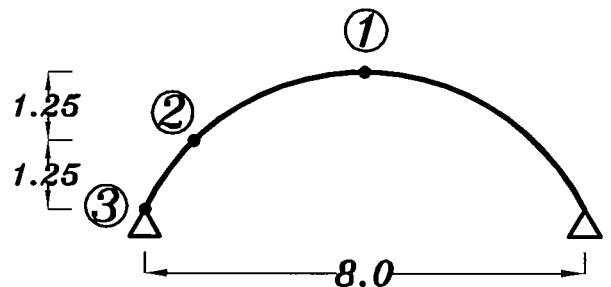
$$R^2 = 16 + R^2 - 5R + 6.25$$

$$5R = 22.25 \rightarrow \boxed{R = 4.45 \text{ m}}$$



Sec. ① $\phi = \text{Zero}$

$$Z = g \cos \phi = 3.0 * \cos 0.0 \\ = + 3.0 \text{ kN/m}^2$$



$$T_1 = T_2 = \frac{RZ}{2} = \frac{4.45 * 3.0}{2} = + 6.675 \text{ kN/m Comp.}$$

Sec. ②

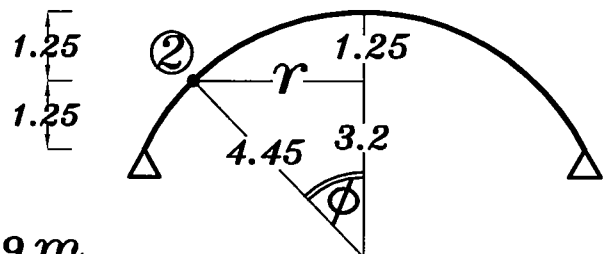
$$\cos \phi = \frac{3.2}{4.45} \rightarrow \boxed{\phi = 44.02^\circ}$$

$$r = R \sin \phi = 4.45 * \sin 44.02^\circ = 3.09 \text{ m}$$

$$S.A. = 2\pi * R * h = 2\pi * 4.45 * 1.25 = 34.95 \text{ m}^2$$

$$W_\phi = g * S.A. = 3.0 * 34.95 = + 104.85 \text{ kN}$$

$$T_1 = \frac{W_\phi}{2\pi r \sin \phi} = \frac{+ 104.85}{2\pi * 3.09 * \sin 44.02^\circ} = + 7.77 \text{ kN/m Comp.}$$



$$R_1 = R_2 = R = 4.45 \text{ m}$$

$$Z = g \cos \phi = 3.0 * \cos 44.02^\circ = + 2.157 \text{ kN/m}^2$$

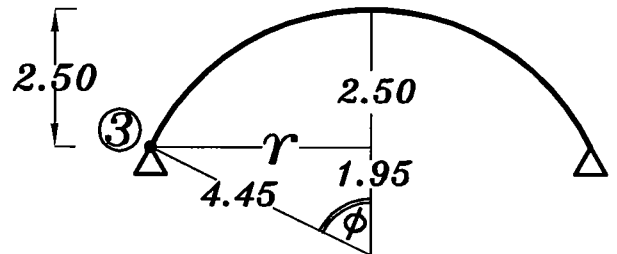
$$\therefore T_1 + T_2 = Z * R \quad \therefore + 7.77 + T_2 = 2.157 * 4.45$$

$$\therefore T_2 = + 1.83 \text{ kN/m Comp.}$$

Sec. ③

$$\cos \phi = \frac{1.95}{4.45} \rightarrow \boxed{\phi = 64.01^\circ}$$

$$r = 4.0 \text{ m}$$



$$S.A. = 2\pi * R * h \quad \text{(shaded semi-circle)} = 2\pi * 4.45 * 2.50 = 69.90 \text{ m}^2$$

$$W_\phi = g * S.A. = 3.0 * 69.90 = + 209.7 \text{ kN}$$

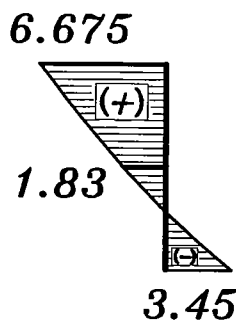
$$T_1 = \frac{W_\phi}{2\pi r \sin \phi} = \frac{+ 209.7}{2\pi * 4.0 * \sin 64.01^\circ} = + 9.28 \text{ kN/m Comp.}$$

$$R_1 = R_2 = R = 4.45 \text{ m}$$

$$Z = g \cos \phi = 3.0 * \cos 64.01^\circ = + 1.31 \text{ kN/m}^2$$

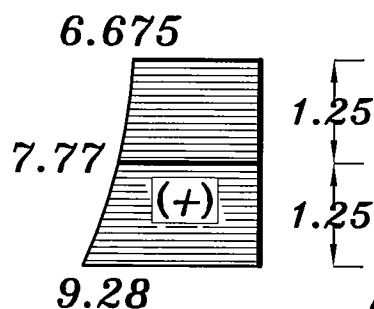
$$\therefore T_1 + T_2 = Z * R \quad \therefore + 9.28 + T_2 = 1.31 * 4.45$$

$$\therefore T_2 = - 3.45 \text{ kN/m Ten.}$$



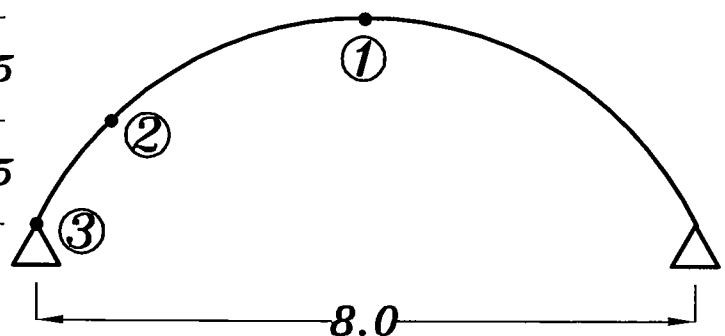
T_2

Diagram (kN/m)



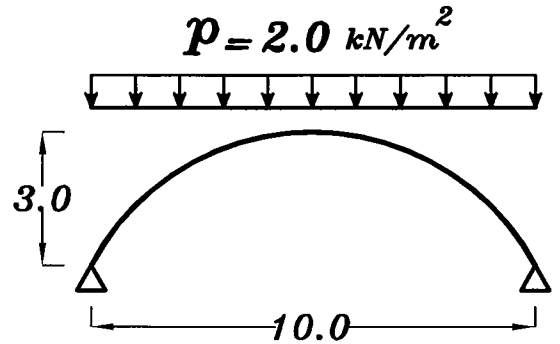
T_1

Diagram (kN/m)



Example.

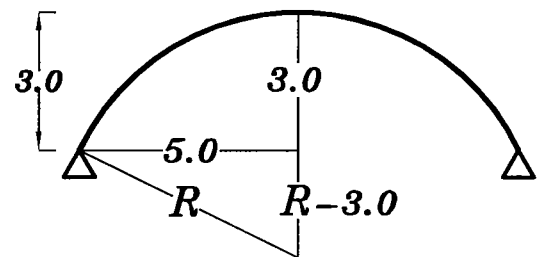
Draw T_1 & T_2 distribution
(at least 3 points) on the vertical
projection of the Dome due to
Live load only. $p = 2.0 \text{ kN/m}^2$



$$R^2 = 5.0^2 + (R - 3.0)^2$$

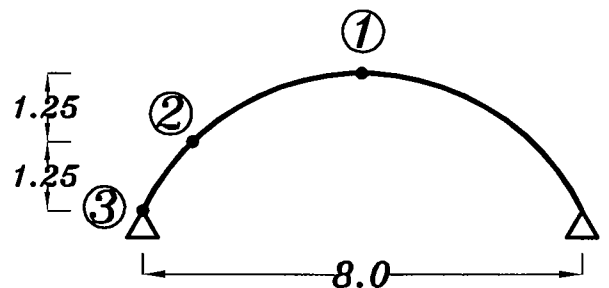
$$R^2 = 25 + R^2 - 6R + 9.0$$

$$6R = 34.0 \rightarrow \boxed{R = 5.66 \text{ m}}$$



Sec. ① $\phi = \text{Zero}$

$$Z = p \cos^2 \phi = 2.0 * \cos^2 0.0 \\ = + 2.0 \text{ kN/m}^2$$



$$T_1 = T_2 = \frac{RZ}{2} = \frac{5.66 * 2.0}{2} = + 5.66 \text{ kN/m Comp.}$$

Sec. ②

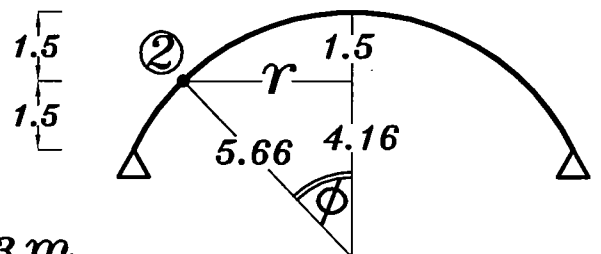
$$\cos \phi = \frac{4.16}{5.66} \rightarrow \boxed{\phi = 42.69^\circ}$$

$$r = R \sin \phi = 5.66 * \sin 42.69^\circ = 3.83 \text{ m}$$

$$\text{Projected area} = \pi * r^2 = \pi * 3.83^2 = 46.08 \text{ m}^2$$

$$W_\phi = p * \text{Projected area} = 2.0 * 46.08 = + 92.16 \text{ kN}$$

$$T_1 = \frac{W_\phi}{2 \pi r \sin \phi} = \frac{+ 92.16}{2 \pi * 3.83 * \sin 42.69^\circ} = + 5.66 \text{ kN/m Comp.}$$



$$R_1 = R_2 = R = 5.66 \text{ m}$$

$$Z = p \cos^2 \phi = 2.0 * \cos^2 42.69^\circ = + 1.08 \text{ kN/m}^2$$

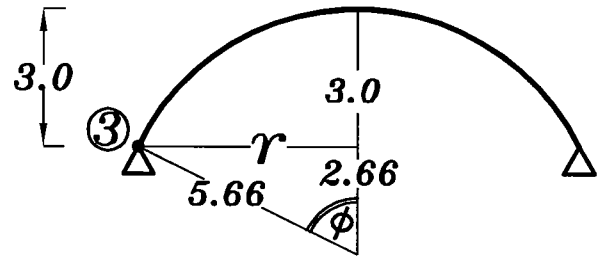
$$\therefore T_1 + T_2 = Z * R \quad \therefore + 5.65 + T_2 = 1.08 * 5.66$$

$$\therefore T_2 = + 0.46 \text{ kN/m Comp.}$$

Sec. ③

$$\cos \phi = \frac{2.66}{5.66} \rightarrow \boxed{\phi = 61.96^\circ}$$

$$r = 5.0 \text{ m}$$



$$\text{Projected area} = \pi * r^2 \text{ (shaded oval)} = \pi * 5.0^2 = 78.54 \text{ m}^2$$

$$W_\phi = p * \text{Projected area} = 2.0 * 78.54 = + 157.08 \text{ kN}$$

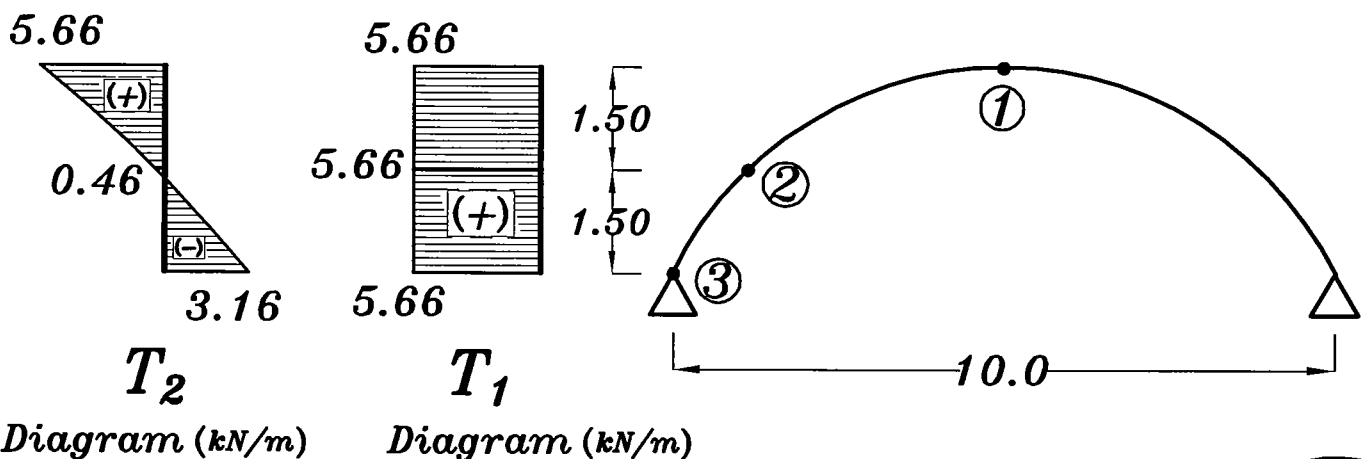
$$T_1 = \frac{W_\phi}{2 \pi r \sin \phi} = \frac{+ 157.08}{2 \pi * 5.0 * \sin 61.96^\circ} = + 5.66 \text{ kN/m Comp.}$$

$$R_1 = R_2 = R = 5.66 \text{ m}$$

$$Z = p \cos^2 \phi = 2.0 * \cos^2 61.96^\circ = + 0.442 \text{ kN/m}^2$$

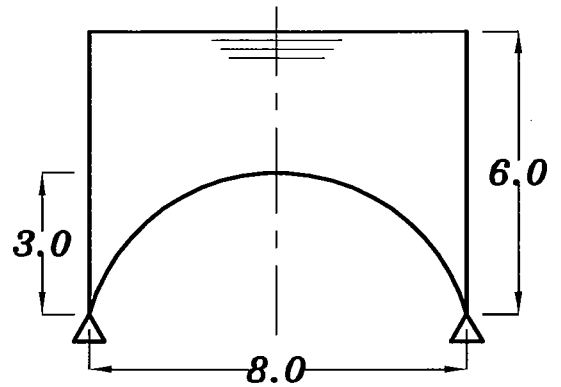
$$\therefore T_1 + T_2 = Z * R \quad \therefore + 5.66 + T_2 = 0.442 * 5.66$$

$$\therefore T_2 = - 3.16 \text{ kN/m Ten.}$$



Example.

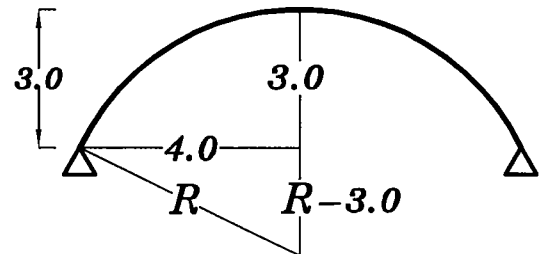
Draw T_1 & T_2 distribution
(at least 3 points) on the vertical
projection of the Dome due to
water pressure only.



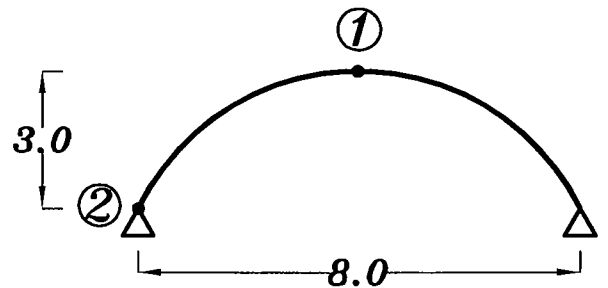
$$R^2 = 4.0^2 + (R - 3.0)^2$$

$$R^2 = 16 + R^2 - 6R + 9.0$$

$$6R = 25.0 \rightarrow \boxed{R = 4.17 \text{ m}}$$



Sec. ① $\phi = \text{Zero}$



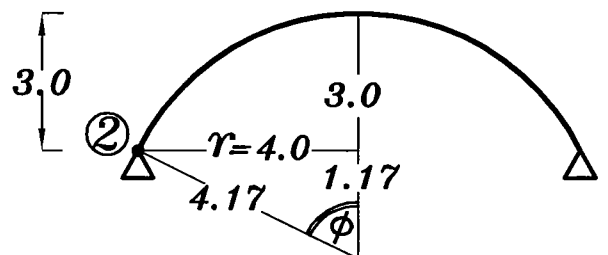
$$Z = \gamma_w * h = 10.0 * 3.0 = + 30 \text{ kN/m}^2$$


$$T_1 = T_2 = \frac{RZ}{2} = \frac{4.17 * 30}{2} = + 62.55 \text{ kN/m Comp.}$$

Sec. ②


$$\cos \phi = \frac{1.17}{4.17} \rightarrow \boxed{\phi = 73.70^\circ}$$

$$r = 4.0 \text{ m}$$




$$\text{Volume of Cylinder} = \pi * r^2 * h$$


$$= \pi * 4.0^2 * 6.0 = 301.6 \text{ m}^3$$

$$\text{Volume of Dome} = \frac{\pi * h}{6} (3r^2 + h^2)$$


$$= \frac{\pi * 3.0}{6} (3 * 4.0^2 + 3.0^2) = 89.53 \text{ m}^3$$

$$\text{Volume of Water} = 301.6 - 89.53 = 212.07 \text{ m}^3$$


$$W_\phi = \gamma_w * \text{Volume} = 10.0 * 212.07 = +2120.7 \text{ kN}$$

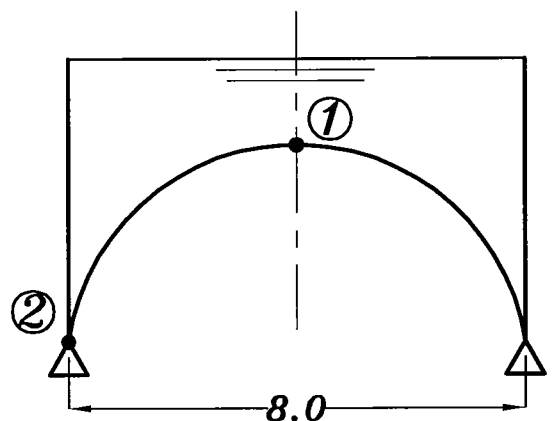
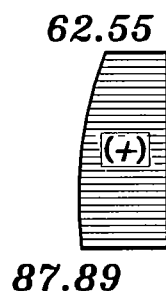
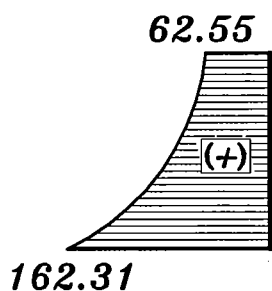
$$T_1 = \frac{W_\phi}{2\pi r \sin \phi} = \frac{+2120.7}{2\pi * 4.0 * \sin 73.70^\circ} = +87.89 \text{ kN/m Comp.}$$

$$R_1 = R_2 = R = 4.17 \text{ m}$$

$$Z = \gamma_w * h = 10.0 * 6.0 = +60 \text{ kN/m}^2$$

$$\therefore T_1 + T_2 = Z * R \quad \therefore +87.89 + T_2 = 60 * 4.17$$

$$\therefore T_2 = +162.31 \text{ kN/m Comp.}$$

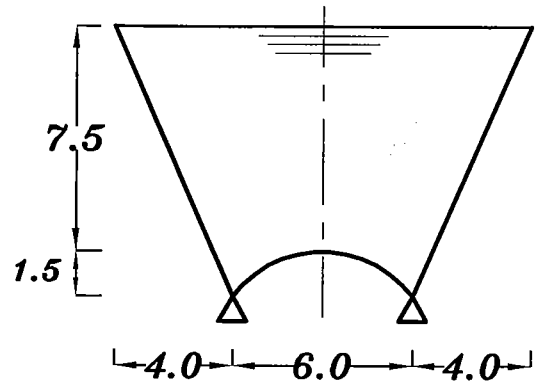


T_2 Diagram (kN/m)

T_1 Diagram (kN/m)

Example.

Draw T_1 & T_2 distribution
on the vertical projection.
due to dead load & water pressure.
 $t_s = 0.16 \text{ m}$



$$\text{Dead Load} = g = t_s \gamma_c = 0.16 * 25 = 4.0 \text{ kN/m}^2$$

For Cone

$$\tan \phi = \frac{9.0}{4.0} \rightarrow \boxed{\phi = 66.03^\circ}$$

Sec. ① $r = 7.0 \text{ m}$

$$W_\phi = \text{Zero} \rightarrow T_1 = \text{Zero}$$

$$Z = g \cos \phi + \gamma_w * h = 4.0 * \cos 66.03^\circ + \gamma_w * \text{Zero} = -1.62 \text{ kN/m}^2$$

اشاره Z $(-Ve)$ لان اتجاها خارج من المحور

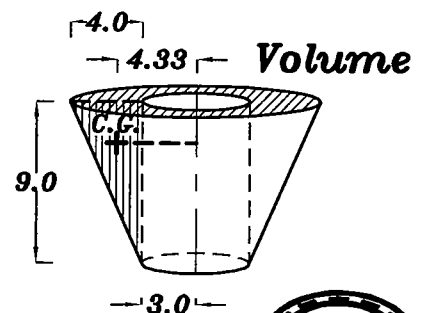
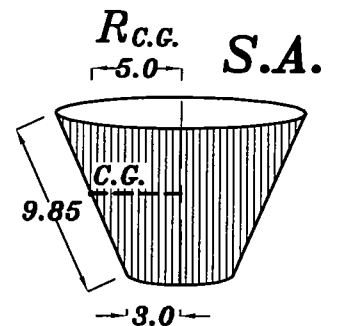
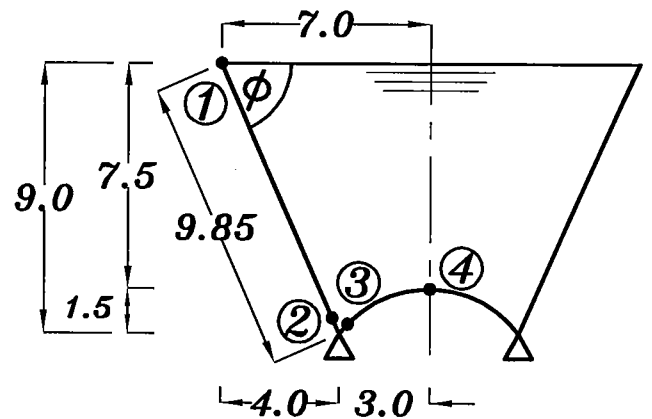
$$R_2 = \frac{r}{\sin \phi} = \frac{7.0}{\sin 66.03^\circ} = 7.66 \text{ m}$$

$$T_2 = Z * R_2 = -1.62 * 7.66 = -12.41 \text{ kN/m Ten.}$$

Sec. ② $r = 3.0 \text{ m}$

$$\begin{aligned} S.A. &= L * 2\pi * R_{c.g.} \\ &= 9.85 * 2\pi * 5.0 = 309.44 \text{ m}^2 \end{aligned}$$

$$\begin{aligned} \text{Volume of water} &= \text{Area} * 2\pi * R_{c.g.} \\ &= \left(\frac{1}{2} * 4.0 * 9.0\right) * 2\pi * 4.33 \\ &= 489.71 \text{ m}^3 \end{aligned}$$



$$W_{\phi} = g * S.A. + \gamma_w * Volume$$

$$= 4.0 * 309.44 + 10.0 * 489.71 = 6134.86 \text{ kN}$$

$$T_1 = \frac{W_{\phi}}{2\pi r \sin \phi} = \frac{+6134.86}{2\pi * 3.0 * \sin 66.03^{\circ}} = +356.18 \text{ kN/m Comp.}$$

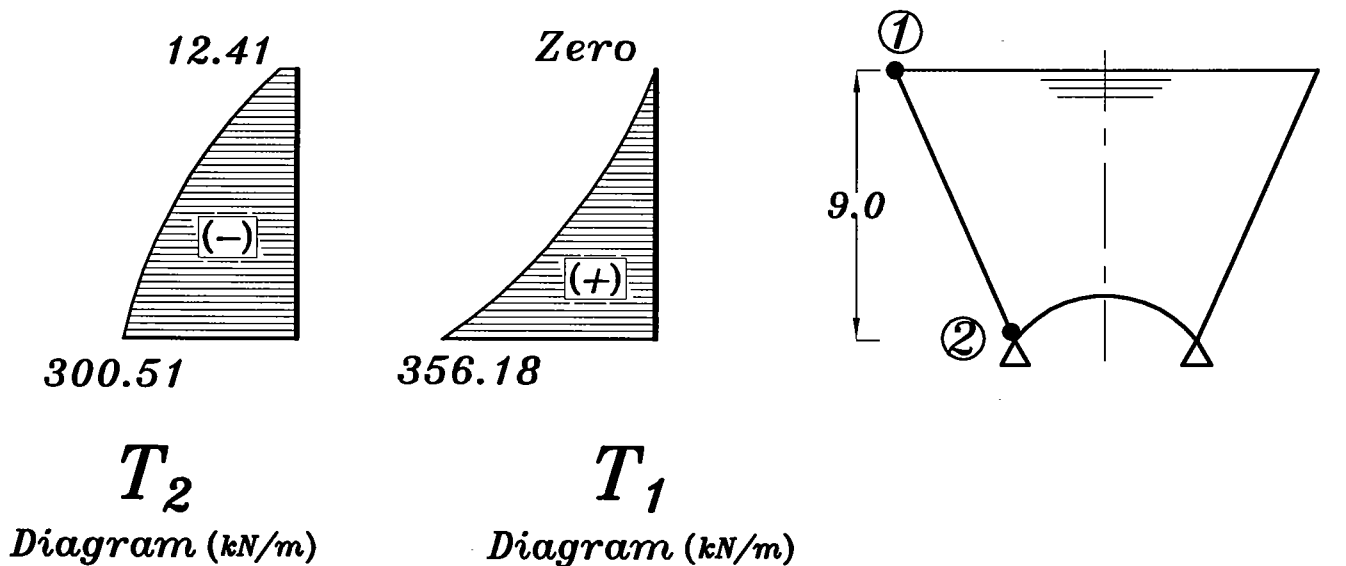
$$Z = g \cos \phi + \gamma_w * h = 4.0 * \cos 66.03^{\circ} + 10 * 9.0 = -91.62 \text{ kN/m}^2$$

اشاره Z (-ve) لان اتجاها خارج من المحور

$$R_2 = \frac{r}{\sin \phi} = \frac{3.0}{\sin 66.03^{\circ}} = 3.28 \text{ m}$$

$$\therefore T_2 = Z * R_2 = -91.62 * 3.28 = -300.51 \text{ kN/m Comp.}$$

T_1 & T_2 distribution For the Cone.

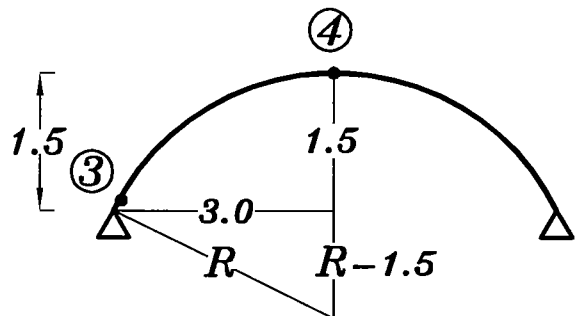


Dome.

$$R^2 = 3.0^2 + (R - 1.5)^2$$

$$R^2 = 9.0 + R^2 - 3R + 2.25$$

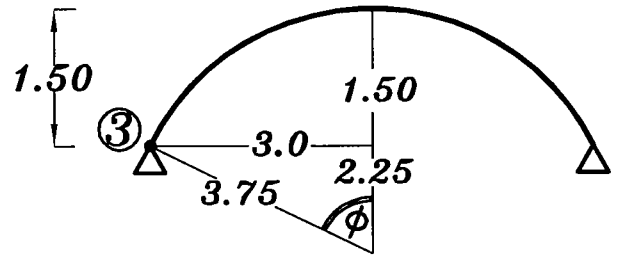
$$3R = 11.25 \rightarrow \boxed{R = 3.75 \text{ m}}$$



Sec. ③

$$\cos \phi = \frac{2.25}{3.75} \rightarrow \boxed{\phi = 53.13^\circ}$$

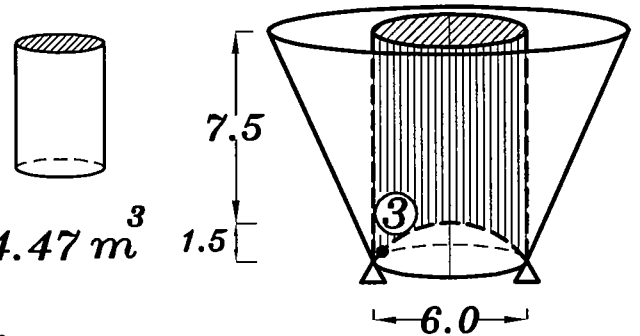
$$r = 3.0 \text{ m}$$



$$S.A. = 2\pi * R * h \quad \text{[Diagram of a dome section]} = 2\pi * 3.75 * 1.50 = 35.34 \text{ m}^2$$

$$\text{Volume of Cylinder} = \pi * r^2 * h$$

$$= \pi * 3.0^2 * 9.0 = 254.47 \text{ m}^3$$



$$\text{Volume of Dome} = \frac{\pi * h}{6} (3r^2 + h^2) \quad \text{[Diagram of a dome section]}$$

$$= \frac{\pi * 1.5}{6} (3 * 3.0^2 + 1.5^2) = 22.97 \text{ m}^3$$

$$\text{Volume of Water}$$



$$= 254.47 - 22.97 = 231.5 \text{ m}^3$$



$$W_\phi = g * S.A. + \gamma_w * \text{Volume}$$

$$= 4.0 * 35.34 + 10.0 * 231.5 = 2456.36 \text{ kN}$$

$$T_1 = \frac{W_\phi}{2\pi r \sin \phi} = \frac{+2456.36}{2\pi * 3.0 * \sin 53.13^\circ} = +162.90 \text{ kN/m Comp.}$$

$$R_1 = R_2 = R = 3.75 \text{ m}$$

$$Z = g \cos \phi + \gamma_w * h = 4.0 * \cos 53.13^\circ + 10 * 9.0 = +92.40 \text{ kN/m}^2$$

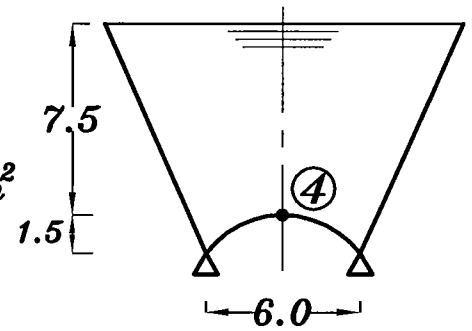
$$\therefore T_1 + T_2 = Z * R \quad \therefore +162.90 + T_2 = 92.40 * 3.75$$

$$\therefore T_2 = +183.6 \text{ kN/m Comp.}$$

Sec. ④ $\phi = \text{Zero}$

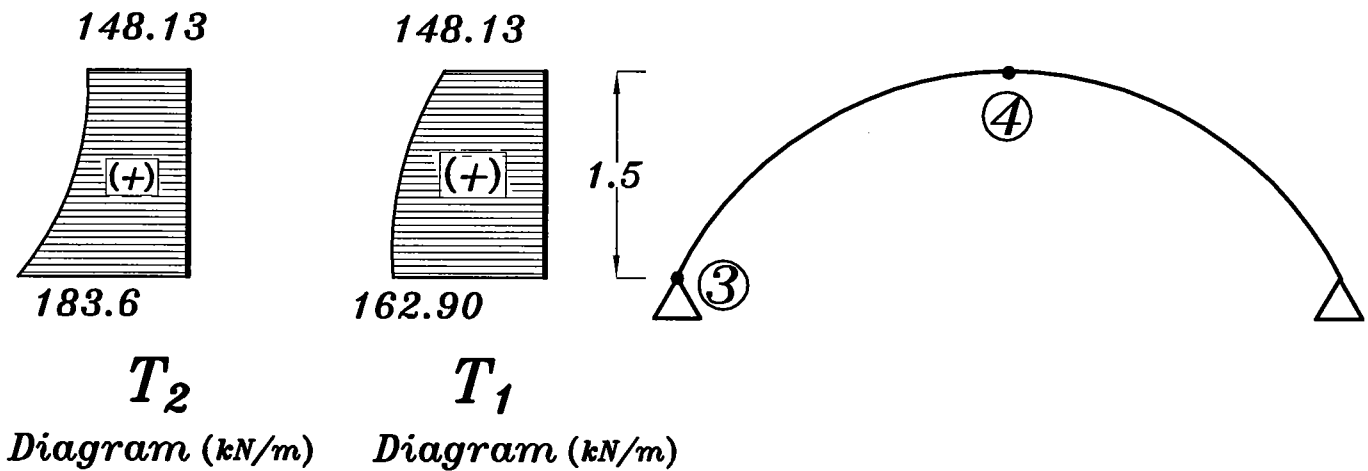
$$Z = g \cos \phi + \delta_w * h$$

$$= 4.0 * \cos 0.0 + 10 * 7.5 = +79.0 \text{ kN/m}^2$$



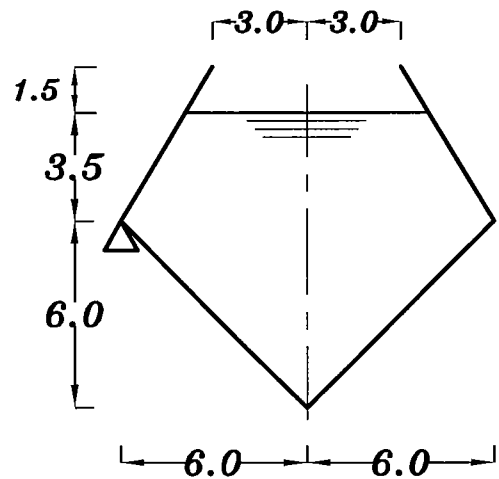
$$T_1 = T_2 = \frac{RZ}{2} = \frac{3.75 * 79.0}{2} = +148.13 \text{ kN/m Comp.}$$

T_1 & T_2 distribution For the Dome.



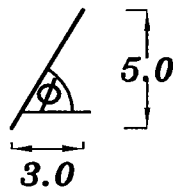
Example.

Draw T_1 & T_2 distribution
on the vertical projection.
due to dead load & water pressure.
 $t_s = 0.20 \text{ m}$



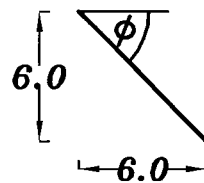
$$\text{Dead Load} = g = t_s \gamma_c = 0.20 * 25 = 5.0 \text{ kN/m}^2$$

First Cone.

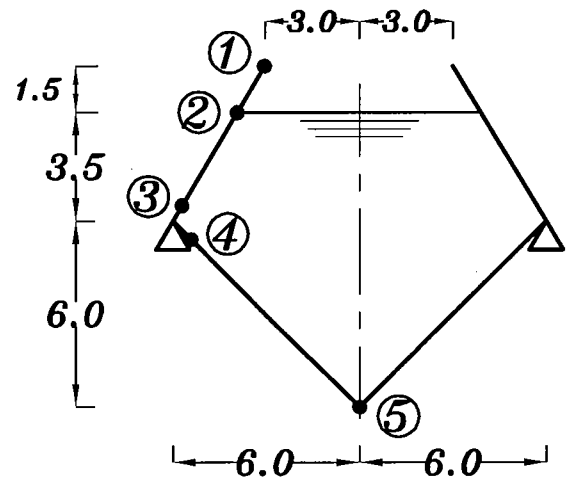


$$\tan \phi = \frac{5.0}{3.0} \rightarrow \boxed{\phi = 59.04^\circ}$$

Second Cone.



$$\tan \phi = \frac{6.0}{6.0} \rightarrow \boxed{\phi = 45.0^\circ}$$



Sec. ① $r = 3.0 \text{ m}$

$$W_\phi = \text{Zero} \rightarrow T_1 = \text{Zero}$$

$$Z = g \cos \phi = 5.0 * \cos 59.04^\circ = +2.572 \text{ kN/m}^2$$

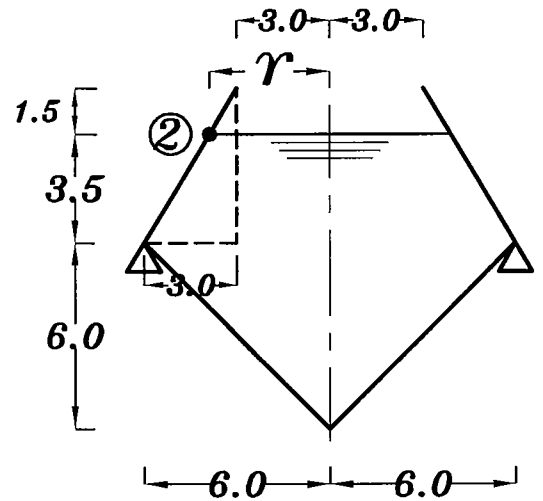
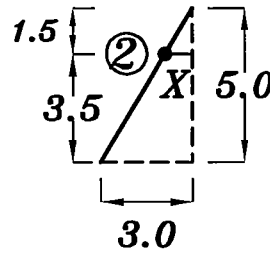
$$R_2 = \frac{r}{\sin \phi} = \frac{3.0}{\sin 59.04^\circ} = 3.50 \text{ m}$$

$$T_2 = Z * R_2 = +2.572 * 3.50 = +9.0 \text{ kN/m Comp.}$$

Sec. ②

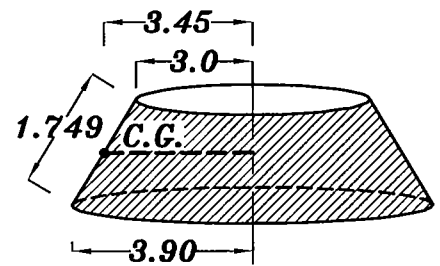
$$\frac{1.5}{5.0} = \frac{X}{3.0} \rightarrow X = 0.9 \text{ m}$$

$$r = 3.0 + 0.9 = 3.90 \text{ m}$$



$$S.A. = L * 2 \pi * R_{C.G.}$$

$$= 1.749 * 2 \pi * 3.45 = 37.91 \text{ m}^2$$



$$W_{\phi} = g * S.A. = 5.0 * 37.91 = + 189.55 \text{ kN}$$

$$T_1 = \frac{W_{\phi}}{2 \pi r \sin \phi} = \frac{+ 189.55}{2 \pi * 3.90 * \sin 59.04^{\circ}} = + 9.02 \text{ kN/m Comp.}$$

$$Z = g \cos \phi = 5.0 * \cos 59.04^{\circ} = + 2.572 \text{ kN/m}^2$$

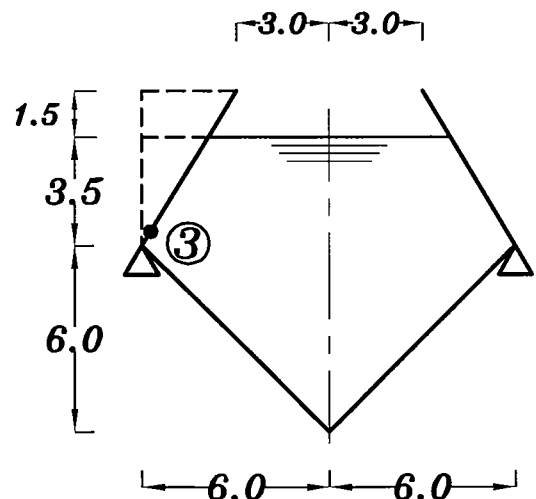
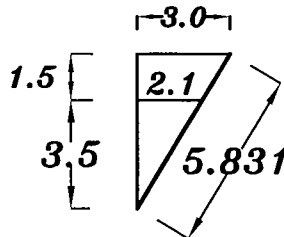
$$R_2 = \frac{r}{\sin \phi} = \frac{3.90}{\sin 59.04^{\circ}} = 4.548 \text{ m}$$

$$T_2 = Z * R_2 = 2.572 * 4.548 = + 11.70 \text{ kN/m Comp.}$$

Sec. ③

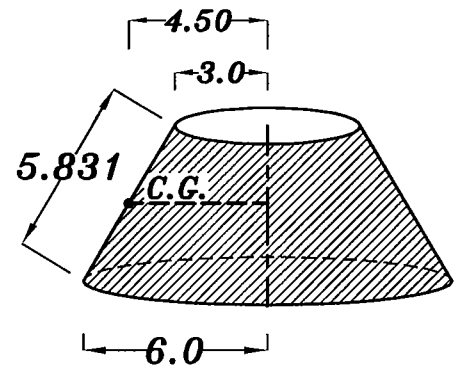
$$r = 6.0 \text{ m}$$

$$\phi = 59.04^{\circ}$$

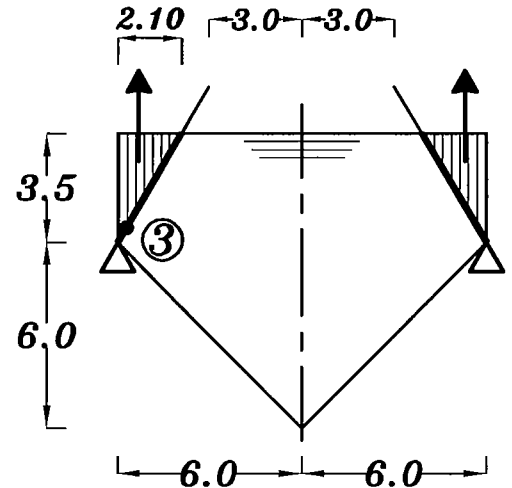
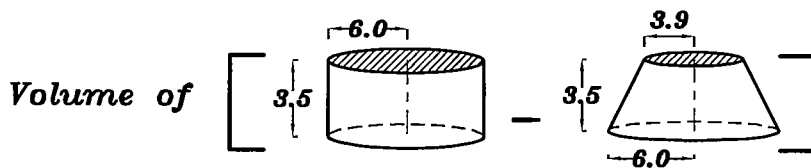


$$S.A. = L * 2 \pi * R_{c.g.}$$

$$= 5.831 * 2 \pi * 4.50 = 164.86 m^2$$



Volume



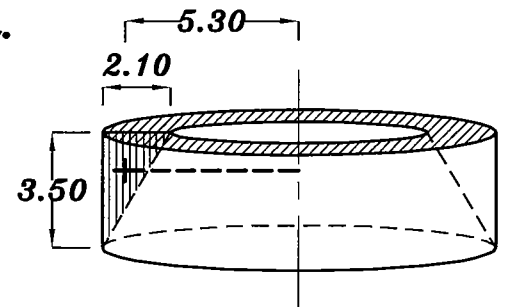
$$Volume = \left[\pi r^2 * h - \frac{\pi h}{3} (a^2 + b^2 + ab) \right]$$

$$= \left[\pi * 6.0^2 * 3.5 - \frac{\pi * 3.5}{3} (3.9^2 + 6.0^2 + 3.9 * 6.0) \right]$$

$$= 122.38 m^3$$

Or we can get the volume From.

$$Volume = Area * 2 \pi * R_{c.g.}$$



$$Volume = \left(\frac{1}{2} * 2.10 * 3.50 \right) * 2 \pi * 5.30 = 65.43 m^3$$

$$= 122.38 m^3$$

$$W\phi = g * S.A. \downarrow - \gamma_w * Volume \uparrow$$

$$= 5.0 * 164.86 - 10.0 * 122.38 = -399.5 \text{ kN} \uparrow$$

تم طرح القيمتين من بعضهما لان وزن السطح ($g * S.A.$) يؤثر رأسيا لأسفل بينما ضغط الماء ($\gamma_w * Volume$) يؤثر رأسيا لأعلى .

$$T_1 = \frac{W\phi}{2\pi r \sin\phi} = \frac{-399.5}{2\pi * 6.0 * \sin 59.04^\circ} = -12.36 \text{ kN/m Comp.}$$

$$Z = g \cos\phi \searrow - \gamma_w * h \swarrow$$

$$= 5.0 * \cos 59.04^\circ - 10 * 3.5 = -32.43 \text{ kN/m}^2$$

$$R_2 = \frac{r}{\sin\phi} = \frac{6.0}{\sin 59.04^\circ} = 7.0 \text{ m}$$

$$\therefore T_2 = Z * R_2 = -32.43 * 7.0 = -227.0 \text{ kN/m Ten.}$$

Sec. ④

$$r = 6.0 \text{ m}$$

$$\phi = 45.0^\circ$$

$$S.A. = \pi * r * L$$



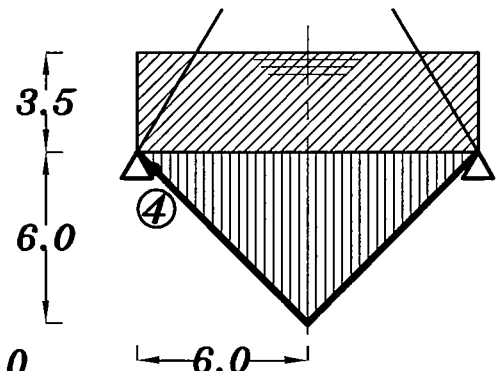
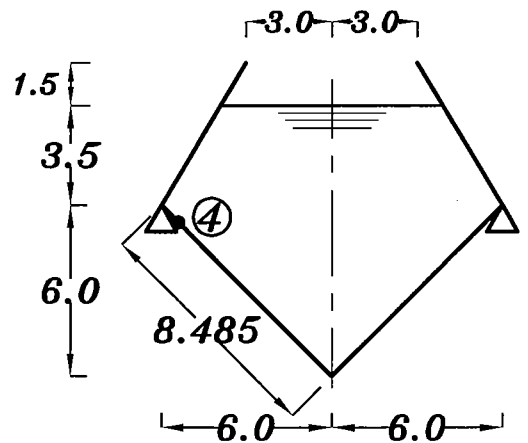
$$= \pi * 6.0 * 8.485 = 159.93 \text{ m}^2$$

$$Volume \left[\begin{array}{c} 3.5 \\ \text{cylinder} \\ 6.0 \end{array} + \begin{array}{c} 6.0 \\ \text{cone} \\ 6.0 \end{array} \right]$$

$$Volume = \pi r^2 * h + \frac{1}{3} * \pi * r^2 * h$$

$$= \pi * 6.0^2 * 3.5 + \frac{1}{3} * \pi * 6.0^2 * 6.0$$

$$= 622.03 \text{ m}^3$$



$$W_{\phi} = g * S.A. + \gamma_w * Volume$$

$$= 5.0 * 159.93 + 10.0 * 622.03 = -7019.95 \text{ kN}$$

اشاره W_{ϕ} (-Ve) لان اتجاها خارج من ال Support

$$T_1 = \frac{W_{\phi}}{2\pi r \sin \phi} = \frac{-7019.95}{2\pi * 6.0 * \sin 45^{\circ}} = -263.36 \text{ kN/m Ten.}$$

$$Z = g \cos \phi + \gamma_w * h$$

$$= 5.0 * \cos 45^{\circ} + 10 * 3.5 = -38.53 \text{ kN/m}^2$$

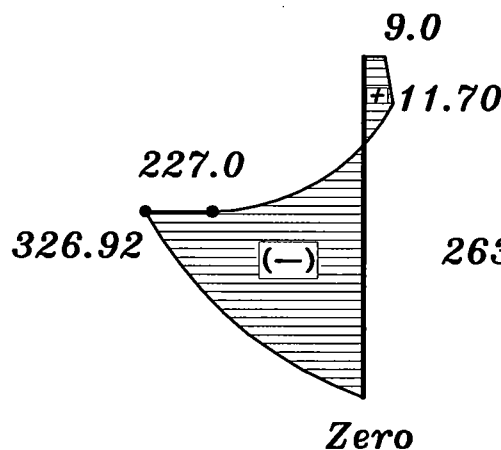
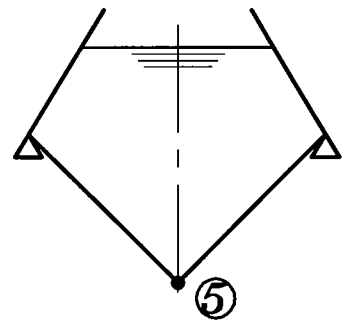
اشاره Z (-Ve) لان اتجاها خارج من المحور

$$R_2 = \frac{r}{\sin \phi} = \frac{6.0}{\sin 45^{\circ}} = 8.485 \text{ m}$$

$$\therefore T_2 = Z * R_2 = -38.53 * 8.485 = -326.92 \text{ kN/m Ten.}$$

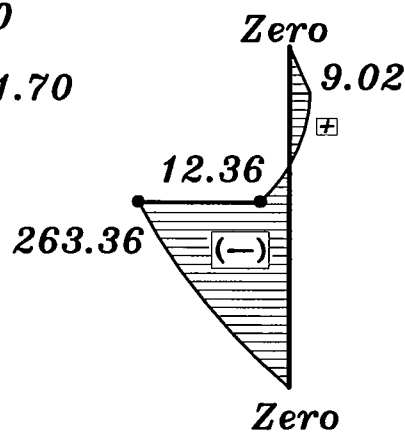
Sec. ⑤ Vertex of the Cone.

$$T_1 = T_2 = \text{Zero}$$



T_2

Diagram (kN/m)



T_1

Diagram (kN/m)

